

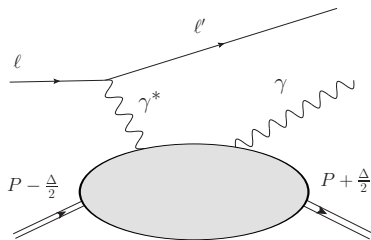
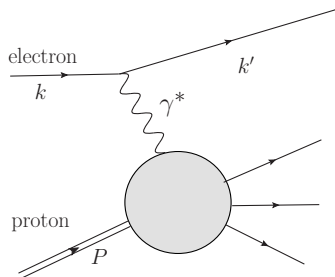
# Recent developments in exclusive nucleon science at EIC

Cédric Lorcé, **Cédric Mezrag**,  
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CPHT, École polytechnique,  
CEA Saclay, Irfu DPhN,  
Università di Pavia & INFN sezione di Pavia

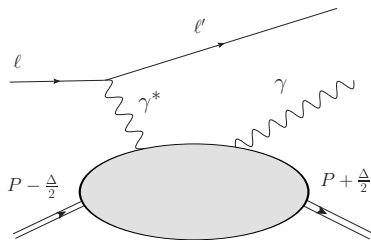
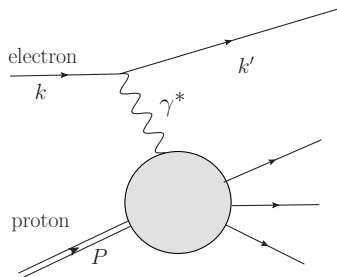
December 15<sup>th</sup>, 2020

# Why deep exclusive processes ?

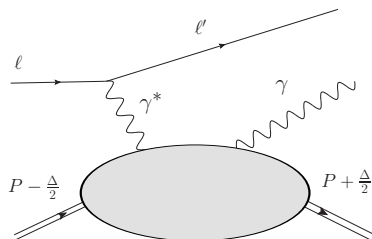
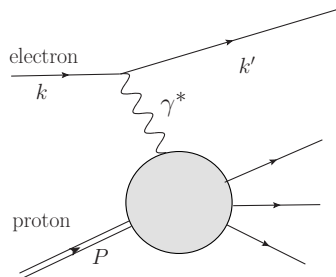


- Deep exclusive processes are generally more difficult to measure than inclusive ones

# Why deep exclusive processes ?



- Deep exclusive processes are generally more difficult to measure than inclusive ones
- Reason : we require *not* to break the proton  $\rightarrow$  small cross sections



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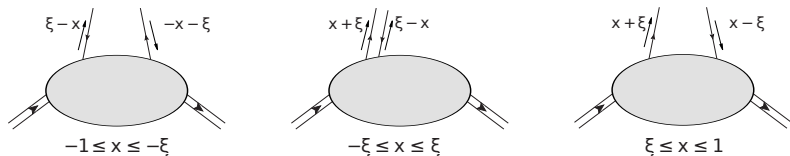
## A curse and a blessing

Not breaking the proton allows one to study the distribution of quarks and gluons in coordinate space

# Nucleon tomography through Generalized Partons Distributions (GPDs)

- Generalized Parton Distributions (GPDs):

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  - ▶ “hadron-parton” amplitudes which depend on three variables  $(x, \xi, t)$  and a scale  $\mu$ ,



- ★  $x$ : average momentum fraction carried by the active parton
- ★  $\xi$ : skewness parameter  $\xi \simeq \frac{x_B}{2-x_B}$
- ★  $t$ : the Mandelstam variable

- Generalized Parton Distributions (GPDs):

- ▶ “hadron-parton” amplitudes which depend on three variables  $(x, \xi, t)$  and a scale  $\mu$ ,
- ▶ are defined in terms of a non-local matrix element,

$$\begin{aligned} & \frac{1}{2} \int \frac{e^{ixP^+z^-}}{2\pi} \langle P + \frac{\Delta}{2} | \bar{\psi}^q(-\frac{z}{2}) \gamma^+ \psi^q(\frac{z}{2}) | P - \frac{\Delta}{2} \rangle dz^- |_{z^+=0, z=0} \\ &= \frac{1}{2P^+} \left[ H^q(x, \xi, t) \bar{u} \gamma^+ u + E^q(x, \xi, t) \bar{u} \frac{i\sigma^{+\alpha} \Delta_\alpha}{2M} u \right]. \end{aligned}$$

