

Finite N_c Corrections in the NLO BK Equation

Lappi, Mäntysaari, A. R.
[Phys. Rev. D 102 074027] (2020)

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Poster session flash talk

Andrecia Ramnath

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University of Jyväskylä
(Māris Grunskis Photography)



Wilson Line Correlators

- Colour Glass Condensate effective field theory: small/moderate virtuality Q^2 , small x_{Bj}
- Wilson lines are basic building blocks

$$U_{\mathbf{x}}^\dagger := P \exp \left\{ ig \int_{x^+} \alpha_{\mathbf{x}}^a(x^+) t^a \right\} \sim \text{---} \left| \begin{array}{c} \color{blue}{\rule{0.5em}{0.5em}} \\ \color{green}{\rule{0.5em}{0.5em}} \end{array} \right. \text{---}$$

- Enter cross sections explicitly within correlators $\langle \dots \rangle$
- Evolution in rapidity of correlators governed by Balitsky Hierarchy \iff JIMWLK equation
- Infinite set of open equations – $\mathcal{O}(n)$ equation needs input from $\mathcal{O}(n+1)$
- First equation leads to BK equation for dipole

$$S_{\mathbf{x}, \mathbf{y}}^{(2)} := \text{tr} \left\{ U_{\mathbf{x}} U_{\mathbf{y}}^\dagger \right\} / N_c \sim \text{---} \left| \begin{array}{c} \color{blue}{\rule{0.5em}{0.5em}} \\ \color{green}{\rule{0.5em}{0.5em}} \end{array} \right. \text{---}$$

- Can use large- N_c limit where expectation values factorise $\langle \text{tr} \{ \} \text{tr} \{ \} \rangle \rightarrow \langle \text{tr} \{ \} \rangle \langle \text{tr} \{ \} \rangle$, but we go beyond this

Next-to-leading Order Balitsky–Kovchegov Equation

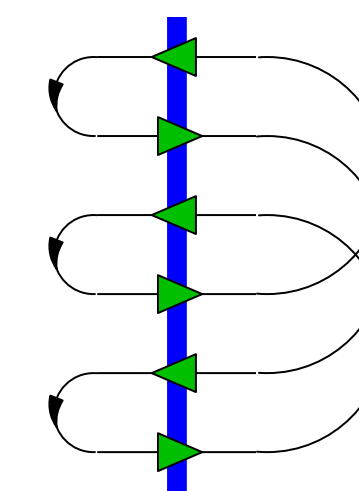
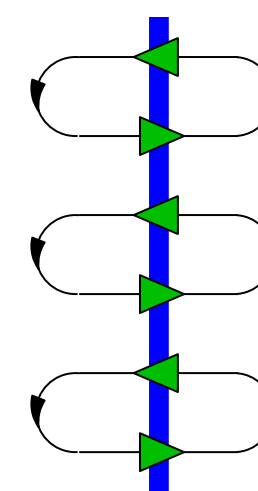
Balitsky, Chirilli [Nucl. Phys. B822:45-87 (2009)]

$$\partial_Y \langle S_{\mathbf{x}, \mathbf{y}}^{(2)} \rangle = \frac{\alpha_s N_c}{2\pi^2} \int_z K_1^{\text{BC}} \langle D_1 \rangle + \frac{\alpha_s^2 N_c^2}{16\pi^4} \int_{z, z'} \left(K_{2,1} \langle D_{2,1} \rangle + K_{2,2} \langle D_{2,2} \rangle \right) + \mathcal{O}(n_f)$$

$$\langle D_1 \rangle = \langle S_{\mathbf{x}, z}^{(2)} S_{z, \mathbf{y}}^{(2)} \rangle - \langle S_{\mathbf{x}, \mathbf{y}}^{(2)} \rangle$$

$$\langle D_{2,2} \rangle = \langle S_{\mathbf{x}, z}^{(2)} S_{z, z'}^{(2)} S_{z', \mathbf{y}}^{(2)} \rangle - (z' \rightarrow z)$$

$$\langle D_{2,1} \rangle = \langle S_{\mathbf{x}, z}^{(2)} S_{z, z'}^{(2)} S_{z', \mathbf{y}}^{(2)} \rangle - \frac{1}{N_c^2} \langle S_{\mathbf{x}, z, z', \mathbf{y}, z, z'}^{(6)} \rangle$$



Gaussian Approximation

- Go beyond **large- N_c** limit. Truncate infinite hierarchy of evolution equations
- Parametrise correlators according to

$$\partial_Y \langle \hat{\mathcal{O}} \rangle := -\frac{1}{2} \int_{uv} G_{uv}(Y) L_u^a L_v^a \hat{\mathcal{O}}$$

