

JAM-small $\times$ Helicity Phenomenology

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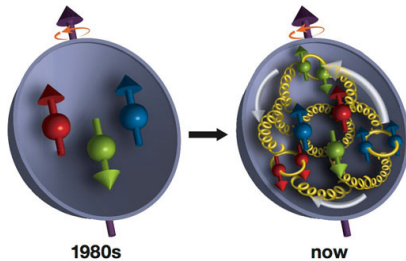
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DIS 2021

Proton Spin Problem



Spin Sum Rule

Jaffe-Manohar Spin Sum Rule:

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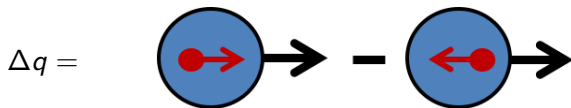
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We can calculate (most) of $\mathbf{S}_q$

Helicity Parton Distribution Functions

$$S_q(Q^2) = \frac{1}{2} \int_0^1 dx \sum_q (\Delta q(x, Q^2) + \Delta \bar{q}(x, Q^2))$$

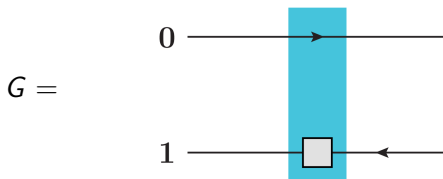


- Q^2 resolution at which we probe the proton
- $x \propto \frac{1}{s}$, we need theory to find the dependence of

Calculating Helicity Distributions

Helicity distributions are computed from the polarized dipole amplitude

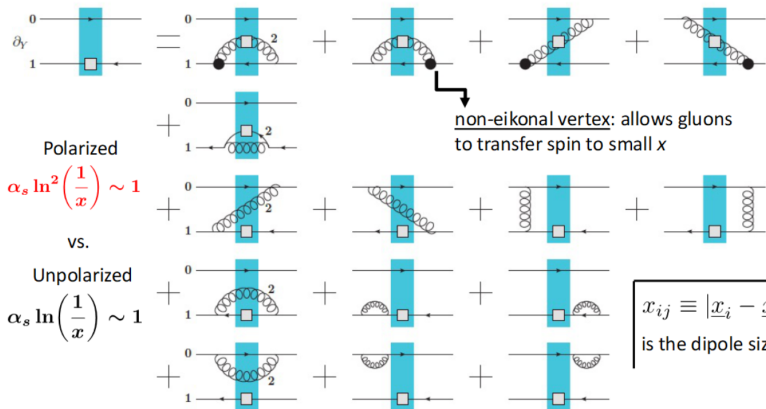
$$\Delta q(x, Q^2) + \Delta \bar{q}(x, Q^2) = \frac{N_c}{2\pi^3} \int_0^{\ln \frac{Q^2}{x\Lambda^2}} d\eta \int_{\max\{0, \ln \frac{1}{x}\}}^{\eta} ds_{10} G_q(s_{10}, \eta)$$



- Rapidity, $\eta = \ln \frac{zs}{\Lambda^2}$, z = momentum fraction of quark
- Log of transverse momentum, $s_{10} = \ln \frac{1}{x_{10}^2 \Lambda^2}$, x_{10} separation between quarks

Helicity Dependent Processes

Small- x helicity (KPS) evolution involves the “polarized dipole amplitude” (Kovchegov, Pitonyak, Sievert: JHEP 1601 (2016), PRL 118 (2017), PRD 95 (2017), PLB 772 (2017), JHEP 1710 (2017); Kovchegov & Sievert PRD 99 (2019); Kovchegov & Cougoulic PRD 100 (2019))



Evolution of polarized dipole amplitude closes in the large N_c limit:

$$G_q(s_{10}, \eta) = G_q^{(0)}(s_{10}, \eta) + \frac{\alpha_s N_c}{2\pi} \int_{s_{10}}^{\eta} d\eta' \int_{s_{10}}^{\eta'} ds_{21} [\Gamma_q(s_{10}, s_{21}, \eta') + 3G_q(s_{21}, \eta')]$$

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- $\Gamma_q(s_{10}, s_{21}, \eta')$ is an auxiliary function which obeys a separate integral equation that mixes with G .