$$\begin{aligned} & \frac{1}{2} \int \frac{e^{ixP^+z^-}}{2\pi} \langle P + \frac{\Delta}{2} | \bar{\psi}^q(-\frac{z}{2}) \gamma^+ \gamma_5 \psi^q(\frac{z}{2}) | P - \frac{\Delta}{2} \rangle dz^- |_{z^+=0, z=0} \\ &= \frac{1}{2P^+} \left[ \tilde{H}^q(x, \xi, t) \bar{u} \gamma^+ \gamma_5 u + \tilde{E}^q(x, \xi, t) \bar{u} \frac{\gamma_5 \Delta^+}{2M} u \right]. \end{aligned}$$

D. Müller *et al.*, Fortsch. Phys. 42 101 (1994)

X. Ji, Phys. Rev. Lett. 78, 610 (1997)

A. Radyushkin, Phys. Lett. B380, 417 (1996)

4 GPDs without helicity transfer + 4 helicity flip GPDs



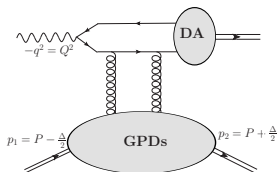
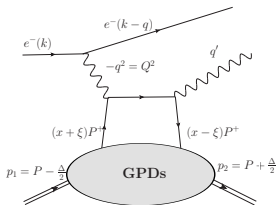
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- ▶ are related to PDF in the forward limit  $H(x, \xi = 0, t = 0; \mu) = q(x; \mu)$
- ▶ are universal, *i.e.* are related to the Compton Form Factors (CFFs) of various exclusive processes through convolutions

$$\mathcal{H}(\xi, t) = \int dx C(x, \xi) H(x, \xi, t)$$



- Polynomiality Property:

$$\int_{-1}^1 dx x^m H^q(x, \xi, t; \mu) = \sum_{j=0}^{\lfloor \frac{m}{2} \rfloor} \xi^{2j} C_{2j}^q(t; \mu) + \text{mod}(m, 2) \xi^{m+1} C_{m+1}^q(t; \mu)$$

X. Ji, J.Phys.G 24 (1998) 1181-1205

A. Radyushkin, Phys.Lett.B 449 (1999) 81-88

Special case :

$$\int_{-1}^1 dx H^q(x, \xi, t; \mu) = F_1(t)$$

Lorentz Covariance

- Polynomiality Property:
- Positivity property:

Lorentz Covariance

$$\left| H^q(x, \xi, t) - \frac{\xi^2}{1 - \xi^2} E^q(x, \xi, t) \right| \leq \sqrt{\frac{q\left(\frac{x+\xi}{1+\xi}\right) q\left(\frac{x-\xi}{1-\xi}\right)}{1 - \xi^2}}$$

A. Radysuhkin, Phys. Rev. D59, 014030 (1999)

B. Pire *et al.*, Eur. Phys. J. C8, 103 (1999)

M. Diehl *et al.*, Nucl. Phys. B596, 33 (2001)

P.V. Pobilitza, Phys. Rev. D65, 114015 (2002)

Positivity of Hilbert space norm

- Polynomiality Property:
- Positivity property:
- Support property:

Lorentz Covariance

Positivity of Hilbert space norm

$$x \in [-1; 1]$$

M. Diehl and T. Gousset, Phys. Lett. B428, 359 (1998)

Relativistic quantum mechanics

- Polynomiality Property:

Lorentz Covariance

- Positivity property:

Positivity of Hilbert space norm

- Support property:

Relativistic quantum mechanics

- Scale evolution property

→ generalization of DGLAP and ERBL evolution equations

D. Müller *et al.*, Fortschr. Phys. 42, 101 (1994)

Renormalization

- Polynomiality Property:

Lorentz Covariance

- Positivity property:

Positivity of Hilbert space norm

- Support property:

Relativistic quantum mechanics

- Scale evolution property

Renormalization

## Problem

- There is no model (until now) fulfilling *a priori* all these constraints.
- Lattice QCD computations remain very challenging.





