

PDF4LHC2021

Benchmarking

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On behalf of PDF4LHC Collaboration

DIS 2021 Workshop



Outline

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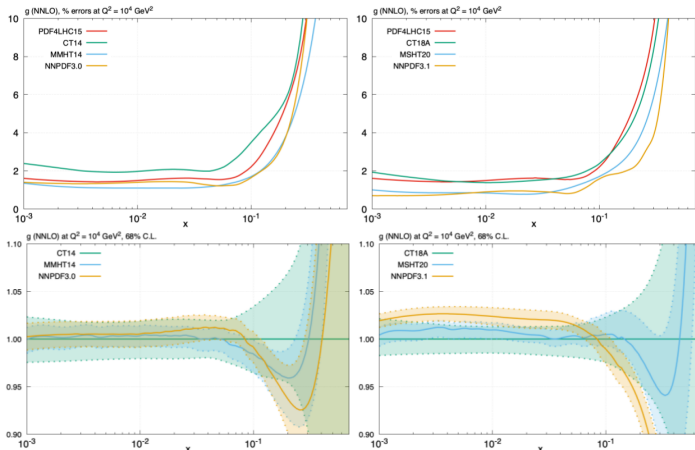
Work undertaken through many useful discussions, many thanks to all members involved.

Introduction - PDF Landscape

- PDF4LHC15 was a 1 year benchmarking exercise of the CT14, MMHT14, NNPDF3.0 PDFs which resulted in a combination set.
- It has now been more than 5 years since the PDF4LHC15 benchmarking exercise.
- Increasing amounts of data coming out of the LHC, greater precision, more channels, more differential \Rightarrow many changes in PDFs.
- In addition there have been theoretical improvements \Rightarrow full NNLO predictions, and methodological improvements (parameterisations, algorithms, etc).
- PDFs now known more accurately and precisely than ever before, but some differences remain \Rightarrow benchmarking needed.
- We consider 3 global PDF fits most recent sets, which include much of the recent datasets: MSHT20, CT18, NNPDF3.1.

Introduction - Changes in PDFs

Gluon



- **Reduction in PDF uncertainties** seen across all 3 groups.
- **Central value agreement not as good**, some differences emerging.

Note: CT18A shown for ease of comparison, however CT18 is the default set.

Plots from L.
Harland-Lang

PDF Benchmarking: Aim and Approach

- New PDFs **CT18**, **MSHT2020**, **NNPDF3.1** \Rightarrow now is a good time to undertake a **benchmarking exercise**, examine and understand differences ahead of a new **PDF4LHC future combination**.
- End result of exercise will be a **PDF4LHC21** set of PDFs.
- Desire to understand **origin of differences**:
 - ▶ Are they due to **variations of experimental input, different theory settings, methodologies**? Are these equally valid choices?
- Seek to **remove as many differences in input/approach as possible**:
 - ▶ **Common input data** - Small subset of datasets \Rightarrow **reduced fits**.
 - ▶ **Common theory** settings wherever possible.
 - ▶ Examine methodological differences in parallel as much as possible.
- Reduced fits offer *ease of comparison at expense of robustness*.
- To benchmark the reduced fits:
 - ▶ Compare **PDFs** directly to look for areas of difference.
 - ▶ Compare χ^2 to determine particular datasets showing differences.
 - ▶ Compare cross-sections and point-by-point **theory predictions**.

PDF Benchmarking: Datasets

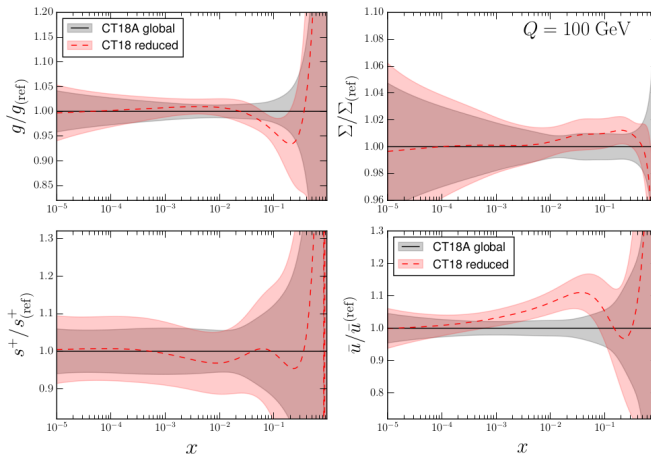
- Chosen subset of datasets fit by all 3 groups in (almost) the same way, list is surprisingly small! **Small reduced fit set.**
- Take **most conservative cuts** applied by any group for consistency.
- Ensure enough datasets and a sufficient variety of dataset types are fit to have **some** (but incomplete) **constraints on all PDF flavours.**
- Overall list:
 - ▶ NMC deuteron to proton ratio in DIS.
 - ▶ NuTeV dimuon cross-sections.
 - ▶ HERA I+II inclusive cross-sections from DIS.
 - ▶ E866 fixed target Drell-Yan ratio pd/pp data.
 - ▶ D0 Z rapidity distribution.
 - ▶ ATLAS W, Z 7 TeV rapidity distribution, only Z peak and central.
 - ▶ CMS 7 TeV W asymmetry.
 - ▶ CMS 8 TeV inclusive jet data.
 - ▶ LHCb 7, 8 TeV W, Z rapidity distributions.
 - ▶ BCDMS proton and deuteron DIS data.

PDF Benchmarking: Theory Settings

- Choose **common theory settings** for simplicity:
 - ▶ Same heavy quark masses ($m_c = 1.4\text{GeV}$, $m_b = 4.75\text{GeV}$) and $\alpha_S(M_Z^2) = 0.118$.
 - ▶ No strangeness asymmetry at input scale: $(s - \bar{s})(Q_0) = 0$.
 - ▶ Perturbative charm.
 - ▶ Positive definite quark distributions (lack of constraint may allow negative fluctuations).
 - ▶ No deuteron or nuclear corrections.
 - ▶ Fixed branching ratio for charm hadrons to muons.
 - ▶ NNLO corrections for dimuon data.
- Note: These are not the chosen settings for any one group, but rather are a compromise to the least common denominator in each case, *we would not recommend them for a full global fit*.

