NLO CORRECTIONS TO DI-HADRON PRODUCTION IN DIS USING THE COLOR GLASS CONDENSATE FORMALISM DIS2021

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Di-hadron angular correlations are a sensitive probe of small x saturation physics in the color glass condensate (CGC). The leading order di-hadron production cross section is well known, but future experiments will be sensitive to next-to-leading order (NLO) effects. Here we calculate the NLO corrections to the di-hadron production cross section in DIS.

## LEADING ORDER DI-HADRON PRODUCTION IN DIS

- At high energy, we use the Color Glass Condensate (CGC) effective theory of QCD. This allows us to treat the heavy nucleus as a classical background (color) field A<sup>μ</sup>.
- The leading order (LO) diagram has the photon split into a  $q\bar{q}$  pair which then interacts with the CGC.



• The LO result is well understood [Gelis and Jalilian-Marian, 2003]. Interaction with the background field is via **multiple scattering**.

## REAL CORRECTIONS

• There are four real diagrams to consider in the eikonal limit using the shockwave approximation. [Ayala et al., 2017]



• We need to integrate over the phase space of the outgoing gluon.

# REAL CORRECTIONS

• Results for real corrections using longitudinally polarized photons.

$$\begin{split} &\int_{k}\left\langle \mathcal{A}_{11}^{L}\right\rangle =\frac{32e^{2}g^{2}Q^{2}N_{c}^{2}z_{2}^{3}(1-z_{2})^{2}(z_{1}^{2}+(1-z_{2})^{2})}{(2\pi)^{2}z_{1}}\int\mathrm{d}^{8}x\left[S_{122'1'}-S_{12}-S_{1'2'}+1\right]e^{ip(x_{1}'-x_{1})}e^{iq(x_{2}'-x_{2})}\\ &\quad \mathcal{K}_{0}(|x_{12}|Q_{2})\mathcal{K}_{0}(|x_{1'2'}|Q_{2})\mathcal{G}(x_{1}'-x_{1}).\\ &\int_{k}\left\langle \mathcal{A}_{33}^{L}\right\rangle =\frac{32e^{2}g^{2}Q^{2}N_{c}^{2}z_{1}z_{3}^{2}(z_{1}^{2}+(1-z_{2})^{2})}{(2\pi)^{4}}\int\mathrm{d}^{10}x\left[S_{11'}S_{22'}-S_{13}S_{23}-S_{1'3}S_{2'3}+1\right]e^{ip(x_{1}'-x_{1})}e^{iq(x_{2}'-x_{2})}\\ &\quad \mathcal{K}_{0}(Qx)\mathcal{K}_{0}(Qx')\frac{(\mathbf{x}_{3}-\mathbf{x}_{1})\cdot(\mathbf{x}_{3}-\mathbf{x}_{1}')}{(x_{3}-x_{1})^{2}(\mathbf{x}_{3}-\mathbf{x}_{1}')^{2}}.\\ &\int_{k}\left\langle \mathcal{A}_{24}^{L}\right\rangle =\frac{32e^{2}g^{2}Q^{2}N_{c}^{2}z_{1}^{3}(1-z_{1})(z_{2}^{2}+(1-z_{1})^{2})}{(2\pi)^{4}}\int\mathrm{d}^{10}x\left[S_{211'3}S_{2'3}-S_{1'3}S_{2'3}-S_{12}+1\right]e^{ip(x_{1}'-x_{1})}e^{iq(x_{2}'-x_{2})}\\ &\quad \mathcal{K}_{0}(|x_{12}|Q_{1})\mathcal{K}_{0}(QX')\frac{(\mathbf{x}_{3}-\mathbf{x}_{2})\cdot(\mathbf{x}_{3}-\mathbf{x}_{2}')}{(\mathbf{x}_{3}-\mathbf{x}_{2})^{2}(\mathbf{x}_{3}-\mathbf{x}_{2}')^{2}}.\\ &\quad \mathcal{Q}_{i}=\sqrt{z_{i}(1-z_{i})}Q, \qquad X=\sqrt{z_{2}z_{1}x_{12}^{2}+z_{3}z_{1}x_{13}^{2}+z_{3}z_{2}x_{23}^{2}},\\ &\quad S_{ij}=\frac{1}{N_{c}}\operatorname{Tr}_{c}\left\langle V(x_{i})V^{\dagger}(x_{j})\right\rangle, \qquad S_{ijkl}=\frac{1}{N_{c}}\operatorname{Tr}_{c}\left\langle V(x_{i})V^{\dagger}(x_{j})V^{\dagger}(x_{l})\right\rangle,\\ &\quad G(x_{i}-x_{j})=\int\frac{\mathrm{d}^{2}\mathbf{k}}{(2\pi)^{2}}\frac{e^{i\mathbf{k}\cdot(\mathbf{x}_{1}-\mathbf{x}_{j})}}{\mathbf{k}^{2}}=\frac{1}{2\pi}\left(\frac{1}{\epsilon}+\gamma_{E}-\log\left(\pi\mu|x_{i}-x_{j}|\right)\right). \end{split}$$

• There are several virtual diagrams to consider in the eikonal limit using the shockwave approximation. (Here each vertical line indicates a separate diagram)



# VIRTUAL CORRECTIONS

• Some of these diagrams can be handled by inserting standard loop corrections to propagators and vertices. Others need to be worked out in full.



$$\int \frac{\mathrm{d}^{4}k_{1}}{(2\pi)^{4}} \frac{\mathrm{d}^{4}k_{2}}{(2\pi)^{2}} \frac{\mathrm{d}^{4}k_{3}}{(2\pi)^{4}} \bar{u}(p)(ig\gamma^{\mu}t^{a})S(k_{3},k_{2})(ig\gamma^{\nu}t^{b})S^{0}(k_{1})(ie\notin(l))S(k_{1}-l,-q)S^{0}(q)^{-1}v(q)$$

$$G^{ba}_{\nu\mu}(k_{2}-k_{1},k_{3}-p)$$

- Derive all NLO contributions to the di-hadron cross section.
- Establish factorization (or lack thereof) in NLO corrections to di-hadron production in DIS.

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### Ayala, A., Hentschinski, M., Jalilian-Marian, J., and Tejeda-Yeomans, M. E. (2017).

Spinor helicity methods in high-energy factorization: Efficient momentum-space calculations in the color glass condensate formalism.

Nuclear Physics B, 920:232–255.

Gelis, F. and Jalilian-Marian, J. (2003).

From deep inelastic scattering to proton-nucleus collisions in the color glass condensate model. *Physical Review D*, 67(7).