

# Central dilepton production in proton-proton collisions with rapidity gap and with forward protons

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# Contents

- ▶ Introduction
- ▶ Sketch of the formalism
- ▶ **Inclusive production**  
(integrated cross section, distributions, structure functions, .....
- ▶ **Cut on  $\xi$  variable(s)**  
(integrated cross section, distributions, structure functions, .....
- ▶ **Range of  $x_{Bj}$**  tested in the  $pp \rightarrow l^+l^-(p)$  processes
- ▶ **Jet and hard emissions**
- ▶ ***SUPERCHIC*** results  
(distributions, differential gap survival factor)
- ▶ Conclusions and outlook

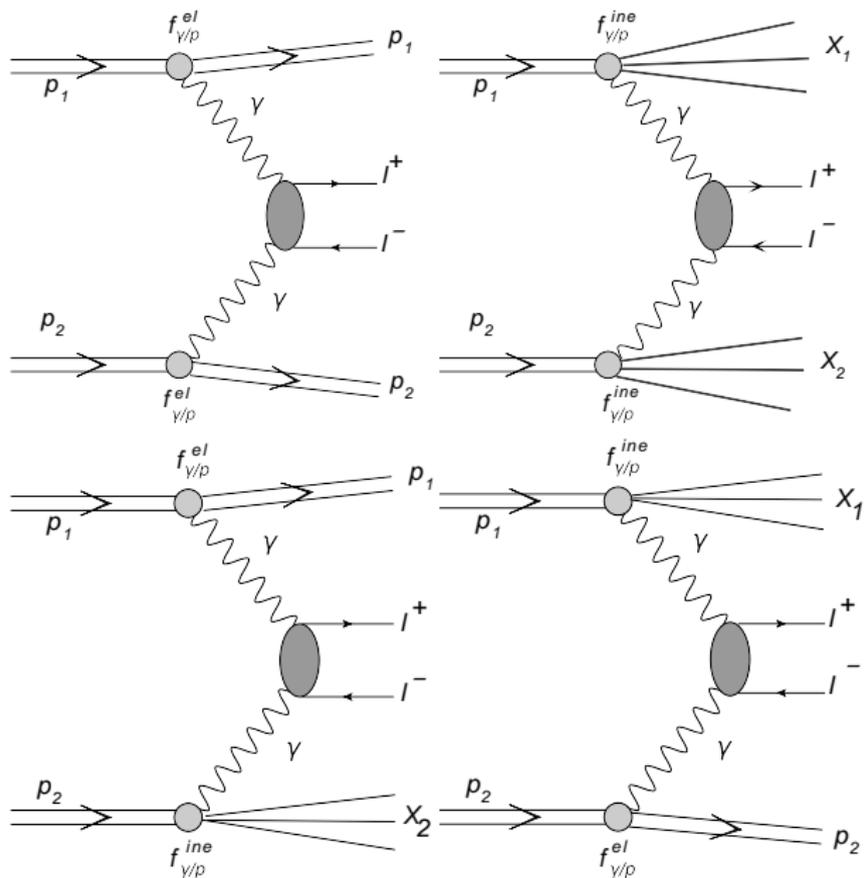
# Introduction

- ▶ We wish to discuss production of dilepton pairs in proton-proton collisions via photon-photon fusion **including photon transverse momenta**.
- ▶ Both ATLAS and CMS performed relevant measurements.
- ▶ Here we concentrate on the case with **one forward proton** (CMS (poor statistics), ATLAS (better statistics)).
- ▶ Our group was the first which proposed to use the formalism with photon transverse momenta.
- ▶ The same formalism can be also used for production of  $W^+W^-$  and  $t\bar{t}$  pairs.
- ▶ Here we wish to discuss consequences of **proton measurement** for the cross section, differential distributions, gap survival factor, etc.
- ▶ We will also use the popular **SUPERCHIC** generator where the same formalism was implemented. It also includes **soft gap survival factor** as developed by the Durham group

# Our previous papers on the subject

- ▶ G.G. da Silveira, L. Forthomme, K. Piotrkowski, W. Schäfer and A. Szczurek, “Central  $\mu^+\mu^-$  production via photon-photon fusion in proton-proton collisions with proton dissociation”, JHEP **02** (2015) 159.
- ▶ M. Luszczak, W. Schäfer and A. Szczurek, “Two-photon dilepton production in proton-proton collisions: Two alternative approaches”, Phys. Rev. **D93** (2016) 074018.
- ▶ M. Luszczak, W. Schäfer and A. Szczurek, “Production of  $W^+W^-$  pairs via  $\gamma^*\gamma^* \rightarrow W^+W^-$  subprocess with photon transverse momenta”, JHEP**05** (2018) 064.
- ▶ P. Lebedowicz and A. Szczurek, “Exclusive and semiexclusive production of  $\mu^+\mu^-$  pairs with Delta isobars and other resonances in the final state and the size of absorption effects”, Phys. Rev. **D98** (2018) 053007.
- ▶ L. Forthomme, M. Luszczak, W. Schäfer and A. Szczurek, “Rapidity gap survival factors caused by remnant fragmentation for  $W^+W^-$  pair production via  $\gamma^*\gamma^* \rightarrow W^+W^-$  subprocess with photon transverse momenta”, Phys. Lett. **B789** (2019) 300.
- ▶ M. Luszczak, L. Forthomme, W. Schäfer and A. Szczurek, “Production of  $t\bar{t}$  pairs via  $\gamma\gamma$  fusion with photon transverse momenta and proton dissociation”, JHEP **02** (2019) 100.

# The mechanisms considered



# Sketch of the formalism

In the  $k_T$ -factorization approach, the cross section for  $l^+l^-$  production can be written in the form

$$\frac{d\sigma^{(i,j)}}{dy_1 dy_2 d^2\mathbf{p}_1 d^2\mathbf{p}_2} = \int \frac{d^2\mathbf{q}_1}{\pi\mathbf{q}_1^2} \frac{d^2\mathbf{q}_2}{\pi\mathbf{q}_2^2} \mathcal{F}_{\gamma^*/A}^{(i)}(x_1, \mathbf{q}_1) \mathcal{F}_{\gamma^*/B}^{(j)}(x_2, \mathbf{q}_2) \frac{d\sigma^*(p_1, p_2; \mathbf{q}_1, \mathbf{q}_2)}{dy_1 dy_2 d^2\mathbf{p}_1 d^2\mathbf{p}_2}, \quad (1)$$

where the indices  $i, j \in \{\text{el}, \text{in}\}$  denote elastic or inelastic final states.

Here the photon flux for inelastic case is integrated over the mass of the remnant.

## Sketch of the formalism

The longitudinal momentum fractions of photons are obtained from the rapidities and transverse momenta of final state  $l^+l^-$  as:

$$\begin{aligned}x_1 &= \sqrt{\frac{\mathbf{p}_1^2 + m_l^2}{s}} e^{+y_1} + \sqrt{\frac{\mathbf{p}_2^2 + m_l^2}{s}} e^{+y_2}, \\x_2 &= \sqrt{\frac{\mathbf{p}_1^2 + m_l^2}{s}} e^{-y_1} + \sqrt{\frac{\mathbf{p}_2^2 + m_l^2}{s}} e^{-y_2}.\end{aligned}\quad (2)$$

Four-momenta of intermediate photons:

$$\begin{aligned}q_1 &\approx \left( x_1 \frac{\sqrt{s}}{2}, \vec{q}_{1t}, x_1 \frac{\sqrt{s}}{2} \right), \\q_2 &\approx \left( x_2 \frac{\sqrt{s}}{2}, \vec{q}_{2t}, -x_2 \frac{\sqrt{s}}{2} \right).\end{aligned}\quad (3)$$

# Photon fluxes

The integrated fluxes for elastic and inelastic processes can be found in our published papers (see also [Budneev](#), [Ginzburg](#), [Serbo et al.](#))

- ▶ The **elastic flux** is expressed via proton **electromagnetic form factors**.
- ▶ The **inelastic flux** is expressed via proton **structure function** ( $F_2$  and  $F_L$ ).