- In the limit  $\xi \rightarrow 0$ , one recovers a density interpretation:
  - ▶ 1D in momentum space ( $x$ )
  - ▶ 2D in coordinate space  $\vec{b}_\perp$  (related to  $t$ )

M. Burkardt, Phys. Rev. D62, 071503 (2000)

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- Possibility to extract density from experimental data

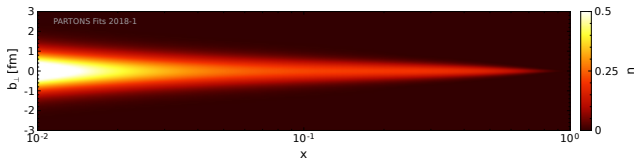


figure from H. Moutarde *et al.*, EPJC 78 (2018) 890

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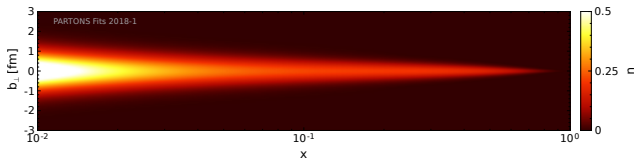


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- Correlation between  $x$  and  $b_\perp \rightarrow$  going beyond PDF and FF.

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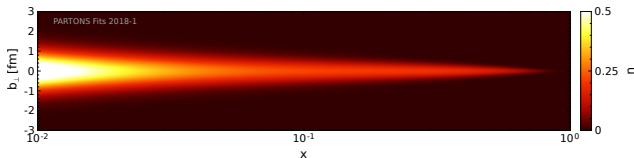
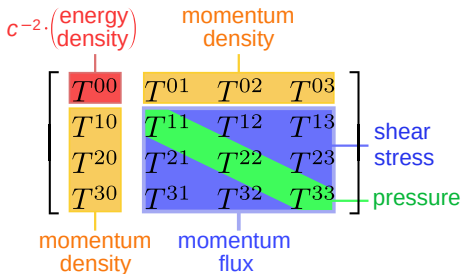


figure from H. Moutarde *et al.*, EPJC 78 (2018) 890

- Correlation between  $x$  and  $b_\perp \rightarrow$  going beyond PDF and FF.
- Caveat: no experimental data at  $\xi = 0$   
 $\rightarrow$  extrapolations (and thus model-dependence) are necessary

# Interpretation of GPDs II

## Connection to the Energy-Momentum Tensor



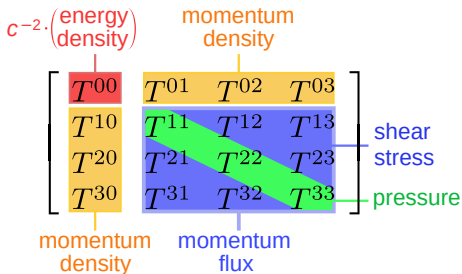
How energy, momentum, pressure are shared between quarks and gluons

Caveat: renormalization scheme and scale dependence

- C. Lorcé *et al.*, PLB 776 (2018) 38-47,  
M. Polyakov and P. Schweitzer,  
IJMPA 33 (2018) 26, 1830025  
C. Lorcé *et al.*, Eur.Phys.J.C 79 (2019) 1, 89

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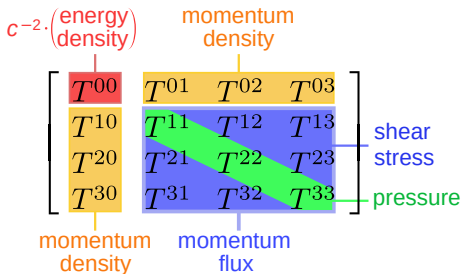
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$$\begin{aligned}
 \langle p', s' | T_{q,g}^{\mu\nu} | p, s \rangle = & \bar{u} \left[ P^{\{\mu\gamma\nu\}} A_{q,g}(t; \mu) + \frac{\Delta^\mu \Delta^\nu - g^{\mu\nu} \Delta^2}{M} C_{q,g}(t; \mu) \right. \\
 & \left. + M g^{\mu\nu} \bar{C}_{q,g}(t; \mu) + \frac{P^{\{\mu i \sigma^\nu\} \Delta}}{2M} B_{q,g}(t; \mu) + \frac{P^{\{\mu i \sigma^\nu\} \Delta}}{2M} D_{q,g}(t; \mu) \right] u
 \end{aligned}$$