Reduced Fits: CT18 changes - central values

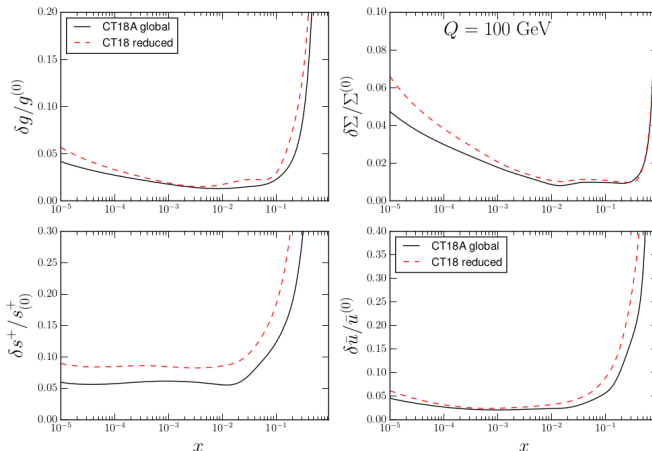
- Current Status:



- Good compatibility with some increase in \bar{u} , and change in high x gluon shape. Some changes in flavour decomposition.

Reduced Fits: CT18 changes - uncertainties

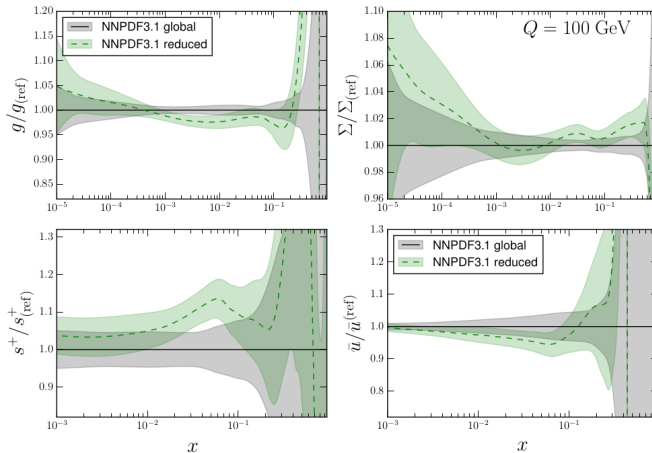
- Current Status:



- Some increase in *nominal* PDF uncertainties, particularly at low x .

Reduced Fits: NNPDF3.1 changes - central values

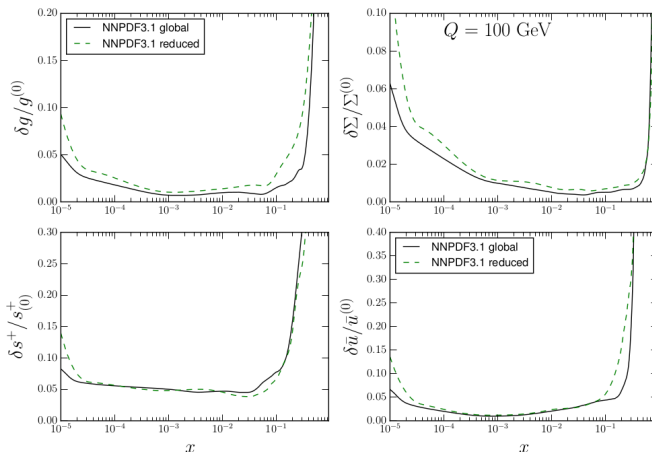
- Current Status:



- Good compatibility, changes in strangeness (see later) and change in large x gluon (removal of top data, addition of CMS 8 TeV jet).

Reduced Fits: NNPDF3.1 changes - uncertainties

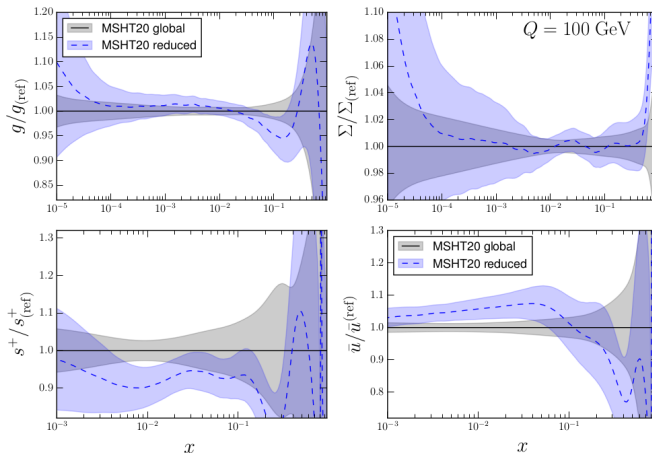
- Current Status:



- Generally **slightly increased uncertainties**, particularly for the **gluon**.

Reduced Fits: MSHT20 changes - central values

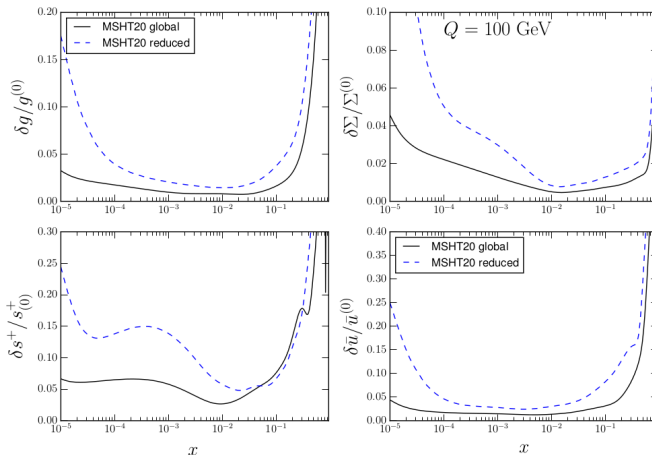
- Current Status:



- Good compatibility, changes in strangeness (removal of 8 TeV ATLAS W, Z data), flavour decomposition and large x gluon.

Reduced Fits: MSHT20 changes - uncertainties

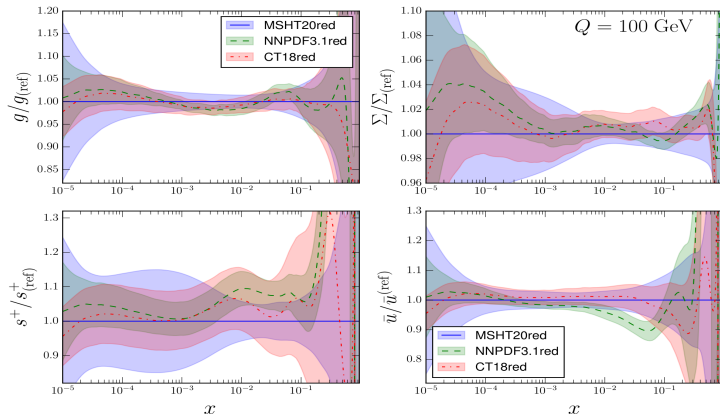
- Current Status:



- General marked **increase in uncertainties** of reduced fit, particularly **outside of regions where there are data**.