If one is interested in modeling what happens with the **proton remnant** than the formalism must be extended. Then the unintegrated inelastic photon distribution (flux) can be written as:

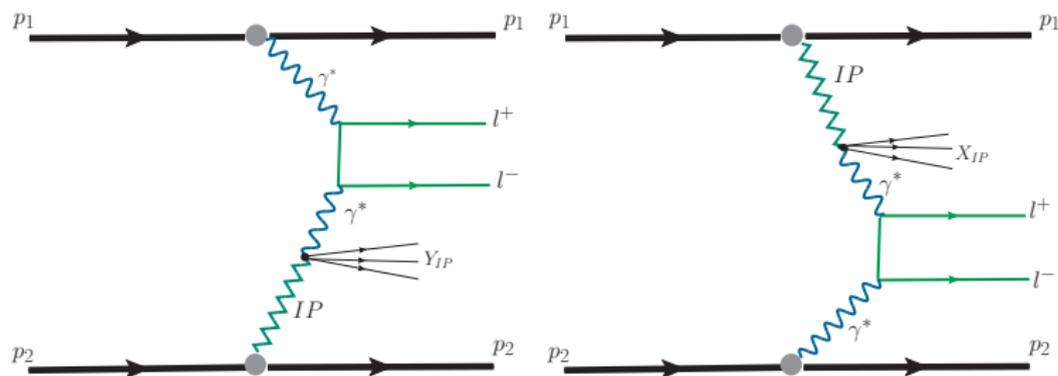
$$\mathcal{F}_{ine}(x, q_t^2) = \int dM^2 \frac{d\mathcal{F}_{ine}}{dM^2}(x, q_t^2, M^2), \quad (4)$$

where  $\frac{d\mathcal{F}_{ine}}{dM^2}(x, q_t^2, M^2)$  is a more differential photon distribution in the proton. We shall call it **doubly-unintegrated** photon distribution (flux).

The latter distribution was used to calculate differential distributions for production of  $W^+W^-$  ([FLSS2019](#)) or  $t\bar{t}$  ([LFSS2019](#)) pairs with rapidity gap at midrapidities.

# Proton from remnants

In principle, proton can be emitted also from the the remnant system. This requires modelling of remnant fragmentation which is not fully under control. Such protons carry typically much reduced longitudinal momentum fraction  $x_{p,i}$  such that  $\xi_i = 1 - x_{p,i} > 0.1$ , i.e. cannot be measured in the Roman pots of the ATLAS or CMS experiments.



**Rysunek:** Diffractive mechanisms of dilepton production in proton-proton collisions.

## Diffractive processes

Only the diffractive mechanism shown in the previous slide could lead to  $\xi_i < 0.1$ . However, the diffractive mechanism happens only in about 10 % of all cases as was measured at HERA. In addition the **pomeron remnant** would destroy the rapidity gap. Such a process was not discussed in the context of  $I^+I^-$  production in p p collisions with rapidity gap requirement. Also the diffractive photon distribution in pomeron was not discussed. One may expect:

$$\frac{d\mathcal{F}_{diff}}{dM^2}(x, q_t^2, M^2) \ll \frac{d\mathcal{F}_{ine}}{dM^2}(x, q_t^2, M^2). \quad (5)$$

In addition, the **pomeron remnant** would destroy the rapidity gap and the **rapidity gap veto** would **almost totally eliminate** contribution of such processes in the context of forward proton measurement discussed in the present paper.

# Arguments of structure functions

Calculated from photon transverse momentum and mass of the remnant.

Bjorken-x:

$$x_{Bj1} = \frac{q_{1t}^2}{q_{1t}^2 + M_X^2 - m_p^2},$$

$$x_{Bj2} = \frac{q_{2t}^2}{q_{2t}^2 + M_Y^2 - m_p^2}.$$

Photon virtuality:

$$Q_1^2 \approx q_{1t}^2,$$

$$Q_2^2 \approx q_{2t}^2.$$

## Forward proton

The ATLAS collaboration analysis impose the consistency requirements:

$$\xi_1 = \xi_{ll}^+ , \quad \xi_2 = \xi_{ll}^- . \quad (6)$$

The longitudinal momentum fractions of the photons were calculated in the ATLAS analysis as:

$$\begin{aligned} \xi_{ll}^+ &= \left( M_{ll} / \sqrt{s} \right) \exp(+Y_{ll}) , \\ \xi_{ll}^- &= \left( M_{ll} / \sqrt{s} \right) \exp(-Y_{ll}) . \end{aligned} \quad (7)$$

Only lepton variables enter the formula. We will use the same formula in our analysis.

# Integration parameters

Multiple integration (**Vegas method**):

$q_{1t}, q_{2t}, \phi_1, \phi_2, y_1, y_2, p_{t,diff}, \phi_{p_{t,diff}}$  and  $M_X$  or  $M_Y$ .

**9 or 10 integration variables.**

Careful adjustment of ranges of some integration parameters is required.

$q_{1t}, q_{2t} < 100 - 500 \text{ GeV}, M_X, M_Y < 500 - 1000 \text{ GeV}.$

# Results

In the calculations described below we shall take typical cuts on dileptons:

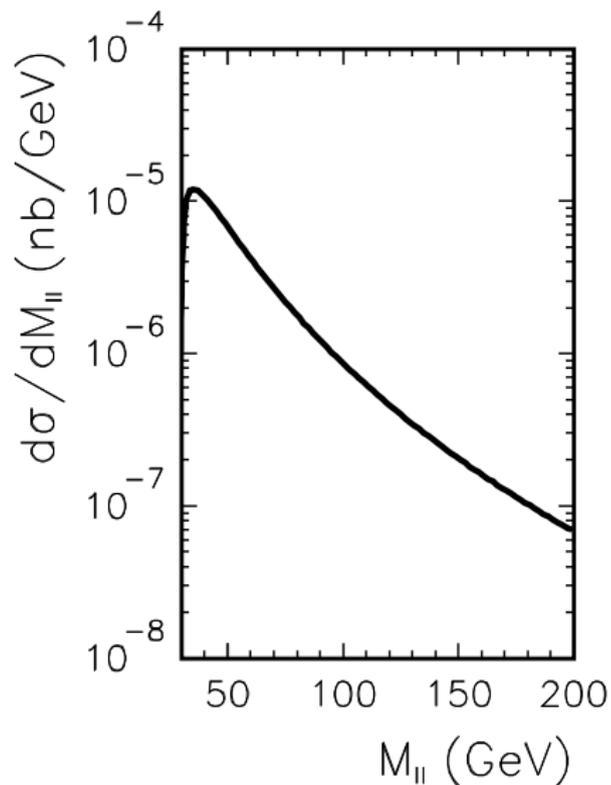
- ▶  $-2.5 < y_1, y_2 < 2.5$
- ▶  $p_{1t}, p_{2t} > 15 \text{ GeV}$

We shall show also results with **extra cuts on  $\xi_{ll}^+$  or  $\xi_{ll}^-$** .