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Constraining the initial condition

What enters observables are linear combinations of hPDFS

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- Three relevant hPDFs in DIS: Δu^+ , Δd^+ and Δs^+
- Three observables that contain these hPDFs in linearly independent combinations: g_1^p , g_1^n and $g_1^{\gamma Z}$.
- Only have data for g_1^p and g_1^n

$$g_1^p(x, Q^2) = \frac{1}{2} \sum_q Z_q^2 \Delta q^+(x, Q^2)$$

Observables predicted by our formalism: Double spin asymmetries

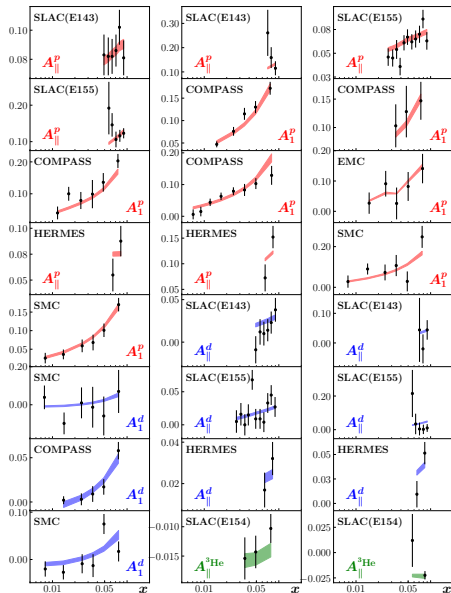
$$A_{||} = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} \propto A_1 \propto g_1$$

$\uparrow (\downarrow)$ is Positive (negative) helicity electron

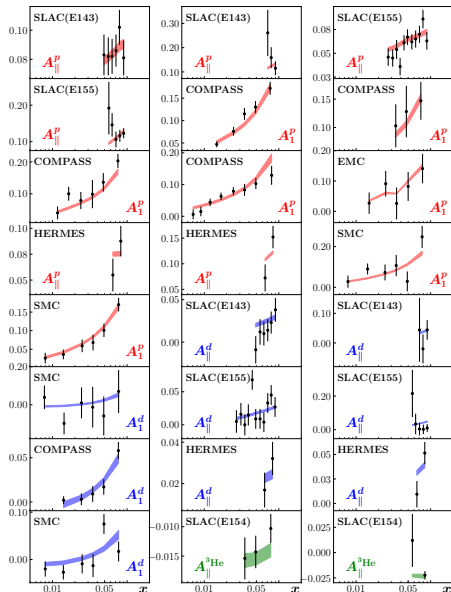
$\uparrow\uparrow (\downarrow\downarrow)$ is Positive (negative) helicity proton

A_1 is a virtual photoproduction asymmetry

Fitting to data

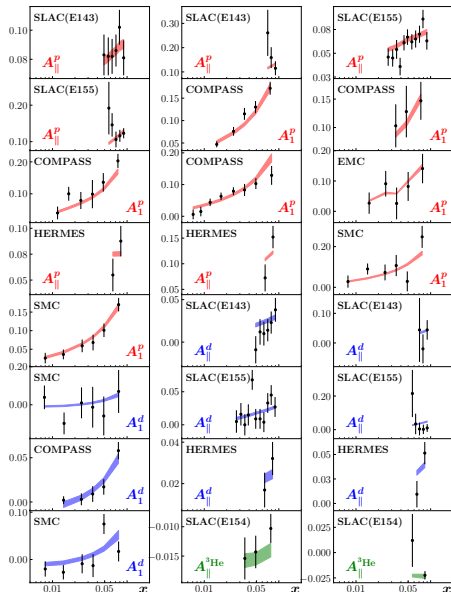


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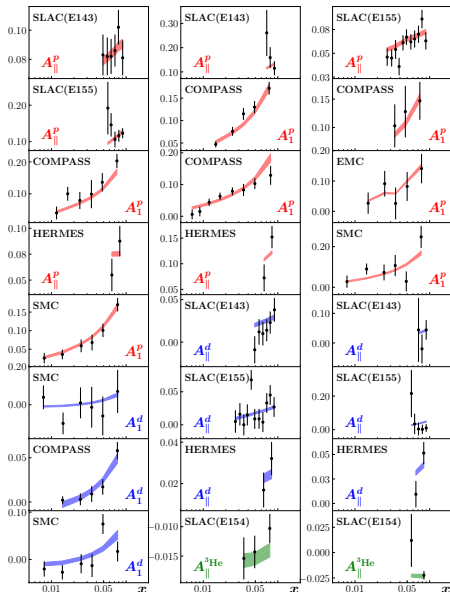
- First fit of small- x theory to polarized data
- With a cut of $x < 0.1$