Reduced Fits PDF Comparison - central values

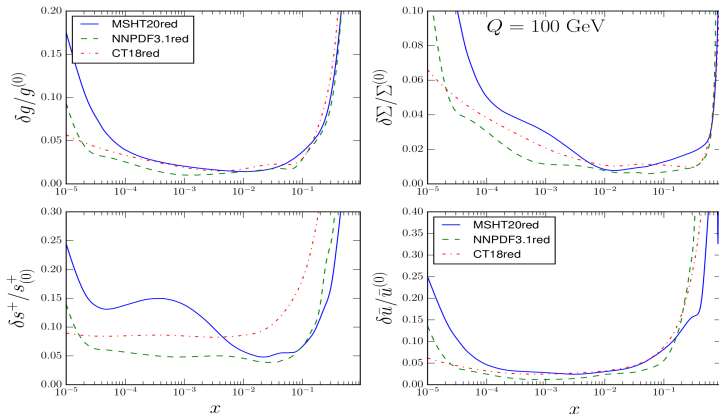
- Current Status:



- Good general agreement within uncertainties, perhaps with the exception of high x flavour decomposition of NNPDF.
- Nonetheless, strangeness and flavour decomposition improved through benchmarking (NuTeV - later). *Note this is without the $t\bar{t}$ added.

Reduced Fits PDF Comparison - uncertainties

- Current Status:



- Similar size uncertainties in data regions, MSHT generally larger errors where constraints lacking in reduced fit.
- Parallel study into differences in uncertainty bands ongoing.

*Note this is without the $t\bar{t}$ added.

PDF4LHC15 in Predictions Datasets χ^2 Comparison

- First make predictions with PDF4LHC15 PDFs, identifies any differences in theory/data between groups with fixed PDFs.

- Current status:

Table from T. Hobbs

ID	Expt.	N_{pt}	χ^2/N_{pt} (CT)	χ^2/N_{pt} (MSHT)	χ^2/N_{pt} (NNPDF)
101	BCDMS F_2^p	329/163 ^{††} /325 [†]	1.35	1.2	1.51
102	BCDMS F_2^d	246/151 ^{††} /244 [†]	0.97	1.27	1.24
104	NMC F_2^d/F_2^p	118/117 [†]	0.92	0.93	0.94
124+125	NuTeV $\nu\mu\mu + \bar{\nu}\mu\mu$	38+33	0.75	0.73	0.84
160	HERAI+II	1120	1.27	1.24	1.74
203	E866 $\sigma_{pd}/(2\sigma_{pp})$	15	0.45	0.54	0.59
245+250	LHCb 7TeV& 8TeV W, Z	29+30	1.5	1.34	1.76
246	LHCb 8TeV $Z \rightarrow ee$	17	1.35	1.65	1.25
248	ATLAS 7TeV W, Z (2016)	34	6.71	7.46	6.51
260	D0 Z rapidity	28	0.61	0.58	0.61
267	CMS 7TeV electron A_{ch}	11	0.45	0.5	0.73
269	ATLAS 7TeV W, Z (2011)	30	1.21	1.23	1.31
545	CMS 8TeV incl. jet	185/174 ^{††}	1.53	1.89	1.78
Total	N_{pt}	—	2263	1991	2256
Total	χ^2/N_{pt}	—	1.31	1.36	1.62

- Similar overall quality of fit for MSHT and CT in χ^2/N , NNPDF significantly larger χ^2/N .
- Differences in some datasets:
 - Difference in NNPDF HERA χ^2 - flavour scheme, disappears in fit.

Reduced Fits Datasets χ^2 Comparison

- Current status:

ID	Expt.	N_{pt}	χ^2/N_{pt} (CT)	χ^2/N_{pt} (MSHT)	χ^2/N_{pt} (NNPDF)
101	BCDMS F_2^p	329/163 ^{††} /325 [†]	1.06	1.00	1.21
102	BCDMS F_2^d	246/151 ^{††} /244 [†]	1.06	0.88	1.10
104	NMC F_2^d/F_2^p	118/117 [†]	0.93	0.93	0.90
124+125	NuTeV $\nu\mu\mu + \bar{\nu}\mu\mu$	38+33	0.79	0.83	1.22
160	HERAI+II	1120	1.23	1.20	1.22
203	E866 $\sigma_{pd}/(2\sigma_{pp})$	15	1.24	0.80	0.43
245+250	LHCb 7TeV& 8TeV W, Z	29+30	1.15	1.17	1.44
246	LHCb 8TeV $Z \rightarrow ee$	17	1.35	1.43	1.57
248	ATLAS 7TeV W, Z (2016)	34	1.96	1.79	2.33
260	D0 Z rapidity	28	0.56	0.58	0.62
267	CMS 7TeV electron A_{ch}	11	1.47	1.52	0.76
269	ATLAS 7TeV W, Z (2011)	30	1.03	0.93	1.01
545	CMS 8TeV incl. jet	185/174 ^{††}	1.03	1.39	1.30
Total	N_{pt}	—	2263	1991	2256
Total	χ^2/N_{pt}	—	1.14	1.15	1.20

- Similar overall quality of fit in χ^2/N .

- Differences remaining in some datasets:

- ▶ NuTeV agreement improved but difference remains, seen in $s + \bar{s}$.
- ▶ Some potential differences in ATLAS 7 TeV W, Z and LHCb?
- ▶ Some differences in NNPDF fit quality to small datasets.

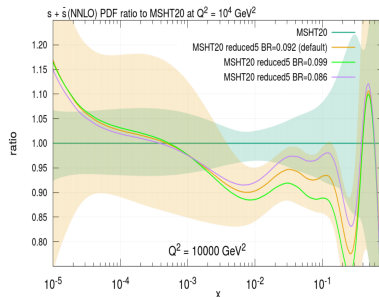
Table from T. Hobbs

Flavour Decomposition - Strangeness and NuTeV

- One of the main differences between the first reduced sets was in the **flavour decomposition and strangeness**.
- NuTeV dimuon data key driver of this, complicated dataset:
 - Requires knowledge of **charm** \rightarrow **hadrons branching ratio (BR)**.
 - Non-isoscalar** nature of target.
 - Prefers non-zero strangeness asymmetry.
 - Acceptance corrections** required.
- $BR(c \rightarrow \mu)$ anti-correlated with total strangeness, **3 groups have different default values**:
 - NNPDF 0.086 ± 0.05
 - MSHT 0.092 ± 0.1 variable.
 - CT 0.099, normalisation uncertainty.