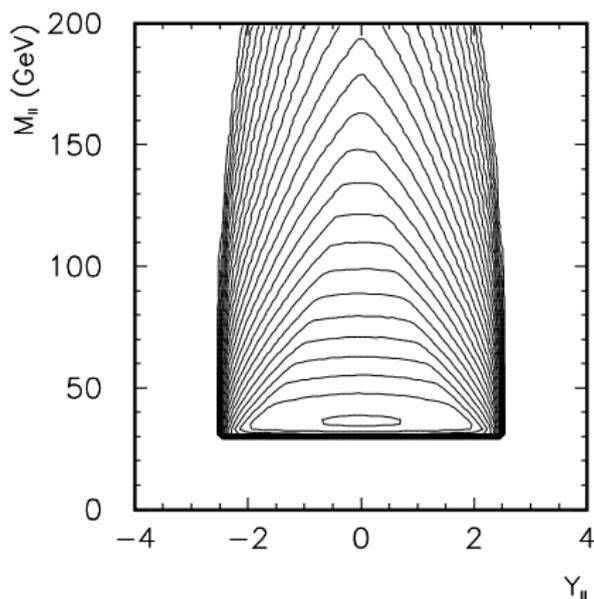
In the following we do not exclude:

- ▶ **mass window around  $Z$ -boson mass  $m_Z$** , as was done in (ATLAS).
- ▶ **cut on lepton acoplanarity**

## Double-elastic contribution

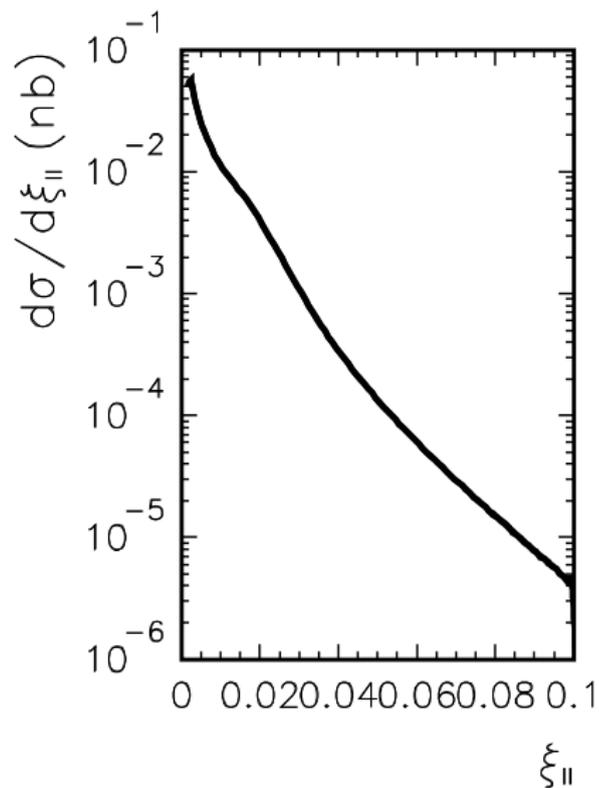


# Double-elastic contribution

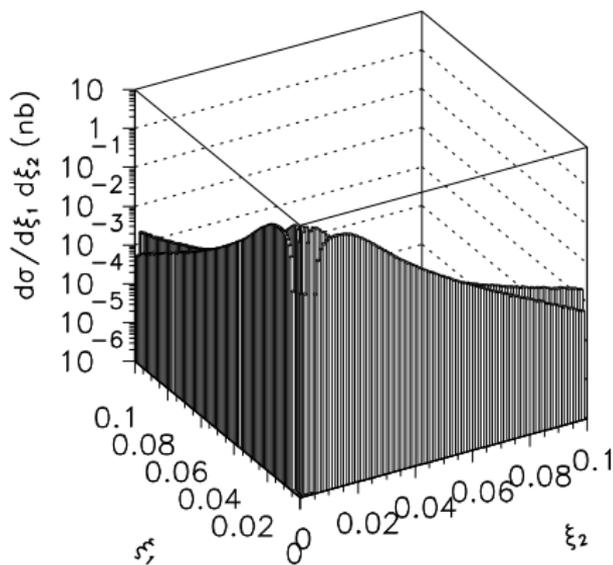


Rysunek: Two-dimension distribution in  $(M_{II}, Y_{II})$ . for double-elastic contribution. Here no cuts on neither  $\xi_1$  nor  $\xi_2$  were imposed.

## Double-elastic contribution

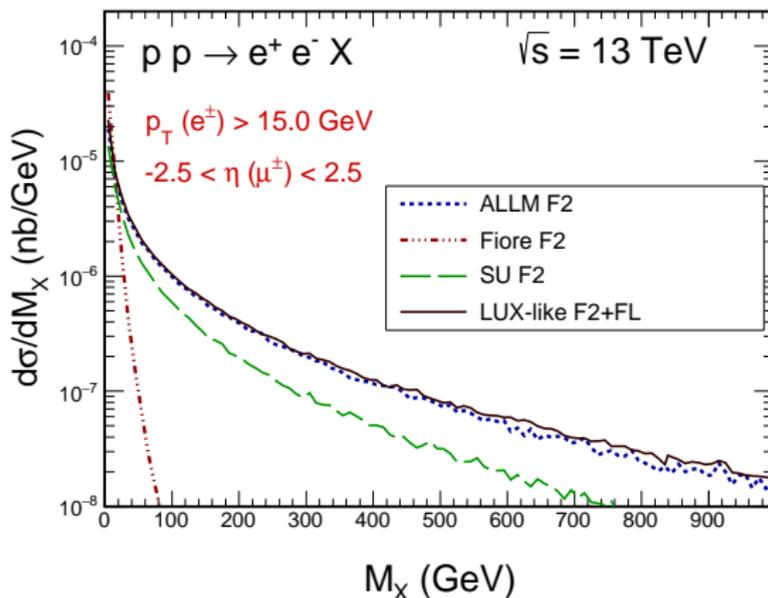


# Double-elastic contribution



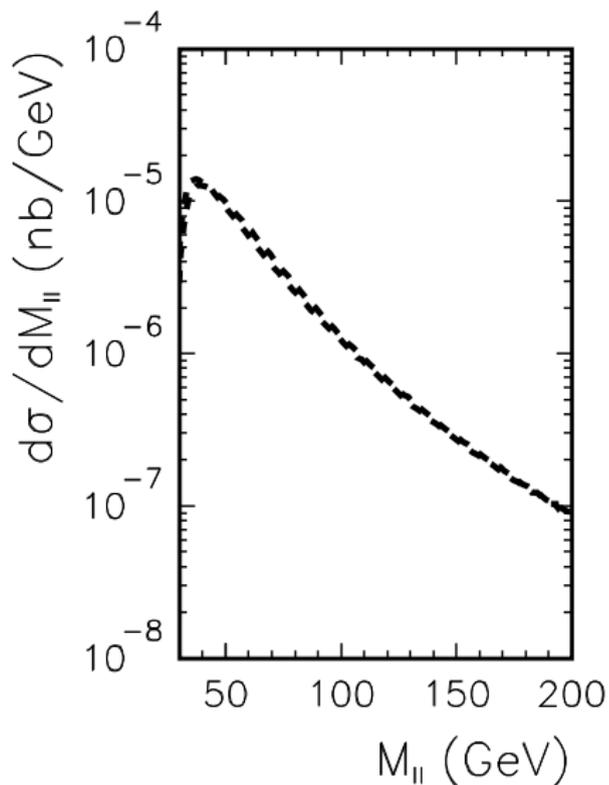
**Rysunek:** Two-dimensional distribution in  $(\xi_{||}^+, \xi_{||}^-)$  for the double-elastic mechanism.