- Operate on \mathcal{O} with Lie derivatives $L_u^a L_v^a \sim$ add gluon emission/absorption vertices
- We have found a non-trivial basis such that **transition matrix** block diagonalises

$$\lim_{\substack{u \rightarrow z \\ v \rightarrow z'}} \mathcal{M}(Y) = \begin{pmatrix} \mathcal{M}_1^{(3 \times 3)}(Y) & 0 & 0 \\ 0 & \mathcal{M}_2^{(2 \times 2)}(Y) & 0 \\ 0 & 0 & \mathcal{M}_3^{(1 \times 1)}(Y) \end{pmatrix}$$

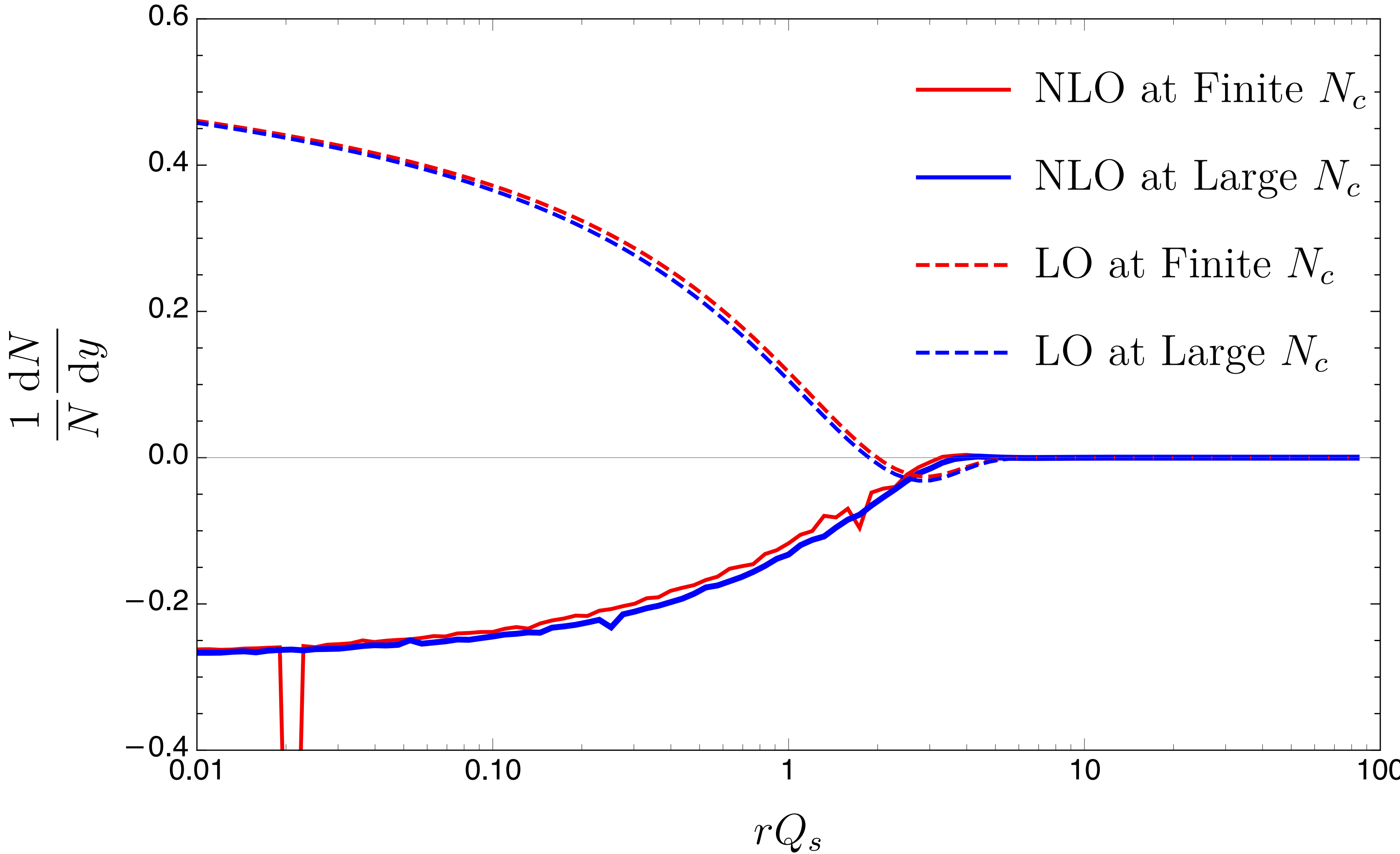
6-point correlators

4-point correlator

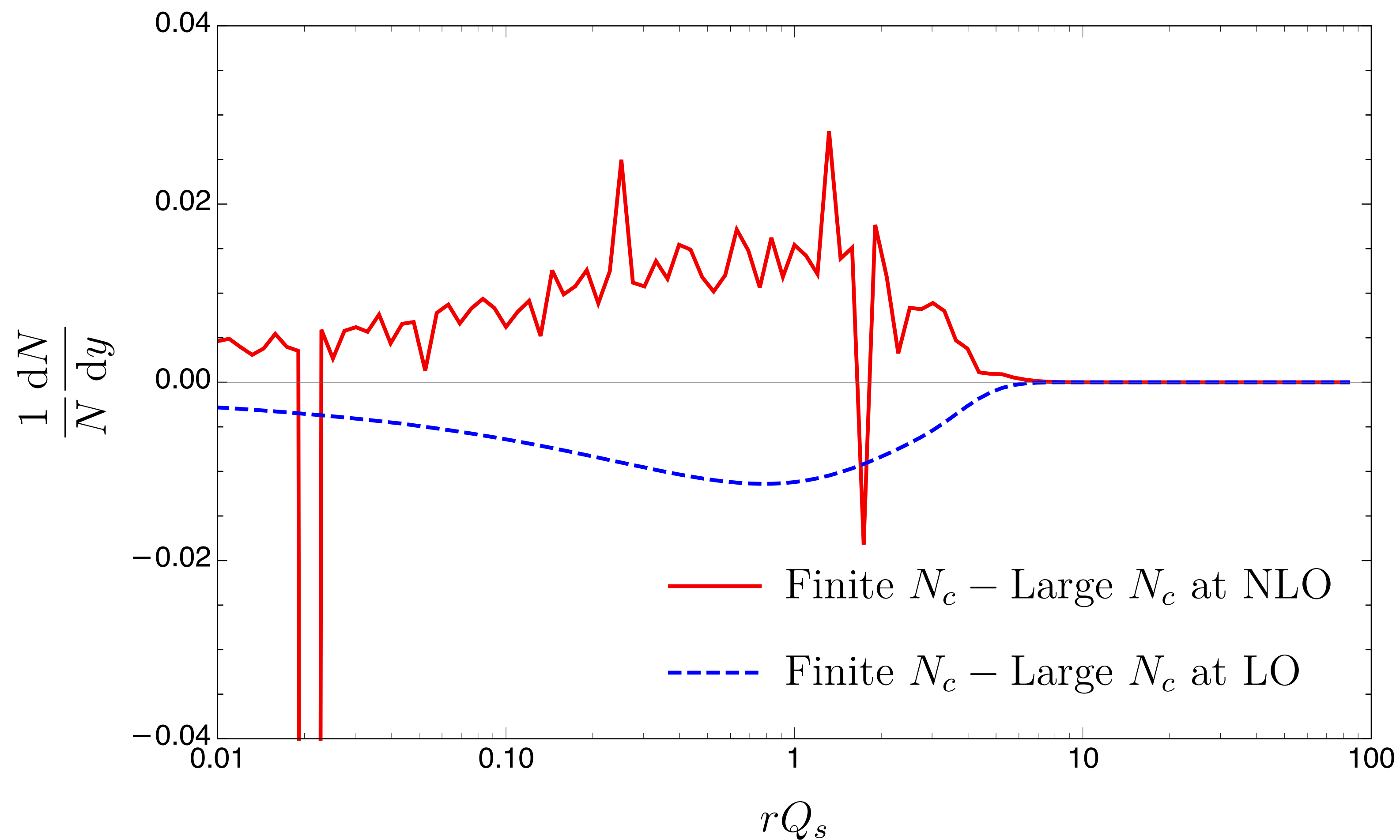
2-point correlator

Iancu, Leonidov, McLerran
 [Nucl.Phys. A692 (2001) 583-645]
 Fujii [Nucl.Phys. A709 (2002)
 236-250]
 Dumitru, Dusling, Gelis, Jalilian-
 Marian, Lappi, Venugopalan
 [Phys.Lett. B697 (2011) 21-25]
 Dusling, Mace, Venugopalan
 [Phys.Rev. D97 (2018) no.1, 016014]

Numerical Results 1/2



Numerical Results 2/2



Conclusion: Naive expectation a priori is finite- N_c corrections at NLO are $1/N_c^2 \sim \mathcal{O}(10\%)$.

Numerics show much smaller correction $\sim \mathcal{O}(1\%)$!

Thank you for watching!