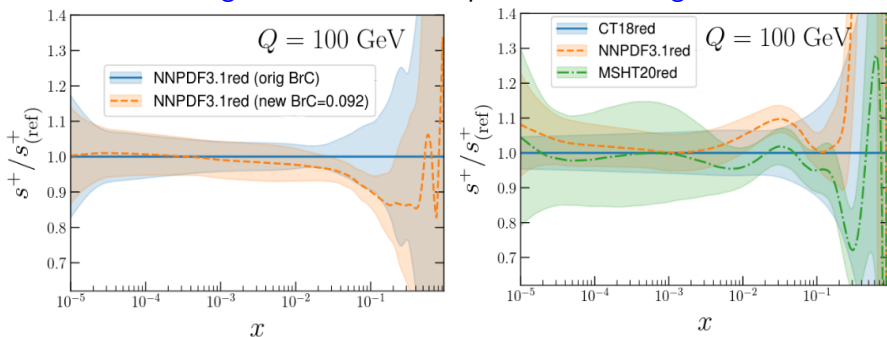
- MSHT20 reduced fit χ^2/N :

Dataset /BR	0.086	0.092	0.099
NuTeV Dimuon	58.8/71	49.6/71	68.5/71
ATLAS 7 TeV W, Z	60.8/34	65.1/34	57.1/34



Flavour Decomposition - Strangeness and NuTeV

- Setting all variables the same in all 3 fits - same **Dimuon BR fixed at 0.092**, all treat non-isoscalarity, same acceptance corrections.
- **NNPDF strangeness reduced** as expected, **CT strangeness increases**.



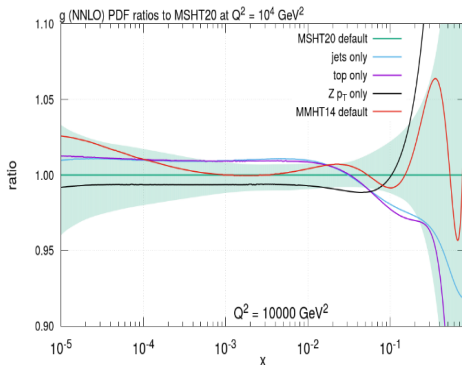
- **Better strangeness agreement**, certainly in data region, now largely within uncertainties between all 3 groups.
- Also aids reduction in flavour decomposition differences.

Plots from J. Rojo

High x gluon

- High x gluon of interest to both reduced and global fits.

- 3 main datasets play a role here - jet data, top data, Zp_T data, different pulls:
- Not straightforward to fit some of them:
 - ▶ Difficulties fitting all bins.
 - ▶ Possible tensions.
 - ▶ Issue of correlated systematics.



- MSHT, CT, NNPDF observe differences in the relative importance of these datasets and the quality of their individual fits
- *does the same hold in reduced fits and can we understand this better in this context?*

ATLAS 8 TeV multi-differential $t\bar{t}$ lepton+jets

- Comes differential in 4 variables with statistical and systematic correlations - $m_{t\bar{t}}, y_t, y_{t\bar{t}}, p_t^T$.
- MSHT*, CT⁺ difficulties fitting all 4 distributions simultaneously.
- MSHT, CT, ATLAS⁻ cannot get good fit to y_t or $y_{t\bar{t}}$ individually.
- NNPDF however able to fit all 4 distributions well individually [†].

Benchmarking:

- Start by adding this to the reduced fit, first check theory predictions for PDF4LHC15 read in (no fitting):
 - Data agree and theory agrees to better than 1%.
 - All groups χ^2 in agreement and follow same pattern:

Distribution/N	MSHT	CT	NNPDF
$p_t^T/8$	3.0	3.1	3.4
$y_t/5$	10.6	10.1	9.5
$y_{t\bar{t}}/5$	17.6	15.3	16.2
$m_{t\bar{t}}/7$	4.3	4.2	4.1

- Differences in global fits likely not from $t\bar{t}$ theory implementations.

* S. Bailey & L. Harland-Lang 1909.10541.

+ Kadir et al 2003.13740.

† Czakon et al 1611.08609.

- ATL-PHYS-PUB-2018-017.

Benchmarking ATLAS 8 TeV $t\bar{t}$ lepton+jets

- *What happens when this dataset is added to the reduced fits?*
- Two cases considered - “uncorrelated” (all systematic and statistical correlations between distributions turned off) and “correlated” (including all correlations, produces a very poor fit):

Distribution/N	$p_t^T/8$	$y_t/5$	$y_{tt}/5$	$m_{tt}/7$	Total
MSHT uncorrelated	3.9	8.4	12.5	6.4	31.2
NNPDF uncorrelated	7.2	3.9	5.1	2.5	18.7
CT uncorrelated	3.4	12.9	17.3	6.1	39.7
MSHT correlated	-	-	-	-	130.6
NNPDF correlated	-	-	-	-	122.7
MSHT decorrelated	-	-	-	-	35.3

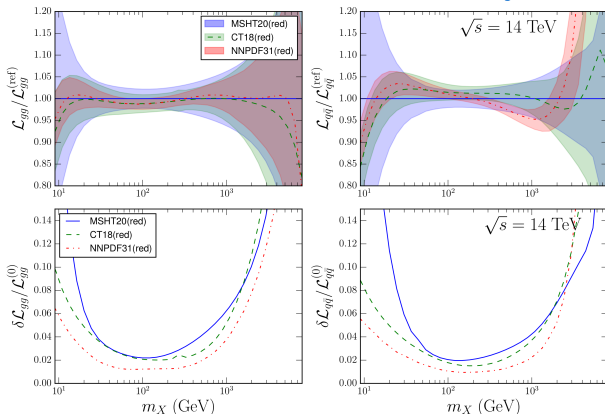
- MSHT observe usual pattern as in global fits, p_t^T and m_{tt} can be fit but y_t , y_{tt} struggle, although better than in full fit. Awful fit if all correlations included, can fit with parton shower decorrelation.
- CT see usual global fit pattern also, poor fits to rapidities y_t , y_{tt} .
- NNPDF however able to fit rapidity distributions in uncorrelated case, yet correlated case similar to MSHT.

Benchmarking ATLAS 8 TeV $t\bar{t}$ lepton+jets Preliminary!

- Potential explanations lie in **other datasets included - tensions?**
- NNPDF-4.0, will have much more jet data, sees similar issues as MSHT, CT, ATLAS for this dataset.
- Useful to **consider different jet datasets** as well as CMS 8 TeV jets.
- Potential further explanation is **division of training and validation data in NNPDF** - training fraction 50% but for small datasets such a division is unfeasible - all data in training.
- Potentially **double-weights small datasets** - e.g. ATLAS $t\bar{t}$.
- May also explain NNPDF better fit of E866 DYratio data and CMS W charge asymmetry data (15 and 11 points respectively):

Dataset	MSHT uncorrelated	NNPDF uncorrelated	MSHT uncorrelated double weight
Total	2314.1	2731.4	2313.3
χ^2/N	1.15	1.20	1.15
DYratio (15)	9.5	5.2	9.2
CMS W asym. (11)	14.2	8.2	10.2
p_t^T (8)	3.8	7.2	4.2
y_t (5)	8.4	4.3	5.8
y_{tt} (5)	12.5	5.7	7.4
m_{tt} (7)	6.4	2.4	6.5
$t\bar{t}$ total	31.2	19.6	23.9

Reduced Fits: Current Status Summary*



- **Very good agreement** in gluon-gluon, quark-quark and quark-gluon luminosities. (Latter two in backup slides).
- **Differences in quark-antiquark luminosity**, still some flavour decomposition differences, although **within MSHT uncertainties**.