# Single-dissociative contribution

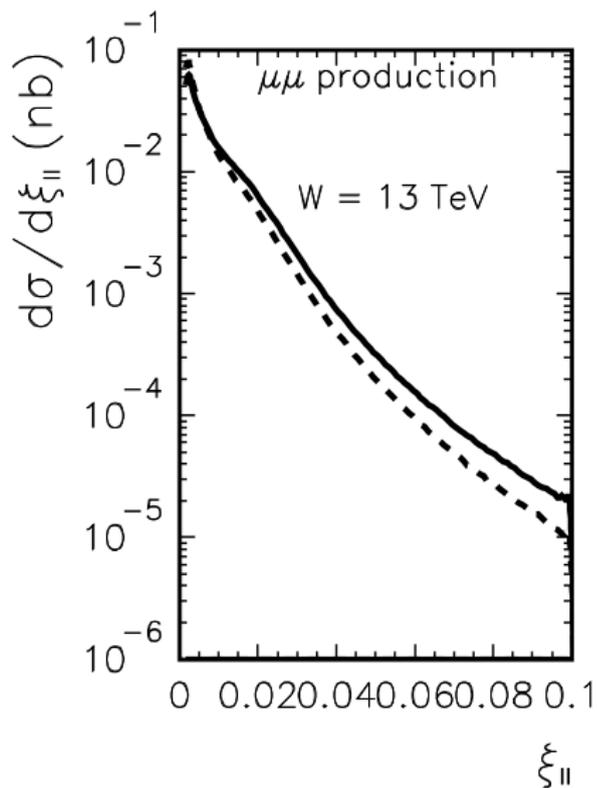


**Rysunek:** Distribution in the mass of the baryonic remnant system ( $M_X$  or  $M_Y$ ) for different structure functions from the literature. In the case of SU parametrization only partonic contribution is included.

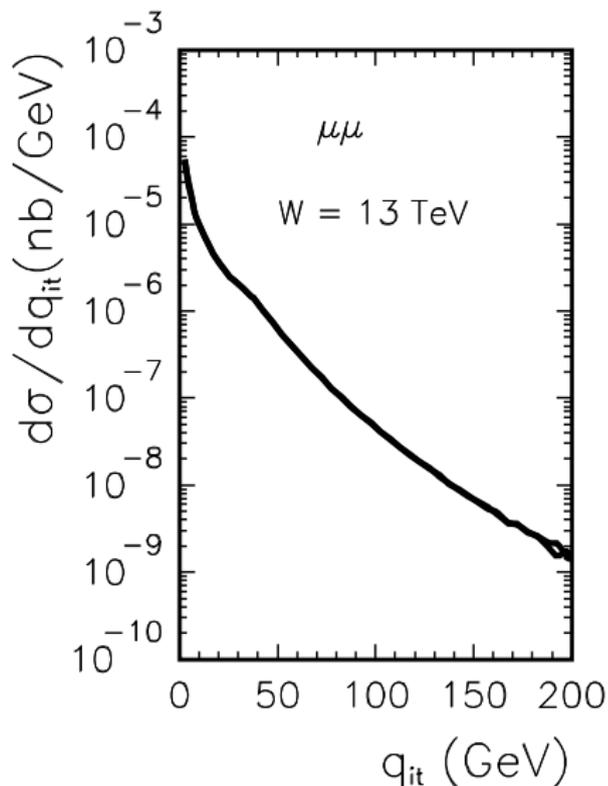
# Single-dissociative contribution



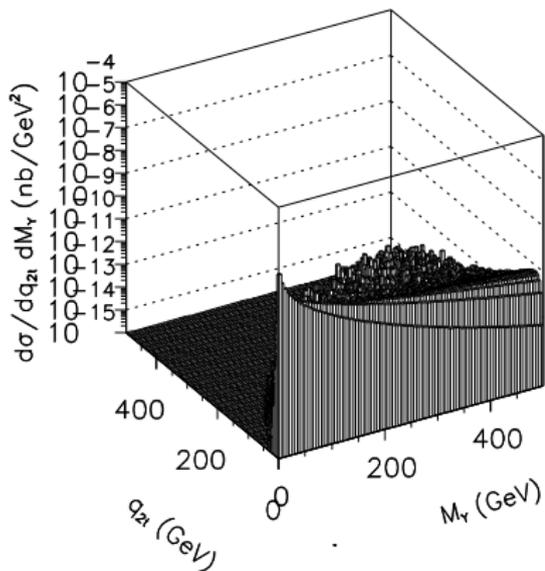
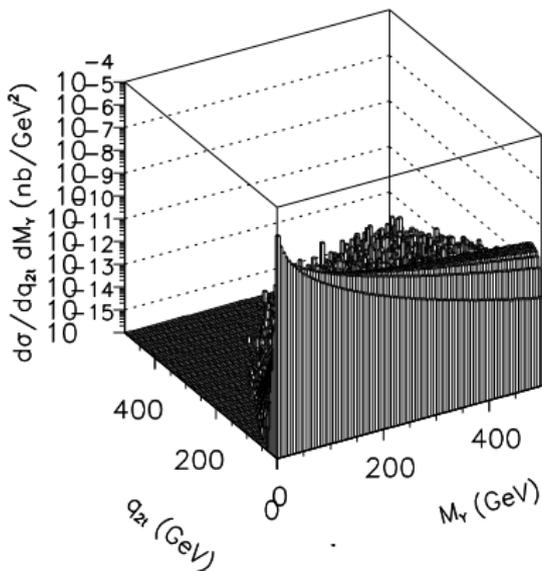
# Single-dissociative contribution



# Single-dissociative contribution

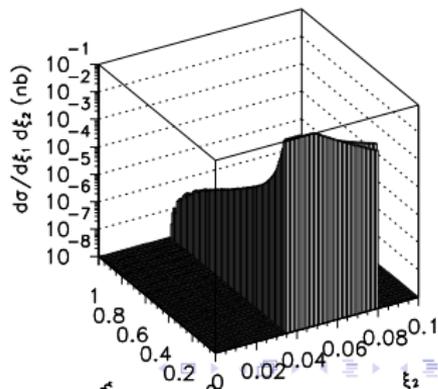
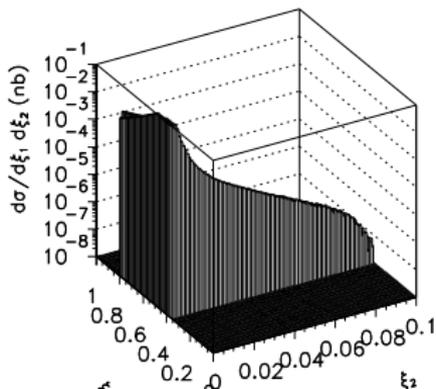
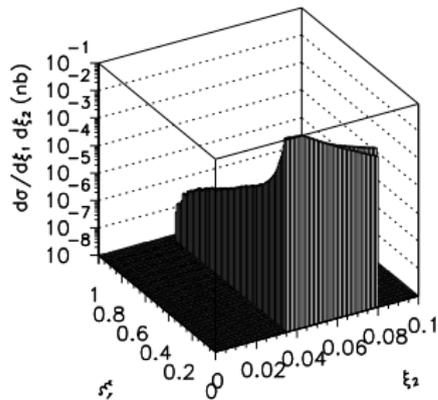
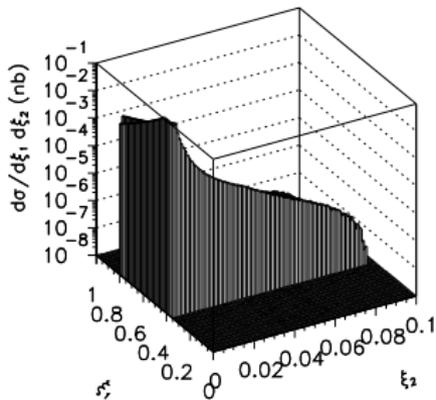


# Single-dissociative contribution



**Rysunek:** Two-dimensional distribution in  $(q_{2t}, M_Y)$  for elastic-inelastic contribution. We show results **without**  $\xi$  cut (left panel) and **with**  $\xi$  cut (right panel).