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$$\int_{-1}^1 dx x H_q(x, \xi, t; \mu) = A_q(t; \mu) + (2\xi)^2 C_q(t; \mu)$$

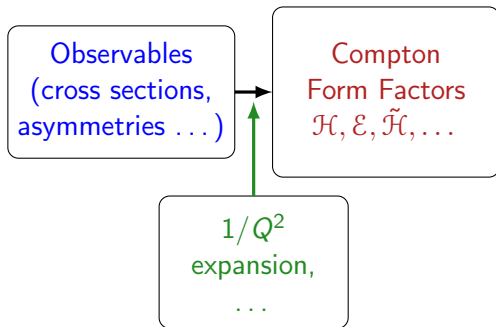
$$\int_{-1}^1 dx x E_q(x, \xi, t; \mu) = B_q(t; \mu) - (2\xi)^2 C_q(t; \mu)$$

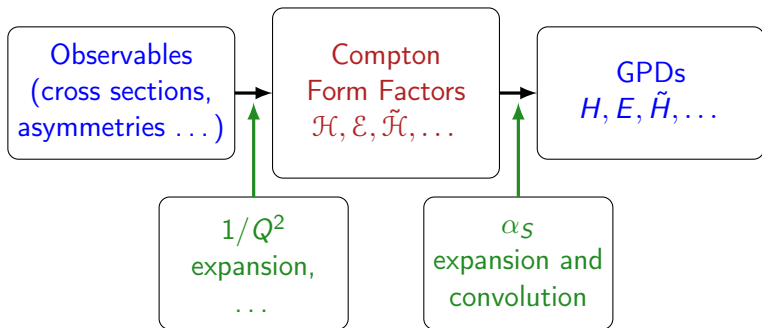
- Ji sum rule
- Fluid mechanics analogy

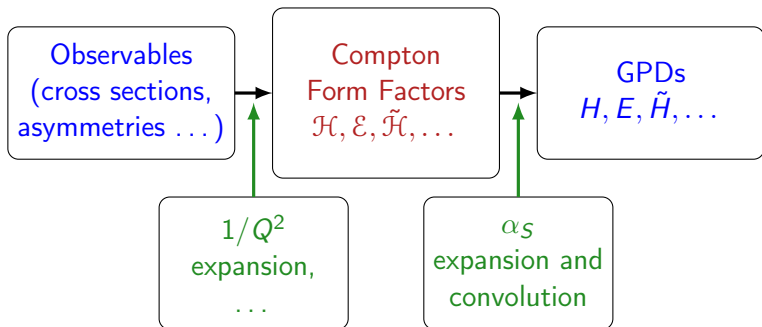
X. Ji, PRL 78, 610-613 (1997)  
 M.V. Polyakov PLB 555, 57-62 (2003)

Observables  
(cross sections,  
asymmetries ...)

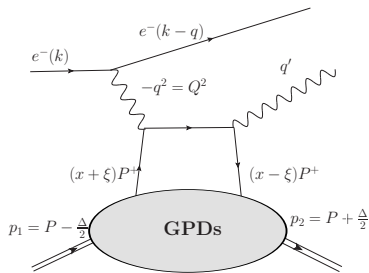




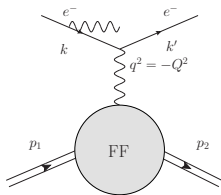
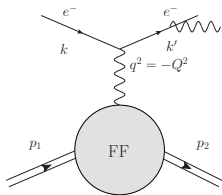
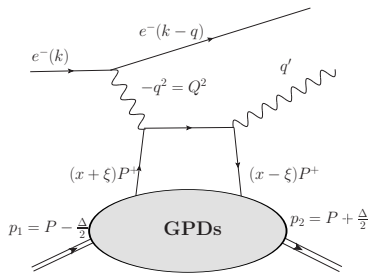




- CFFs play today a central role in our understanding of GPDs
- Extraction generally focused on CFFs



- Best studied experimental process connected to GPDs  
→ Data taken at Hermes, Compass, JLab 6, JLab 12

