

Central exclusive production of η_c and χ_{c0} in the light-front $k_\perp$ -factorization approach

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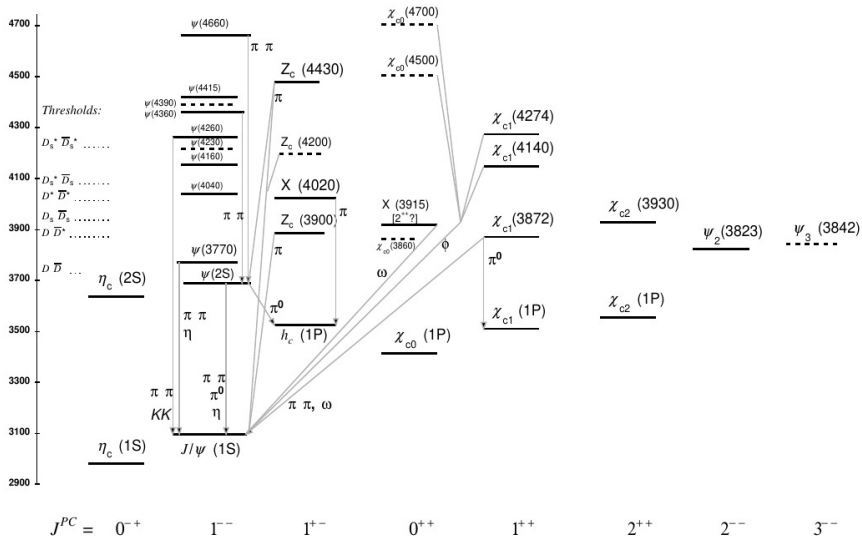
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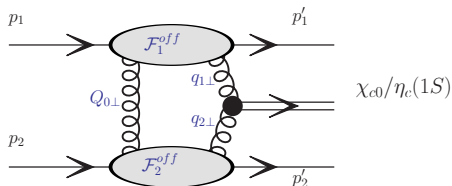
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Introduction $\Rightarrow \eta_c(1S), \chi_{c0} (1P)$



mass spectra of $c\bar{c}$ states P.A. Zyla *et al.* (Particle Data Group), Prog. Theor. Exp. Phys. **2020**, 083C01 (2020)

Introduction



Generic diagram for **central exclusive production** of η_c and χ_{c0} ,
[Phys.Rev.D102, 114028\(2020\)](#)

$$\mathcal{V}^{c_1 c_2} \Rightarrow \mathcal{V}^{c_1 c_2}(g^* g^* \rightarrow \eta_c(1S))$$

Prompt hadroproduction of $\eta_c(1S, 2S)$ in the k_T -factorization approach, [JHEP02, 037\(2020\)](#),

$$\mathcal{V}^{c_1 c_2} \Rightarrow \mathcal{V}^{c_1 c_2}(g^* g^* \rightarrow \chi_{c0}(1P))$$

Hadroproduction of scalar P -wave quarkonia in the light-front k_T -factorization approach
[JHEP06, 101\(2020\)](#)

$$\mathcal{M} = \frac{s}{2} \pi^2 \frac{1}{2} \frac{\delta_{c_1 c_2}}{N_c^2 - 1} \int d^2 Q \mathcal{V}^{c_1 c_2} \frac{\mathcal{F}_g^{\text{off}}(x_1, x', Q^2, q_1^2, \mu^2, t_1) \mathcal{F}_g^{\text{off}}(x_2, x', Q^2, q_2^2, \mu^2, t_2)}{Q^2 q_1^2 q_2^2},$$

Durham model of CEP, [Int. J. Mod. Phys. A 29, 1430031 \(2014\)](#), [arXiv:1405.0018 [hep-ph]]

$$\sigma = \frac{1}{2s} \frac{1}{2^8 \pi^4 s} \int |\mathcal{M}|^2 dt_1 dt_2 dy d\phi.$$

$$t_1 = (p_1 - p'_1)^2, \quad t_2 = (p_2 - p'_2)^2 \quad \text{and} \quad \phi \in (0, 2\pi)$$