*Note this is without the $t\bar{t}$ added.

Conclusions and Future Work

- Fitting reduced datasets **checks consistency between different groups**, provides an environment to analyse origin of differences.
- **Good overall consistency** is now observed in the reduced fits between the three groups involved, **particularly in luminosities**.
- Sources of **differences in strangeness in reduced fits largely identified**, currently **analysing high x gluon region** of interest.
- Some **differences in flavour decomposition** and **uncertainties** of reduced fits remain, mainly **outside of data regions**.
- Several possibilities for further investigations:
 - ▶ Continue **analysis of high x gluon differences**, consider **different jet datasets** - and their effects on both the ATLAS $t\bar{t}$ and the gluon.
 - ▶ Ongoing effort to consider **different uncertainties**.
 - ▶ **Expand reduced fits towards global fits**.
- Overall **very good progress** towards benchmarking the global fits and beyond that eventual combination \Rightarrow **PDF4LHC21**.

Many thanks to all those involved in this work/discussions, special thanks to T. Hobbs, T.-J. Hou, L. Harland-Lang, P. Nadolsky, E. Nocera, J. Rojo, R. Thorne for providing tables/plots/fits.

Backup Slides

Introduction - New Datasets (MSHT20)

LHCb W, Z data at
high rapidity

CMS $W+c$

Precision DY data

⇒ Flavour
Decomposition

LHC Jet, Zp_T , $t\bar{t}$
data

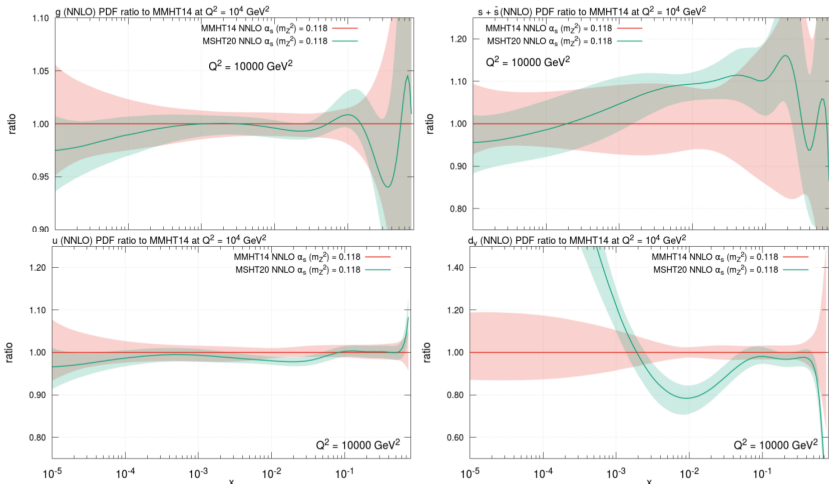
⇒ High \times gluon

Data set	Points	NLO χ^2/N_{pts}	NNLO χ^2/N_{pts}
DØ W asymmetry	14	0.94 (2.53)	0.86 (14.7)
$\sigma_{t\bar{t}}$ [93] - [94]	17	1.34 (1.39)	0.85 (0.87)
LHCb 7+8 TeV $W+Z$ [95,96]	67	1.71 (2.35)	1.48 (1.55)
LHCb 8 TeV $Z \rightarrow ee$ [97]	17	2.29 (2.89)	1.54 (1.78)
CMS 8 TeV W [98]	22	1.05 (1.79)	0.58 (1.30)
CMS 7 TeV $W+c$ [99]	10	0.82 (0.85)	0.86 (0.84)
ATLAS 7 TeV jets $R=0.6$ [18]	140	1.62 (1.59)	1.59 (1.68)
ATLAS 7 TeV $W+Z$ [20]	61	5.00 (7.62)	1.91 (5.58)
CMS 7 TeV jets $R=0.7$ [100]	158	1.27 (1.32)	1.11 (1.17)
ATLAS 8 TeV $Z p_T$ [75]	104	2.26 (2.31)	1.81 (1.59)
CMS 8 TeV jets $R=0.7$ [101]	174	1.64 (1.73)	1.50 (1.59)
ATLAS 8 TeV $t\bar{t} \rightarrow l+l$ sd [102]	25	1.56 (1.50)	1.02 (1.15)
ATLAS 8 TeV $t\bar{t} \rightarrow l^+l^-$ sd [103]	5	0.94 (0.82)	0.68 (1.11)
ATLAS 8 TeV high-mass DY [73]	48	1.79 (1.99)	1.18 (1.26)
ATLAS 8 TeV W^+W^- + jets [104]	30	1.13 (1.13)	0.60 (0.57)
CMS 8 TeV $(d\sigma_{t\bar{t}}/dp_{T,t}dy_t)/\sigma_{t\bar{t}}$ [105]	15	2.19 (2.20)	1.50 (1.48)
ATLAS 8 TeV W^+W^- [106]	22	3.85 (13.9)	2.61 (5.25)
CMS 2.76 TeV jets [107]	81	1.53 (1.59)	1.27 (1.39)
CMS 8 TeV $\sigma_{t\bar{t}}/dy_t$ [108]	9	1.43 (1.02)	1.47 (2.14)
ATLAS 8 TeV double differential Z [74]	59	2.67 (3.26)	1.45 (5.16)
Total, LHC data in MSHT20	1328	1.79 (2.18)	1.33 (1.77)
Total, non-LHC data in MSHT20	3035	1.13 (1.18)	1.10 (1.18)
Total, all data	4363	1.33 (1.48)	1.17 (1.36)

- Lots of new information constraining PDFs.

MSHT20, 2012.04684

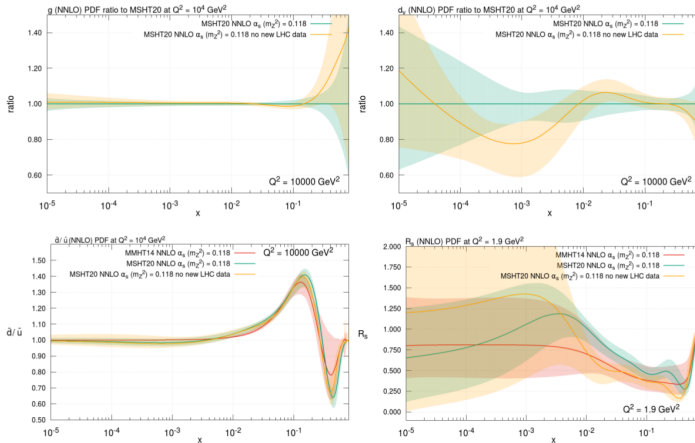
Introduction - Changes in PDFs: MSHT20



- Notable changes in **strangeness** (ATLAS W, Z data), **down valence** (new data and parameterisation), **gluon** (new jets, top, Zp_T data).