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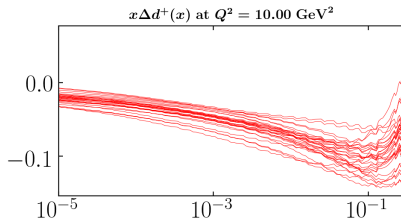
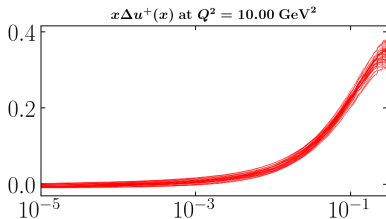
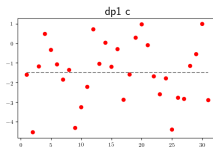
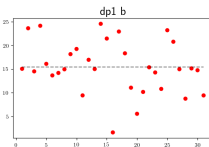
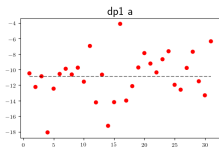
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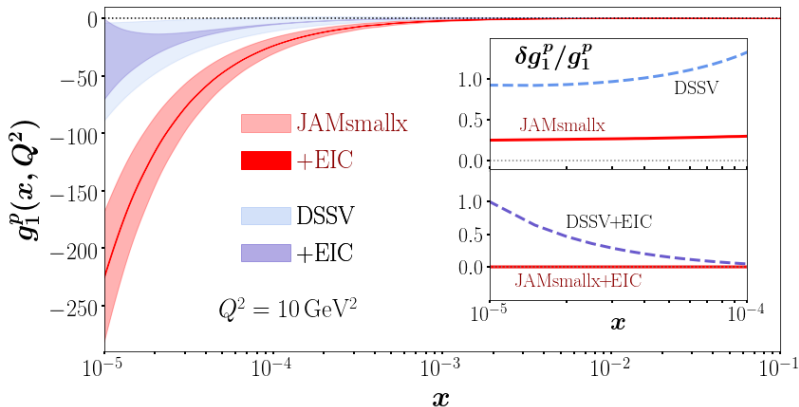


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- $\chi^2/npts = 1.01$

Monte-Carlo generation of parameters that tend towards minimum χ^2



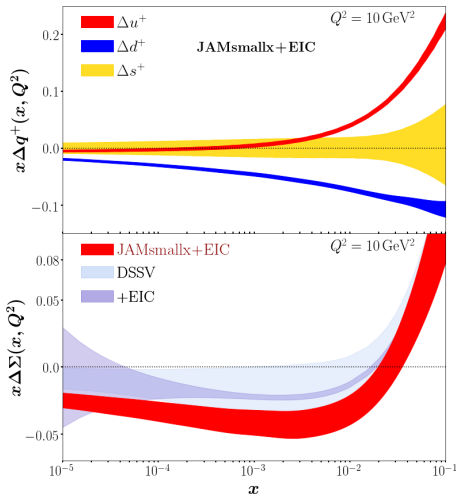
Predictions for Electron Ion Collider



- Predict large negative g_1
- Significant improvement in error from EIC

Helicity PDFs

Preliminary extraction of hPDFs and $\Delta\Sigma = \frac{1}{2} \sum_q \Delta q^+(x, Q^2)$
(assuming $\Delta s^+ = 0$)



- We have a theory that describes the hPDFs in terms of the polarized dipole amplitude
- Performed the first small- x fit to world polarized DIS data
- Predicted g_1 down to $x = 10^{-5}$
- While maintaining control over the uncertainty
- Preliminary extraction of the hPDFs and quark spin contribution

- Fit to other measurements (Semi-inclusive DIS) to further constrain the helicity PDFs
- Large N_c & N_f (include quarks into quark evolution)(Kovchegov, Tawabutr, JHEP 08 (2020))
- Include higher-order correction to evolution, such as the single log contribution and running coupling (See Josh's talk: Wednesday 13:45 in the spin session)