R. S. Pasechnik, A. Szczurek, and O. V. Teryaev,
[Phys. Rev. D 78, 014007 \(2008\)](#),

Off-shell vertices

$$\mathcal{V}_{\mu\nu}^{ab}(g^* g^* \rightarrow \chi_{c0}) = 4\pi\alpha_s \frac{\text{Tr}[t^a t^b]}{\sqrt{N_c}} 2\mathcal{T}_{\mu\nu} = \frac{4\pi\alpha_s}{\sqrt{N_c}} \delta^{ab} \mathcal{T}_{\mu\nu},$$

$$\mathcal{T} = n_\nu^+ n_\mu^- \mathcal{T}_{\mu\nu} = |\mathbf{q}_1| |\mathbf{q}_2| G_1(q_1^2, q_2^2) + (\mathbf{q}_1 \cdot \mathbf{q}_2) G_2(q_1^2, q_2^2),$$

$$G_1(q_1^2, q_2^2) = |\mathbf{q}_1| |\mathbf{q}_2| \frac{4m_c}{q_2^2} \int \frac{dz d^2 \mathbf{k}}{z(1-z)16\pi^3} \psi_{\chi_{c0}}(z, \mathbf{k}) 2z(1-z)(2z-1) \left[\frac{1}{l_A^2 + \varepsilon^2} - \frac{1}{l_B^2 + \varepsilon^2} \right]$$

$$G_2(q_1^2, q_2^2) = 4m_c \int \frac{dz d^2 \mathbf{k}}{z(1-z)16\pi^3} \psi_{\chi_{c0}}(z, \mathbf{k}) \left[\frac{1-z}{l_A^2 + \varepsilon^2} + \frac{z}{l_B^2 + \varepsilon^2} \right] \\ + \frac{4m_c}{q_2^2} \int \frac{dz d^2 \mathbf{k}}{z(1-z)16\pi^3} \psi_{\chi_{c0}}(z, \mathbf{k}) 4z(1-z) \left[\frac{\mathbf{q}_2 \cdot \mathbf{l}_A}{l_A^2 + \varepsilon^2} - \frac{\mathbf{q}_2 \cdot \mathbf{l}_B}{l_B^2 + \varepsilon^2} \right],$$

$$\mathcal{V}_{\mu\nu}^{ab}(g^* g^* \rightarrow \eta_c) = (-i)4\pi\alpha_s \epsilon_{\mu\nu\alpha\beta} q^\alpha q^\beta \frac{\delta^{ab}}{2\sqrt{N_c}} 2I(q_1^2, q_2^2),$$

where $I(q_1^2, q_2^2) = F_{\gamma^* \gamma^* \rightarrow \eta_c}(q_1^2, q_2^2)/(e_c^2 \sqrt{N_c})$.

$$I(q_1^2, q_2^2) = 4m_c \int \frac{dz d^2 \mathbf{k}}{z(1-z)16\pi^3} \psi_{\eta_c}(z, \mathbf{k}) \left\{ \frac{1-z}{(\mathbf{k} - (1-z)\mathbf{q}_2)^2 + z(1-z)q_1^2 + m_c^2} \right. \\ \left. + \frac{z}{(\mathbf{k} + z\mathbf{q}_2)^2 + z(1-z)q_1^2 + m_c^2} \right\},$$

Off-diagonal gluons

KMR off-diagonal gluon:

[Int. J. Mod. Phys. A **29**, 1430031 \(2014\)](#), [arXiv:1405.0018 [hep-ph]], [Eur. Phys. J. C **35**, 211–220 \(2004\)](#)

$$\mathcal{F}_{g,\text{KMR}}^{\text{off}}(x_i, x', Q_{\perp}^2, q_{i\perp}^2, \mu^2, t_i) = R_g \frac{d}{d \ln q_{\perp}^2} \left[xg(x, q_{\perp}^2) \sqrt{T_g(q_{\perp}^2, \mu^2)} \right]_{q_{\perp}^2 = Q_{\perp}^2} F(t),$$

$$Q_{i\perp}^2 = \min(Q_{\perp}^2, q_{i\perp}^2), \quad i = 1, 2 - \text{Durham prescription}$$

$$Q_{i\perp}^2 = \sqrt{Q_{\perp}^2 q_{i\perp}^2} \quad i = 1, 2 - \text{BPSS prescription}$$

CDHI off-diagonal gluon:

[Eur. Phys. J. C **61**, 369–390 \(2009\)](#)

$$\mathcal{F}_{g,\text{CDHI}}^{\text{off}}(x_i, x', Q_{\perp}^2, q_{i\perp}^2, \mu^2, t_i) = R_g \left[\frac{\partial}{\partial \log \bar{Q}^2} \sqrt{T_g(\bar{Q}^2, \mu^2)} xg(x, \bar{Q}^2) \right] \cdot \frac{2Q_{\perp}^2 q_{\perp}^2}{Q_{\perp}^4 + q_{\perp}^4} \cdot F(t),$$

$$F(t) = \exp\left(\frac{bt}{2}\right), \quad b = 4 \text{ GeV}^{-2},$$

PST off-diagonal:

[Phys. Rev. D **78**, 014007 \(2008\)](#).

$$\mathcal{F}_{g,\text{PST}}^{\text{off}}(x_i, x', Q_{\perp}^2, q_{i\perp}^2, \mu^2, t_i) = \sqrt{Q_{\perp}^2 f_g^{\text{GBW}}(x', Q_{\perp}^2) q_{\perp}^2 f_g^{\text{GBW}}(x, q_{\perp}^2)} \sqrt{T_g(q_{\perp}^2, \mu^2)} F(t),$$

$$f_g^{\text{GBW}}(x, q_{\perp}^2) = \frac{3\sigma_0}{4\pi^2\alpha_s} R_0^2 q_{\perp}^2 \exp[-R_0^2 q_{\perp}^2],$$

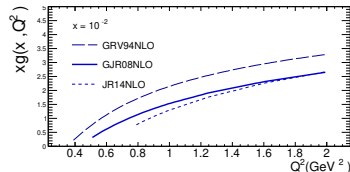
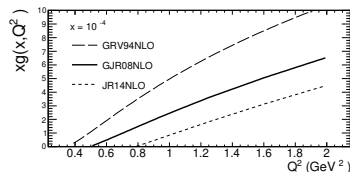
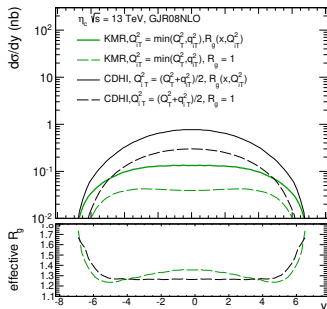
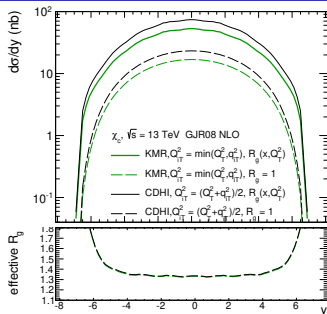
[J.HighEnergyPhys.03\(2018\)102.](#)

$$f_g^{RS}(x, |\mathbf{q}|) = q^2 \frac{\sigma_0}{\alpha_s} \frac{N_c}{8\pi^2} \int_0^\infty r dr J_0(|\mathbf{q}|r) \left(1 - \frac{\sigma(x, r)}{\sigma_0}\right).$$

[Phys.Rev.D88, 074016\(2013\)](#)

$$T_g(q_{\perp}^2, \mu^2) = \exp \left[- \int_{q_{\perp}^2}^{\mu^2} \frac{dk_{\perp}^2}{k_{\perp}^2} \frac{\alpha_s(k_{\perp}^2)}{2\pi} \right] \times \int_0^{1-\Delta} \left[z P_{gg}(z) + \sum_q P_{qg}(z) \right] dz, \\ \mu^2 = M^2 + q_{\perp}^2.$$