# $\xi_{||}^+$ or $\xi_{||}^-$ cuts

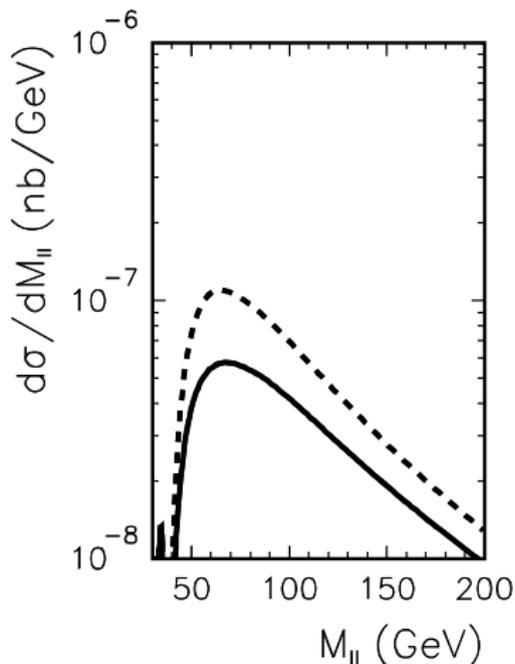


# $\xi_{||}^+$ or $\xi_{||}^-$ cuts

Tablica: Integrated cross section for  $\mu^+\mu^-$  with one p in  $0.035 < \xi_{||}^\pm < 0.08$ . Here  $p_{1t}, p_{2t} > 15$  GeV and  $-2.5 < y_1, y_2 < 2.5$ . In the paranthesis result with  $p_{t,sum} < 5$  GeV. 2UN – doubly unintegrated photon distribution and GEN – generator version.

contribution	c.s. in fb without $\xi$ -cuts	c.s. in fb with $\xi$ -cuts
elastic-elastic, cut on proton 1	358.68	5.4591
elastic-elastic, cut on proton 2	.....	5.4592
elastic-inelastic, cut on proton 1, SU, 0-100 GeV	427.8949	10.0190 (3.3492)
inelastic-elastic, cut on proton 2 SU, 0-100 GeV	427.0130	10.0186 (3.3491)
elastic-inelastic, VDM (no $\Omega$ ), 0-100 GeV	98.0215 (2UN)	
inelastic-elastic, VDM (no $\Omega$ ), 0-100 GeV	98.0297 (2UN)	
elastic-inelastic SU partonic	449.1076 (2UN)	
inelastic-elastic SU partonic	449.0985 (2UN)	
elastic-inelastic, cut on proton 1, ALLM	468.6102 (2UN)	11.8292
inelastic-elastic, cut on proton 2, ALLM	468.6102 (2UN)	11.8294
elastic-inelastic, new Szczurek	461.5330 (2UN)	12.6046 [14.1823] (5.9311)
inelastic-elastic, new Szczurek	461.5750 (2UN)	12.6032 [14.1806] (5.9309)
elastic-inelastic, ALLM	571.871 (GEN)	9.711
inelastic-elastic, ALLM	571.562 (GEN)	9.621
elastic-inelastic, LUX-like, $F_2 + F_L$	635.215 (GEN)	19.894
inelastic-elastic, LUX-like, $F_2 + F_L$	635.102 (GEN)	19.831
elastic-inelastic, LUX-like, $F_2$ only	..... (GEN)	.....
inelastic-elastic, LUX-like, $F_2$ only	656.702 (GEN)	.....
elastic-inelastic, cut on proton 1, resonances	38.6709 (2UN)	0.57872
inelastic-elastic, cut on proton 2 resonances	38.6639 (2UN)	0.57872
elastic-inelastic, cut on proton 1, $\Delta^+$	28.5844 (2UN)	0.42755
inelastic-elastic, cut on proton 2 $\Delta^+$	28.5814 (2UN)	0.42763

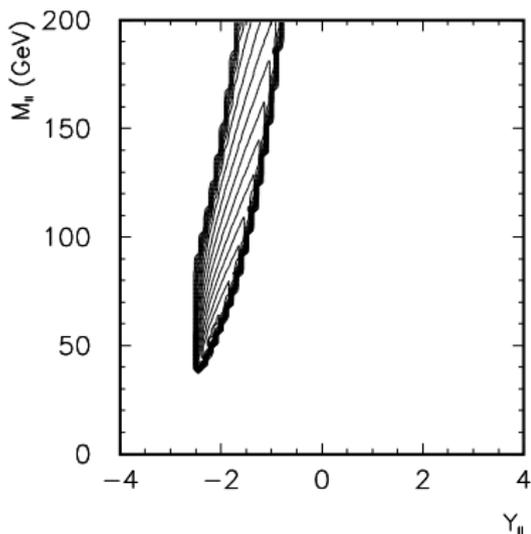
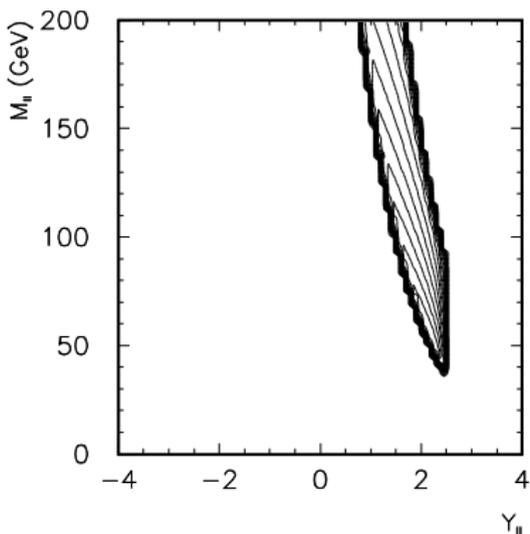
$\xi_{ll}^+$  or  $\xi_{ll}^-$  cuts



**Rysunek:** Distribution in dilepton invariant mass for four different contributions considered.

Here the cuts on  $\xi_{ll}^+$  or  $\xi_{ll}^-$  are imposed. The solid line is for double elastic contribution and the dashed line is for single dissociation.

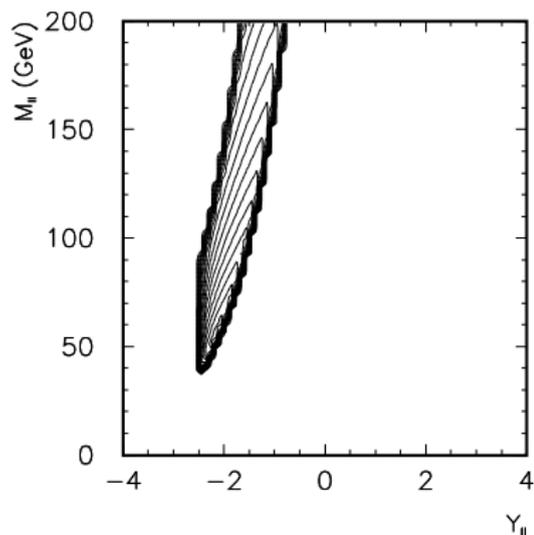
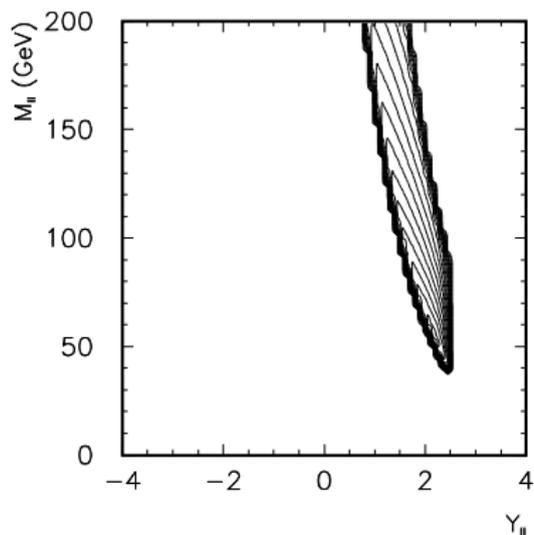
## $\xi$ -cut, double-elastic contribution



**Rysunek:** Two-dimension distribution in  $(M_{II}, Y_{II})$ . for double-elastic contribution. Here we have imposed **experimental condition** for  $\xi_1$  (left panel) or  $\xi_2$  (right panel).