More details in R. Thorne's MSHT20 talk.

Effect of new LHC data in MSHT20



Main effect on details of flavour, i.e. d_v shape, increase in strange quark for $0.001 < x < 0.3$ and \bar{d}, \bar{u} details, though also partially from parameterisation change. Decrease in high- x gluon.

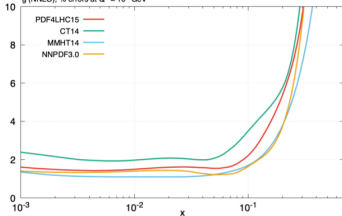
*MSHT20 2012.04684.

Slide from R. Thorne

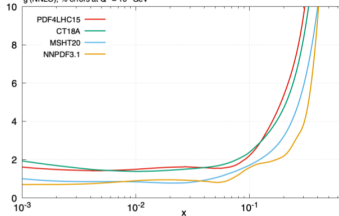
Introduction - Changes in PDFs: Uncertainties

Gluon

g (NNLO), % errors at $Q^2 = 10^4 \text{ GeV}^2$

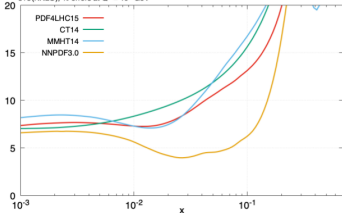


g (NNLO), % errors at $Q^2 = 10^4 \text{ GeV}^2$

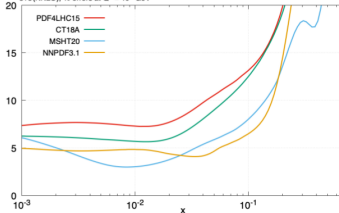


Strange

$s+\bar{s}$ (NNLO), % errors at $Q^2 = 10^4 \text{ GeV}^2$



$s+\bar{s}$ (NNLO), % errors at $Q^2 = 10^4 \text{ GeV}^2$

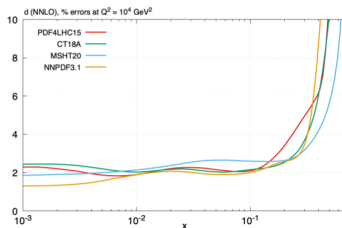
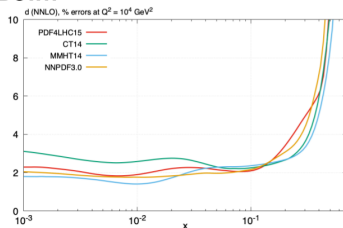


- **Reduction in PDF uncertainties** seen across all 3 groups.
Note: CT18A shown for ease of comparison, however CT18 is the default set.

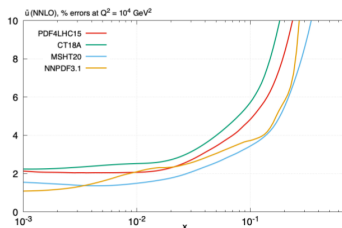
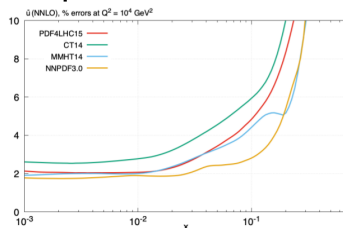
Plots from L.
Harland-Lang

Introduction - Changes in PDFs: Uncertainties

Down



Anti-up



- **Reduction in PDF uncertainties** seen across all 3 groups.

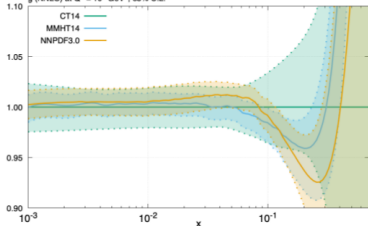
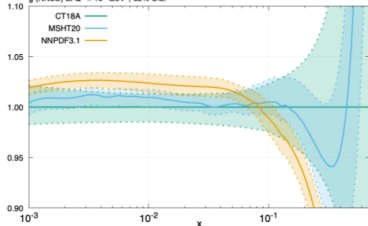
Note: CT18A shown for ease of comparison, however CT18 is the default set.

Plots from L. Harland-Lang

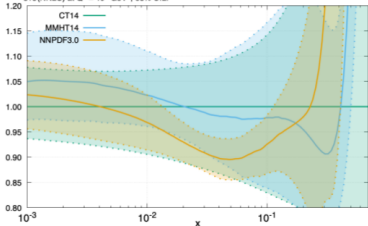
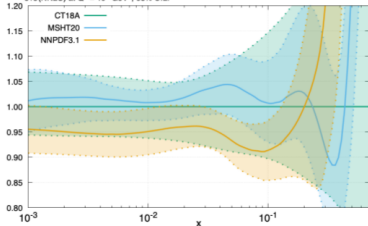
Introduction - Changes in PDFs: Central Values

Gluon

Plots from L. Harland-Lang

g (NNLO) at $Q^2 = 10^4 \text{ GeV}^2$, 68% C.L.g (NNLO) at $Q^2 = 10^4 \text{ GeV}^2$, 68% C.L.

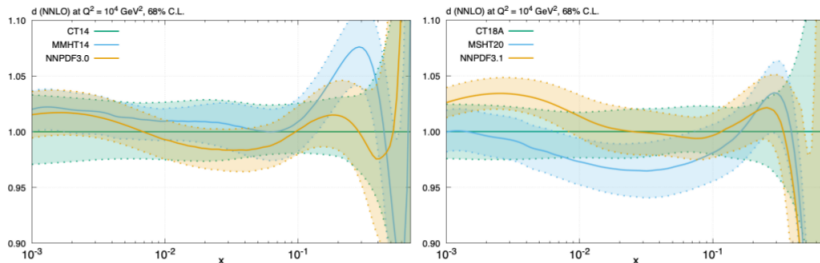
Strange

s+s̄ (NNLO) at $Q^2 = 10^4 \text{ GeV}^2$, 68% C.L.s+s̄ (NNLO) at $Q^2 = 10^4 \text{ GeV}^2$, 68% C.L.

- Central value agreement not as good, some differences emerging.

Introduction - Changes in PDFs: Central Values

Down



- Central value agreement not as good, some differences emerging.

- In summary:

- ▶ Large amount of progress since the last PDF4LHC combination on experimental, theoretical and methodological fronts.
- ▶ Some differences emerging between the 3 sets.