Effective skewedness correction

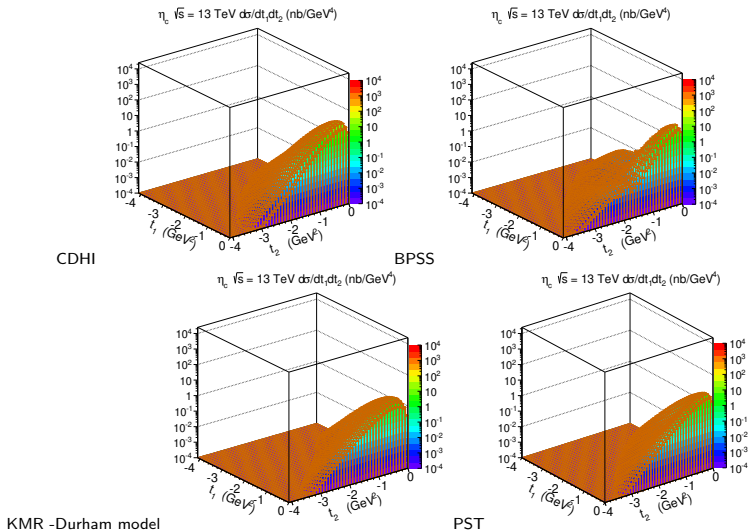


Shuvaev prescription

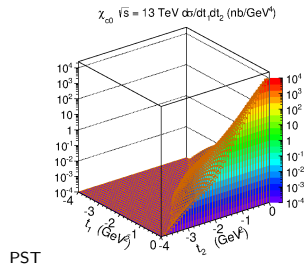
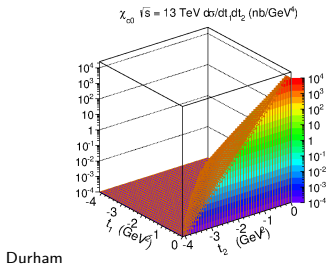
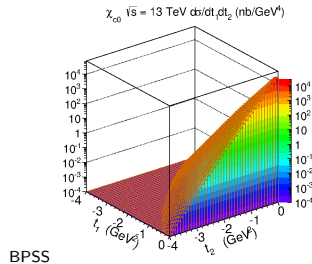
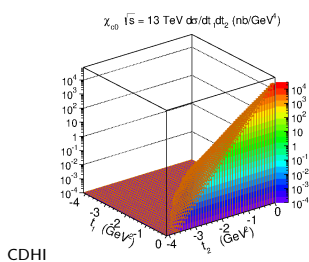
$$R_g = \frac{2^{2\lambda+3}}{\sqrt{\pi}} \frac{\Gamma(\lambda + 5/2)}{\Gamma(\lambda + 4)},$$

$$\lambda = \frac{d}{d \ln(1/x)} \left[\ln \left(xg(x, q_{\perp}^2) \right) \right]$$

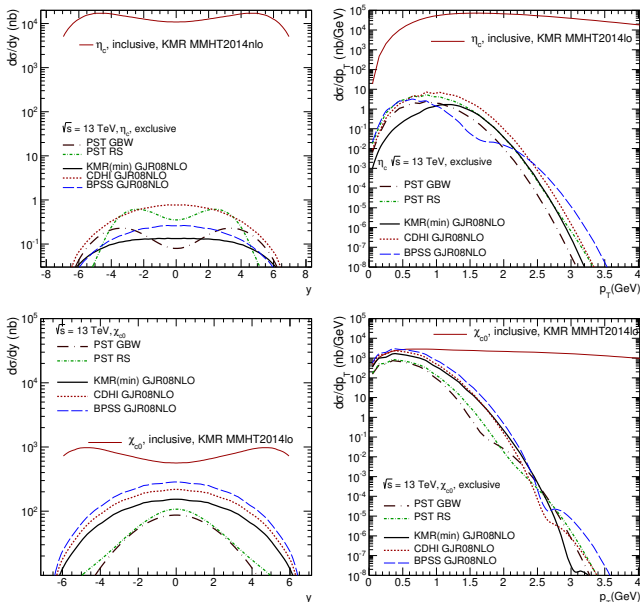
η_c - distribution in $t_1 \times t_2$, $\sqrt{s} = 13 \text{ TeV}$



χ_{c0} - distribution in $t_1 \times t_2$, $\sqrt{s} = 13 \text{ TeV}$



Exclusive vs. inclusive distributions



Absorptive correction to $pp \rightarrow pVp$ processes

$$\mathcal{M}(Y, y, \mathbf{p}_1, \mathbf{p}_2) = \mathcal{M}^{(0)}(Y, y, \mathbf{p}_1, \mathbf{p}_2) - \delta\mathcal{M}(Y, y, \mathbf{p}_1, \mathbf{p}_2),$$

$$\mathcal{M}^{(0)}(Y, y, \mathbf{p}_1, \mathbf{p}_2) = i s \Phi_1(\mathbf{p}_1) R_{\mathbf{p}}(Y - y, \mathbf{p}_1^2) \\ \times V(\mathbf{p}_1, \mathbf{p}_2) R_{\mathbf{p}}(y, \mathbf{p}_2^2) \Phi_2(\mathbf{p}_2)$$

$$\delta\mathcal{M}(Y, 0, \mathbf{p}_1, \mathbf{p}_2) = \int \frac{d^2 \mathbf{k}}{2(2\pi)^2} T(s, \mathbf{k}) \exp\left(-\frac{1}{2} B_D(\mathbf{p}_1 + \mathbf{k})^2\right) \\ \exp\left(-\frac{1}{2} B_D(\mathbf{p}_2 - \mathbf{k})^2\right) \times V(\mathbf{p}_1 + \mathbf{k}, \mathbf{p}_2 - \mathbf{k})$$

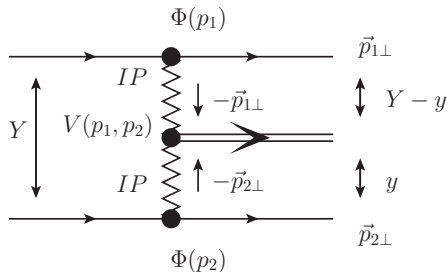
$$T(s, \mathbf{k}) = \sigma_{\text{tot}}^{pp}(s) \exp\left(-\frac{1}{2} B_{\text{el}}(s) \mathbf{k}^2\right)$$

$$\sqrt{s} = 13 \text{ TeV} \Rightarrow \sigma_{\text{tot}}^{pp} = (110.6 \pm 3.4) \text{ mb},$$