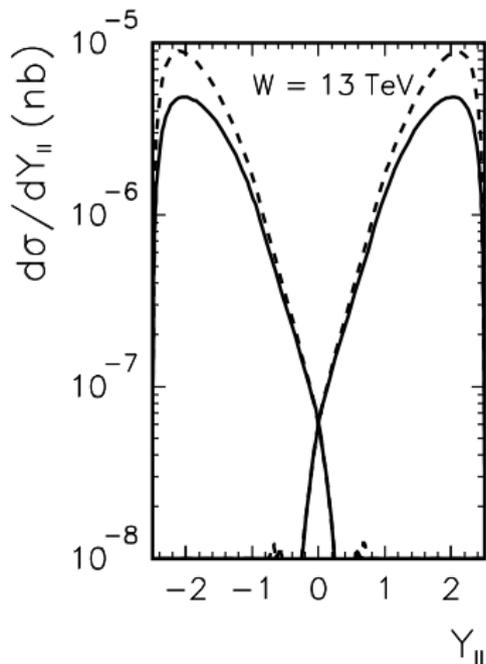
The  $p_{t, II} > 15$  GeV condition was imposed in addition.

## $\xi$ -cut, single-dissociative contribution



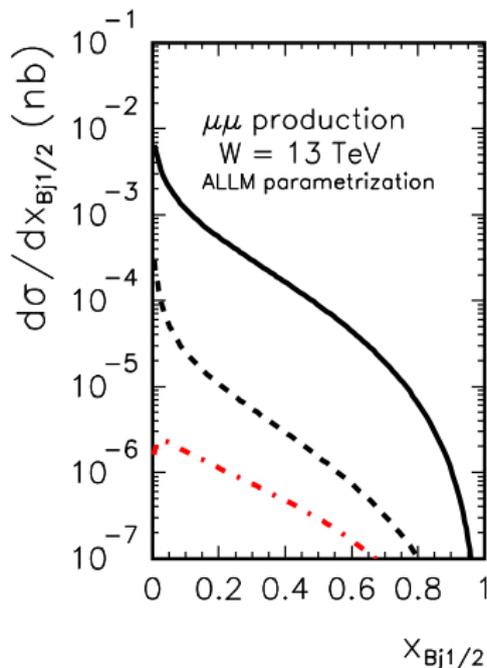
**Rysunek:** Two-dimensional distribution in  $(M_{II}, Y_{II})$  for elastic-inelastic (left panel) and inelastic-elastic (right panel) contributions. Here we have imposed **experimental condition** on  $\xi_1$

$\xi_{||}^+$  or  $\xi_{||}^-$  cuts



**Rysunek:** Distribution in dilepton rapidity for four different contributions considered. Here the cuts on  $\xi_{||}^+$  or  $\xi_{||}^-$  are imposed. The solid line is for double elastic contribution and the dashed line is for single dissociation contribution

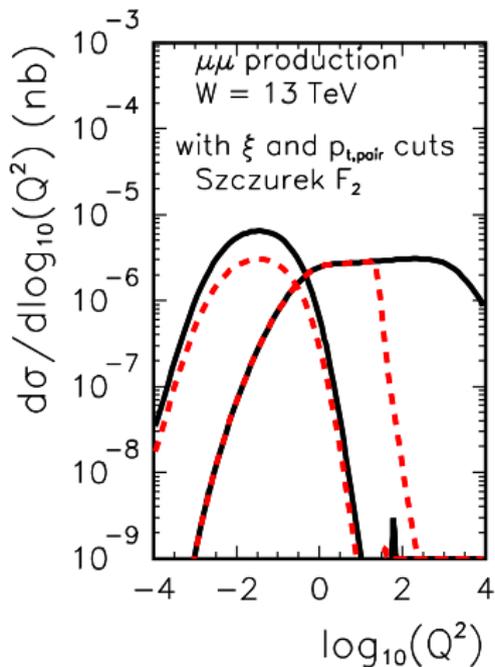
$\xi_{||}^+$  or  $\xi_{||}^-$  cuts



**Rysunek:** Distribution in  $x_{Bj}$  for single dissociative process. Shown are results **without** (solid line) and **with** (dashed line) cuts on longitudinal momentum fraction  $\xi$ .

In this calculation the ALLM parametrization of  $F_2$  structure

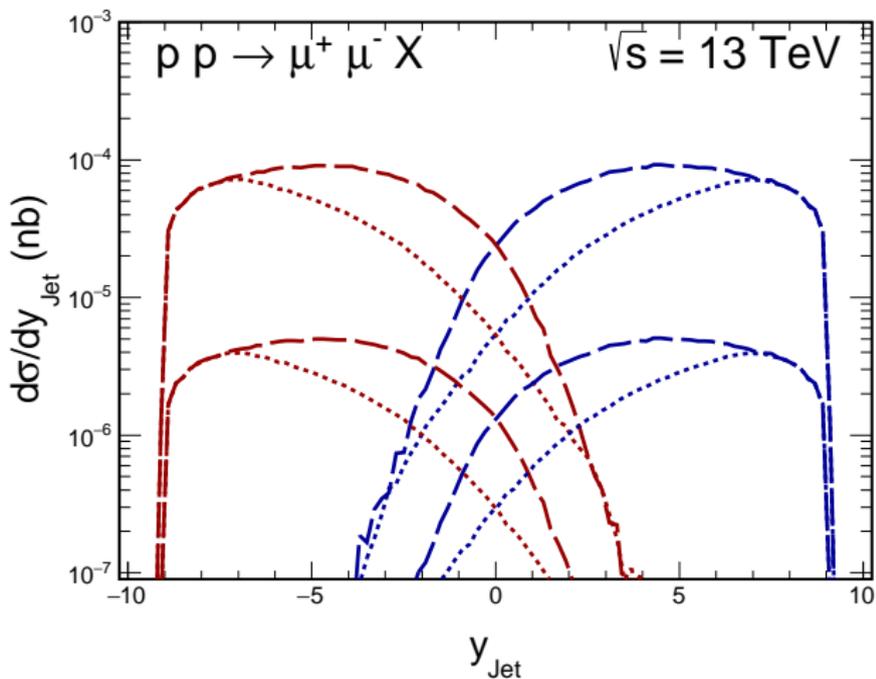
$\xi_{||}^+$  or  $\xi_{||}^-$  cuts



**Rysunek:** Distribution in  $\log_{10}(Q_i^2)$  for single dissociative process with cut on  $\xi$  and  $p_{t, \text{pair}}$  (red dashed line). We show distributions for elastic (left) and inelastic (right) vertex.

In this calculation a **new Szczurek parametrization** of  $F_2$  was used.