⇒ now is a good time to undertake a **benchmarking exercise** ahead of a new **PDF4LHC future combination**.

Plots from L. Harland-Lang

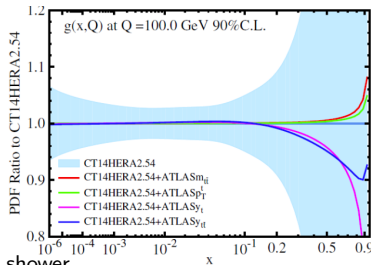
ATLAS 8 TeV multi-differential $t\bar{t}$ lepton+jets

- MSHT*, find **difficulties fitting all 4 distributions** - $m_{t\bar{t}}, y_t, y_{t\bar{t}}, p_t^T$ - simultaneously. CT find same and fit only p_t^T and $m_{t\bar{t}}$ together.
- MSHT, CT⁺, ATLAS⁻ cannot get good fit to y_t or $y_{t\bar{t}}$ individually.
- NNPDF however able to fit all 4 distributions well individually[†].
- Different pulls observed for $m_{t\bar{t}}, p_t^T$ relative to $y_t, y_{t\bar{t}}$:
- CT, MSHT decorrelate parton shower systematic to obtain reasonable fit to p_t^T and $m_{t\bar{t}}$ for former or all 4 for latter:

p_T	0.53
y_t	3.12
$y_{t\bar{t}}$	3.51
$M_{t\bar{t}}$	0.70
$p_T + M_{t\bar{t}}$	5.73
Combined	7.00

Decorrelate parton shower

(within and between)



Plot from C.-P. Yuan

Distribution	p.s. correlated	p.s. decorrelated
Combined	7.00	1.80
$p_1^t + M_{t\bar{t}}$	5.73	0.66

* S. Bailey & L. Harland-Lang 1909.10541.

† Czakon et al 1611.08609.

+ Kadir et al 2003.13740.

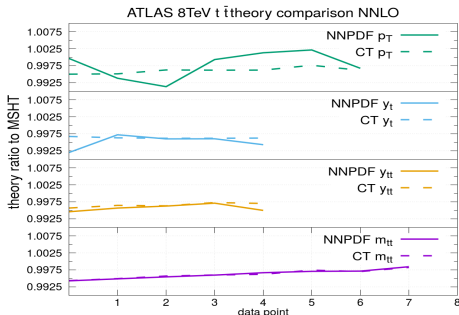
- ATL-PHYS-PUB-2018-017.

Benchmarking ATLAS 8 TeV $t\bar{t}$ lepton+jets

- Start by adding this to the reduced fit, first **check theory predictions for PDF4LHC15 read in (no fitting)**.
- Differences noted in data treatment due to shifting (MSHT) to centre of asymmetric errors, differences in theory due to inclusion (MSHT) or not (CT, NNPDF) of EW corrections.
- Upon removal of these differences, data agree and theory agrees to better than 1%.
- All groups χ^2 in agreement and follow same pattern:


Distribution/N	MSHT	CT	NNPDF
$p_t^T/8$	3.0	3.1	3.4
$y_t/5$	10.6	10.1	9.5
$y_{t\bar{t}}/5$	17.6	15.3	16.2
$m_{t\bar{t}}/7$	4.3	4.2	4.1

- Differences in global fits likely not from $t\bar{t}$ theory implementations.



ATLAS 8 TeV multi-differential $t\bar{t}$ lepton+jets: MSHT20*

- MSHT observe the rapidity y_t and y_{tt} distributions have very poor fit quality even when fit alone.
- Moreover, fitting the p_t^T and m_{tt} together or all 4 datasets combined results also in a very poor fit:

p_T	0.53	Decorrelate parton shower (within and between) 		
y_t	3.12			
y_{tt}	3.51			
M_{tt}	0.70			
$p_T + M_{tt}$	5.73			
Combined	7.00			

Distribution	p.s. correlated	p.s. decorrelated
Combined	7.00	1.80
$p_{\perp}^t + M_{tt}$	5.73	0.66

- Tensions exists between shifts required for large systematics of the different distributions, particularly parton shower uncertainty (and ISR/FSR and hard scattering systematics).
- Two-point systematic evaluated using 2 Monte Carlo generators, assuming any correlation factor determined applies fully correlated way across all bins and distributions is a strong assumption.

* S. Bailey & L. Harland-Lang 1909.10541 and MSHT20 2012.04684.

ATLAS 8 TeV multi-differential $t\bar{t}$ lepton+jets: MSHT20*

- Assumption of full correlation of parton shower systematic can be relaxed, then a reasonable fit is possible.
- CT decorrelate this systematic between distributions and fit the p_t^T and $m_{t\bar{t}}$ combination only by default †.
- MSHT do this decorrelation between all 4 distributions and also split it into 2 sources varying smoothly within each distribution:

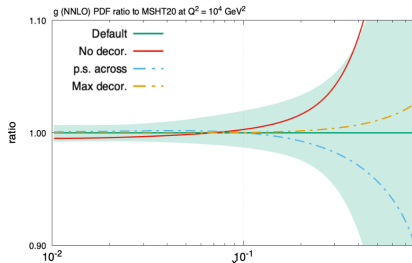
$$\beta_i^{(1)} = \cos \left[\pi \left(\frac{y_{tt,i} - y_{tt,\min}}{y_{tt,\max} - y_{tt,\min}} \right) \right] \beta_i^{\text{tot}}, \quad \beta_i^{(2)} = \sin \left[\pi \left(\frac{y_{tt,i} - y_{tt,\min}}{y_{tt,\max} - y_{tt,\min}} \right) \right] \beta_i^{\text{tot}}.$$

- Then a reasonable fit is possible, e.g. in MSHT20:

Baseline	No decor.	parton shower across	Max decor.
1.04	6.84	1.69	0.81

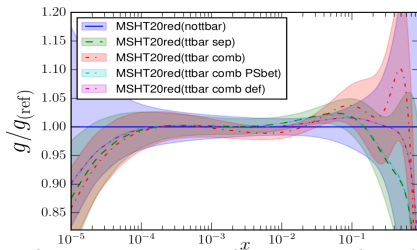
* S. Bailey & L. Harland-Lang 1909.10541 and MSHT20 2012.04684.

† T.-J. Hou et al, CT18 1912.10053.