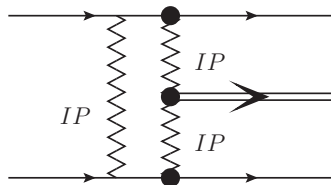
$$B_{\text{el}} = (20.36 \pm 0.19) \text{ GeV}^{-2}$$

G. Antchev *et al.* [TOTEM Collaboration],

[Eur. Phys. J. C 79, no.2, 103 \(2019\)](#)

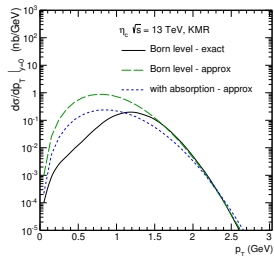
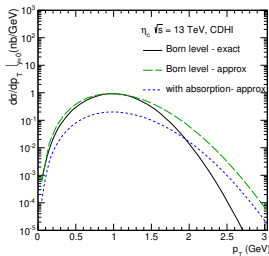
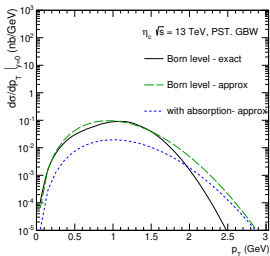
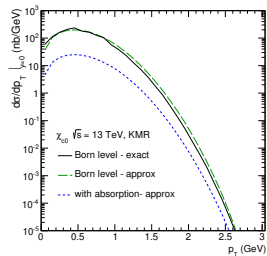
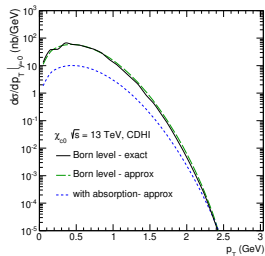
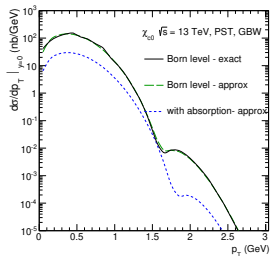


Born level diagram



absorptive correction

Absorptive correction - results



Gap survival probability at mid rapidity

χ_{c0}	$\frac{d\sigma}{dy}_{\text{tot}} _{y=0}$ [nb]	$\frac{d\sigma}{dy}_{\text{tot}}^{\text{abs}} _{y=0}$ [nb]	$S^2_{y=0}$
PST GBW	17	3.7	0.22
PST RS	21	4.5	0.21
CDHI GJR08NLO	42	7.5	0.18
KMR GJR08NLO	29	3.7	0.13
BPSS GJR08NLO	61	8.0	0.13

η_c	$\frac{d\sigma}{dy}_{\text{tot}} _{y=0}$ [nb]	$\frac{d\sigma}{dy}_{\text{tot}}^{\text{abs}} _{y=0}$ [nb]	$S^2_{y=0}$
PST GBW	1.8×10^{-2}	3.9×10^{-3}	0.22
PST RS	9.0×10^{-3}	1.9×10^{-3}	0.21
CDHI GJR08NLO	1.8×10^{-1}	4.0×10^{-2}	0.22
KMR GJR08NLO	1.3×10^{-1}	3.0×10^{-2}	0.23
BPSS GJR08NLO	5.8×10^{-2}	2.2×10^{-2}	0.38

$$S^2 \equiv \frac{d\sigma/dy|_{y=0}}{d\sigma_{\text{Born}}/dy|_{y=0}}$$

Summary

- Transition amplitude for $g^* g^* \rightarrow \eta_c$ and $g^* g^* \rightarrow \chi_{c0}$ was calculated using light-cone wave functions of $c\bar{c}$ states in the frame work of potential models.
- We also proposed a way to calculate the soft effects (in the region of small gluon transverse momenta) using the GBW or RS UGDs, which were obtained from the respective color dipole cross sections and a simple (PST) prescription for its off-diagonal extrapolation.
- Central exclusive processes in proton-proton colisions are sensitive to the low scale, especially η_c , which is the main uncertainties in the results.
- In our calculation of absorptive corrections, we restricted ourselves to the so-called elastic rescattering correction.
- Depending on the gluon distribution used, we obtain for the χ_c the gap survival values of $S^2 = (0.13 - 0.21)$, while for the η_c production, they are somewhat higher, $S^2 = (0.21 - 0.38)$.