# $\xi_{||}^+$ or $\xi_{||}^-$ cuts, minijets



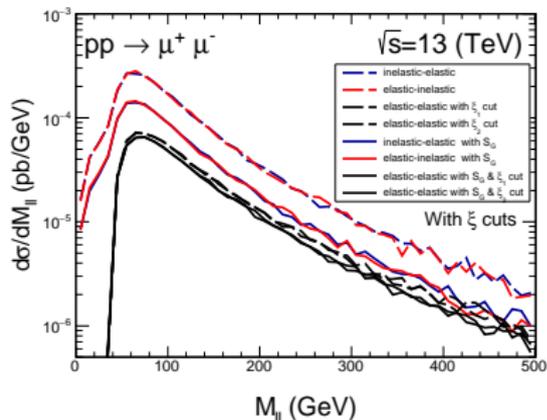
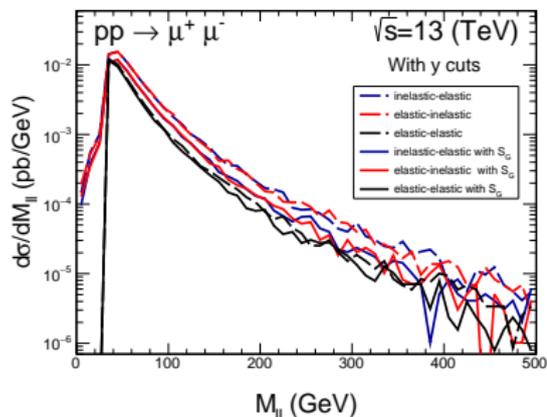
Rysunek: Distribution in rapidity of (mini)jets for inclusive case (upper curves) and for the case with cut on  $\xi_{1/2}$  and  $p_{t,pair} < 5$

# SUPERCHIC analysis

**Tablica:** Integrated cross section for  $\mu^+\mu^-$  production in pb for  $\sqrt{s} = 13$  TeV using SUPERCHIC program.  $0.035 < \xi_{\parallel}^{\pm} < 0.08$ . To calculate absorption effects we used model no 4 as implemented in the SUPERCHIC generator.

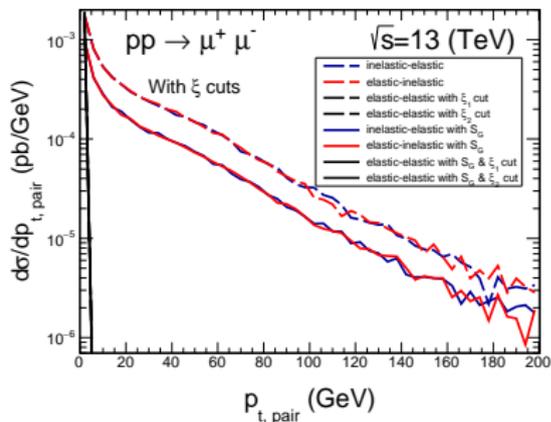
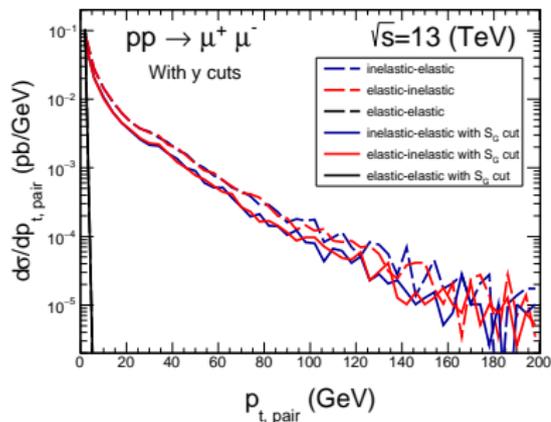
reaction	no soft $S_G$	with soft $S_G$	$\langle S_G \rangle$
-2.5 < $Y_{\parallel}$ < 2.5			
elastic-elastic	0.54438	0.50402	0.926
inelastic-elastic	0.89595	0.64283	0.717
elastic-inelastic	0.89587	0.64254	0.717
inelastic-inelastic	1.62859	0.24172	0.15
-2.5 < $y_1, y_2$ < 2.5 in addition			
elastic-elastic	0.42268	0.39355	0.931
inelastic-elastic	0.69241	0.51092	0.738
elastic-inelastic	0.69246	0.51087	0.738
$\xi$ cut in addition			
elastic-elastic, cut on $\xi_1$	0.00762	0.00675	0.886
elastic-elastic, cut on $\xi_2$	0.00762	0.00675	0.886
inelastic-elastic, cut on $\xi_2$	0.02718	0.01416	0.521
elastic-inelastic, cut on $\xi_1$	0.02717	0.01416	0.521
$p_{t,pair} < 5$ GeV in addition			
elastic-elastic	.....	.....	.....
inelastic-elastic, cut on $\xi_2$	0.008035 (2000)	0.00435	0.541
elastic-inelastic, cut on $\xi_1$	0.008056 (2000)	0.00436	0.541

# SUPERCHIC analysis



**Rysunek:** Distribution in dimuon invariant mass for the different contributions considered. We consider the case **without**  $\xi$  cuts (left panel) and **with**  $\xi$  cuts (right panel).

# SUPERCHIC analysis



**Rysunek:** Distribution in dimuon transverse momentum for the different contributions considered. We consider the case **without**  $\xi$  cuts (left panel) and **with**  $\xi$  cuts (right panel).

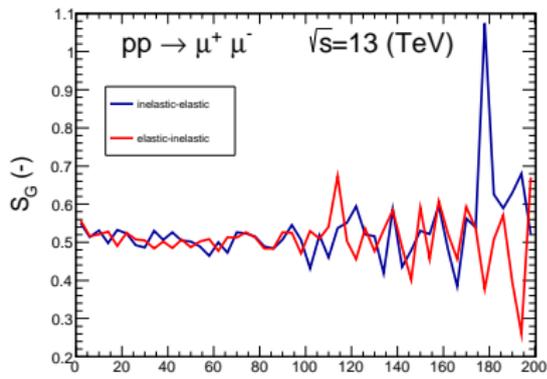
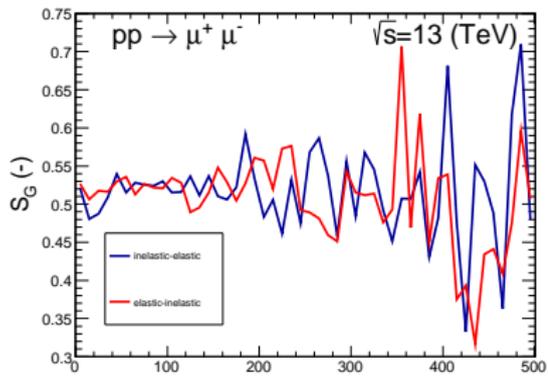
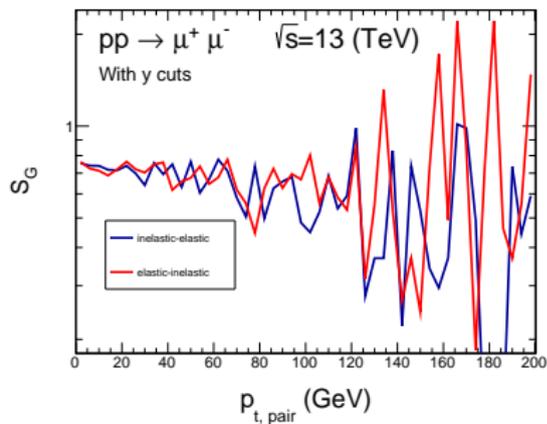
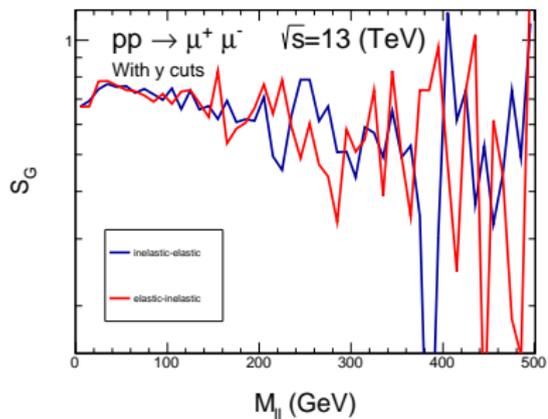
# SUPERCHIC analysis, gap survival function

We shall show corresponding gap survival factor calculated as:

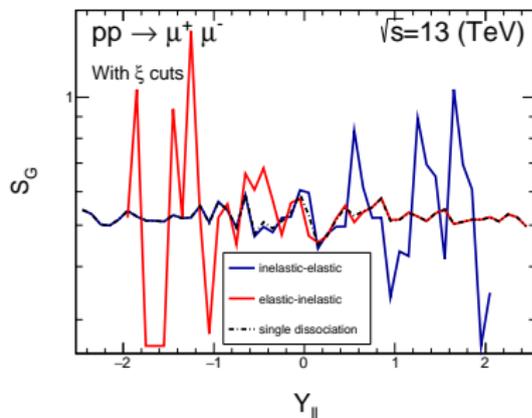
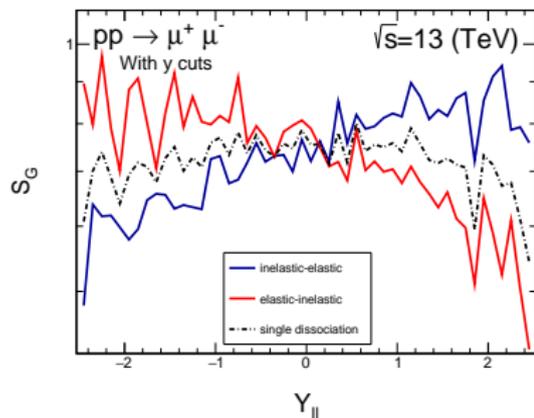
$$S_G(M_{II}) = \frac{d\sigma/dM_{II}|_{withSR}}{d\sigma/dM_{II}|_{withoutSR}}, \quad (8)$$

$$S_G(p_{t,pair}) = \frac{d\sigma/dp_{t,pair}|_{withSR}}{d\sigma/dp_{t,pair}|_{withoutSR}}, \quad (9)$$

# SUPERCHIC analysis, gap survival function

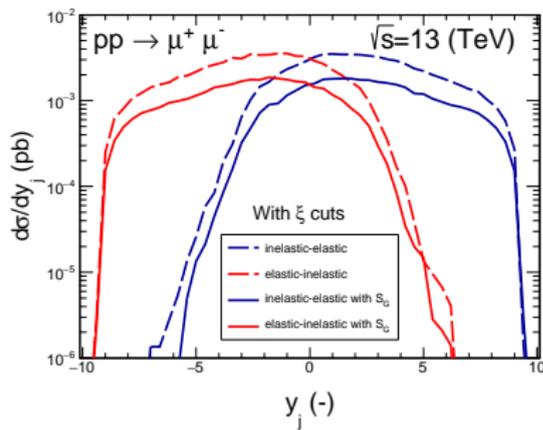
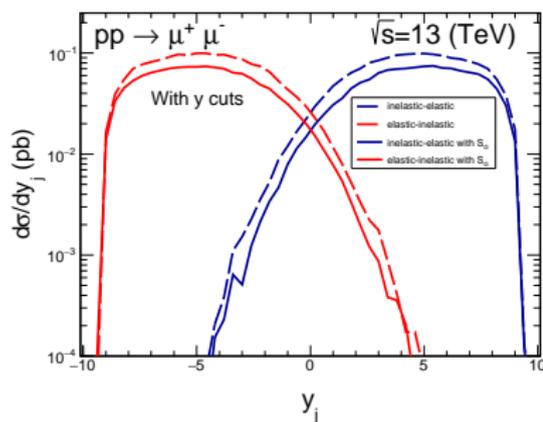


# SUPERCHIC analysis, gap survival function



**Rysunek:** The soft gap survival factor as a function of rapidity of the  $\mu^+ \mu^-$  pair for single proton dissociation. We show the result **without**  $\xi$  cuts (left panel) and **with**  $\xi$  cuts (right panel). The dash-dotted black line is effective gap survival factor for both single-dissociation components added together.

# SUPERCHIC analysis, minijet



**Rysunek:** Distribution in the (mini)jet rapidity for the inclusive case of no  $\xi$  cut (left panel) and when the cut on  $\xi$  is imposed (right panel) for elastic-inelastic and inelastic-elastic contributions as obtained from the SUPERCHIC generator. We show result **without** (dashed line) and **with** (solid line) soft rescattering correction.

# SUPERCHIC, gap survival factor due to jet emission

Tablica: Gap survival factor due to minijet emission. In all cases  $p_{1t}, p_{2t} > 15$  GeV.

contribution	without $S_G$	with $S_G$
cut on $Y_{  }$ only		
elastic-inelastic	0.76304	0.78756
inelastic-elastic	0.76278	0.78898
cut on $y_1$ and $y_2$ in addition		
elastic-inelastic	0.77366	0.79250
inelastic-elastic	0.76926	0.78744
cut on $\xi_1$ or $\xi_2$ in addition		
elastic-inelastic	0.48954	0.49986
inelastic-elastic	0.48374	0.49508
cut on $p_{t,pair} > 5$ GeV in addition		
elastic-inelastic	0.8505	0.8560
inelastic-elastic	0.8395	0.8600

# Conclusions

- ▶ In the present paper we have discussed dilepton production via photon-photon fusion **with one forward proton** which can be measured in forward detectors such as AFP for the ATLAS experiment.
- ▶ We have consider both **double-elastic** and **single-dissociative** contributions (it was argued that the contribution of **double dissociation is negligible** when forward proton is measured).
- ▶ In the latter case we have considered both continuum production as well as  $\Delta^+$ /resonance production. The continuum contribution is calculated for **different parametrizations of the deep-inelastic structure functions** from the literature.
- ▶ We have imposed **conditions on  $\xi_1$  or  $\xi_2$**  for the forward emitted protons. Several distributions have been shown and discussed.

# Conclusions

- ▶ Particularly interesting is the distribution in  $M_{//}$  and the distribution in  $Y_{//}$  which has **minimum at  $Y_{//} \sim 0$** . The minimum at  $Y_{//} = 0$  is caused by the experimental condition on  $\xi_{//}^{\pm}$  related to the leading proton.
- ▶ We have also made calculations with the popular **SUPERCHIC** generator and compared corresponding results to the results of our code(s). In general, the results are almost identical.
- ▶ We have calculated also soft rapidity gap survival factor (probability of no hadron emission in the range of the main (ATLAS, CMS) detector) as a function of  $M_{//}$ , transverse momentum of the dilepton pair, mass of the proton remnant and  $Y_{//}$ .
- ▶ No evident dependences on the variables have been found for the single dissociation, **except of distribution in  $Y_{//}$** . We have found different (much larger) gap survival factor for fully elastic contribution than for single proton

# Conclusions

- ▶ The soft gap survival factor for single dissociative contribution **strongly depends on whether proton is measured or not**. It is significantly smaller when proton is measured.
- ▶ We have also calculated **gap survival factor due to mini(jet) emission** by checking whether the minijet enters or not the main detector.
- ▶ The second type of the gap survival **also strongly depends on whether the outgoing proton is measured or not**. It is about 0.8 for inclusive case (no proton measurement) and about 0.5 for the case with proton measurement in forward proton detector (with typical limited  $\xi$  value).
- ▶ small  $p_{t,pair} \rightarrow$  large  $y_{jet} \rightarrow$  large  $S_{jet}$ .

# Outlook

- ▶ In the moment only **fiducial cross section** was measured. In future one should measure **differential distributions** (better statistics, or lower  $p_{t,min}$ ).
- ▶ Study **large  $p_{t,pair}$  region** or even in bins of  $p_{t,pair}$ .
- ▶ When calculating absorptive corrections it is assumed that any interaction (**independent of final state**) will destroy rapidity gap or break another experimental condition on final state.  
This has no deep justification for experimental conditions implemented for large luminosities. (pile ups).  
Study theoretically **final state related to absorptive proceses (extra pomeron exchange)**.