ATLAS 8 TeV multi-differential $t\bar{t}$ lepton+jets

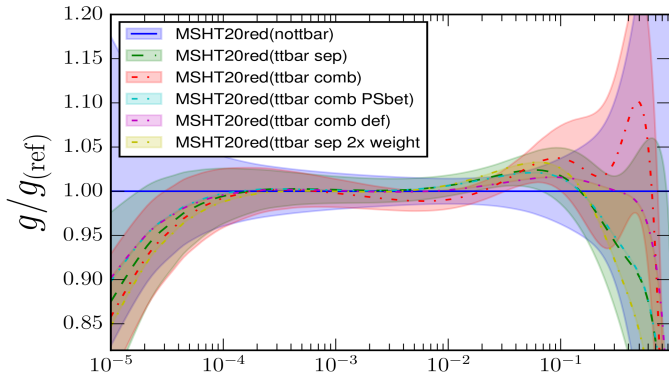
- What effect does the inclusion of this data in the reduced fit have on the gluon?



- Fitting all 4 distributions separately, uncorrelated \Rightarrow gluon moves down at high x , driven by the rapidity data.
- Applying correlations \Rightarrow gluon raised and shape altered at high x .
- Decorrelating parton shower between distributions \Rightarrow reverts the gluon to shape obtained when all 4 separately uncorrelated fitted.
- Additionally decorrelating within distributions \Rightarrow moves gluon closer to fit without $t\bar{t}$ data as its constraining power is reduced.
- Overall, gluon shape moves in direction of global fit gluon.

ATLAS 8 TeV multi-differential $t\bar{t}$ lepton+jets gluon

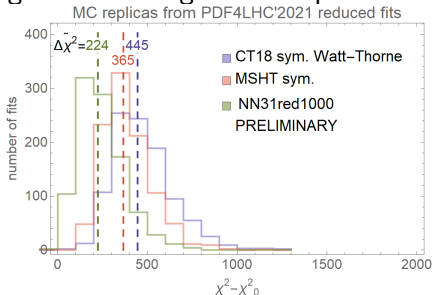
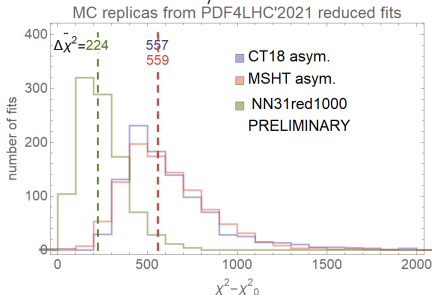
- What effect does the inclusion of this data in the reduced fit have on the gluon?



- Double weighting (yellow) pulls gluon further in direction of rapidity pull (lower at high x) as expected.

Reduced Fits χ^2 replica distributions

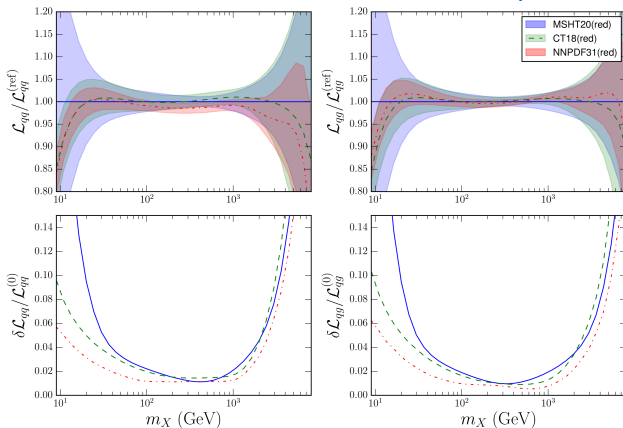
- As well as the overall PDFs, can analyse χ^2 .
- Can use CT/MSHT reduced fit eigenvectors to generate replicas.



- Overall distributions of reduced fits replicas **similar between CT and MSHT**, particularly non-symmetrised versions.
- Symmetrised versions in better agreement** with NNPDF but still different.
- Some limited qualitative agreement** at least for symmetrised case.

Plots from P. Nadolsky

Reduced Fits: Current Status Summary*



- **Very good agreement** in the gluon-gluon, quark-quark and quark-gluon luminosities.
- Differences in **quark-antiquark luminosity**, still some flavour decomposition differences, **although within MSHT uncertainties**.

*Note this is without the $t\bar{t}$ added.

Deuteron and Nuclear Corrections in MSHT20

- Several older DIS datasets use deuteron or heavy nuclear targets.
- Deuteron data required to fully separate u , d at moderate-large x .
- Heavy nuclear data, via C.C. scattering, required for more constraints on flavour decomposition and strange (dimuon data).
- Deuteron correction is 4-parameter prefactor to usual average of p and n :

$$F^d(x, Q^2) = c(x) [F^p(x, Q^2) + F^n(x, Q^2)] / 2,$$

$$c(x) = (1 + 0.01N) [1 + 0.01c_1 \ln^2(x_p/x)], \quad x < x_p,$$

$$c(x) = (1 + 0.01N) [1 + 0.01c_2 \ln^2(x/x_p) + 0.01c_3 \ln^{20}(x/x_p)], \quad x > x_p,$$

- Nuclear correction is prefactor*: *de Florian et al arXiv:1112.6324.

$$f^A(x, Q^2) = R_f(x, Q^2, A) f(x, Q^2).$$

- This is multiplied by a 3-parameter modification function to allow penalty-free change in shape and/or normalisation.
- Both deuteron and nuclear corrections prefer modifications of 1%.
More details on all of this in MMHT14 1412.3989, MSHT20 2012.04684.

Future Work

- Several possibilities for further investigations:
 - ▶ Continue **analysis of high x gluon differences**, consider **different jet datasets** - and their effects on both the ATLAS $t\bar{t}$ and the gluon.
⇒ Of interest to both reduced fit benchmarking and global fits.
 - ▶ Further work perhaps to identify source of **flavour decomposition differences**?
 - ▶ Ongoing effort to consider different uncertainties - CT implementing MSHT dynamic tolerance to analyse **reduced fit uncertainty differences**. Could repeat for NNPDF by generating Hessian set.
 - ▶ **Expand reduced fits towards global fits** to see how any remaining differences alter.
- Once this is done we can consider a combination of the global fit PDFs ⇒ PDF4LHC21.

Conclusions

- Fitting reduced datasets is a good mechanism to **check consistency between different groups**, provides an environment where any differences in treatment are more relevant to the overall PDFs.
- Allows analysis of origin of differences \Rightarrow are they due to different, equally valid choices in theoretical, methodological or data approaches.
- **Good overall consistency** found between the three groups involved, **particularly in luminosities**.
- Sources of **differences in strangeness in reduced fits largely identified**, currently **analysing high x gluon region** of interest.
- Some **differences in flavour decomposition** and **uncertainties** remain, mainly **outside of data regions**.
- Overall **very good progress** towards benchmarking the global fits and beyond that eventual combination.

Many thanks to all those involved in this work/discussions, special thanks to T. Hobbs, T.-J. Hou, L. Harland-Lang, P. Nadolsky, E. Nocera, J. Rojo, R. Thorne for providing tables/plots/fits.