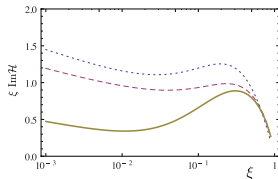
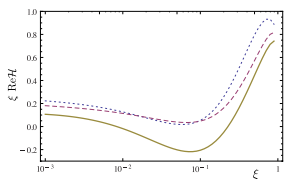
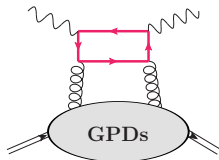


- Best studied experimental process connected to GPDs
  - Data taken at Hermes, Compass, JLab 6, JLab 12
- Interferes with the Bethe-Heitler (BH) process
  - ▶ Blessing: Interference term boosted w.r.t. pure DVCS one
  - ▶ Curse: access to the angular modulation of the pure DVCS part difficult

M. Defurne *et al.*, Nature Commun. 8 (2017) 1, 1408

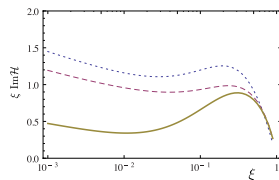
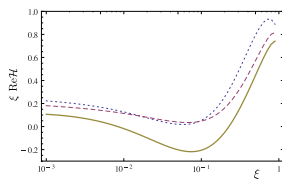
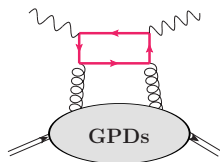
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H. Moutarde *et al.*, PRD 87 (2013) 5, 054029

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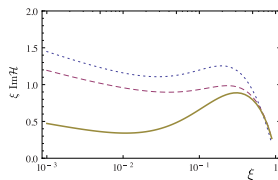
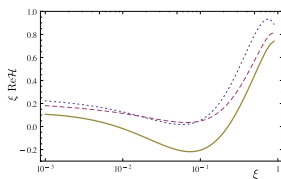
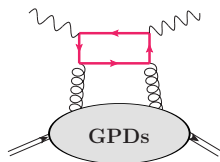
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- Recent N2LO studies, impact needs to be assessed

V. Braun *et al.*, JHEP 09 (2020) 117



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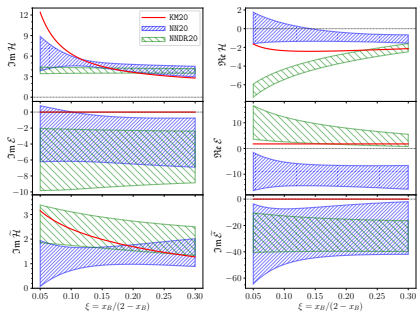
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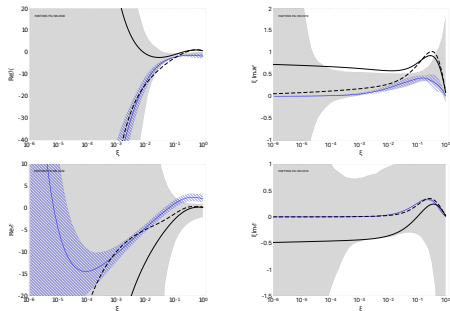
V. Braun *et al.*, JHEP 09 (2020) 117

- Evolution equations: needs for open evolution codes

A. Vinnikov, hep-ph/0604248



M. Cuić *et al.*, PRL 125, (2020), 232005



H. Moutarde *et al.*, EPJC 79, (2019), 614

- Recent effort on bias reduction in CFF extraction (ANN)  
additional ongoing studies, J. Grigsby *et al.*, arXiv:2012.04801
- Studies of ANN architecture to fulfil GPDs properties (dispersion relation, polynomiality, . . .)
- Recent efforts on propagation of uncertainties (allowing impact studies for EIC and EICC)

- At all order in  $\alpha_S$ , dispersion relations relate the real and imaginary parts of the CFF.

I. Anikin and O. Teryaev, PRD 76 056007  
M. Diehl and D. Ivanov, EPJC 52 (2007) 919-932

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- For instance at LO:

$$\text{Re}(\mathcal{H}(\xi, t)) = \frac{1}{\pi} \int_{-1}^1 dx \text{Im}(\mathcal{H}(x, t)) \left[ \frac{1}{\xi - x} - \frac{1}{\xi + x} \right] + \underbrace{2 \int_{-1}^1 d\alpha \frac{D(\alpha, t)}{1 - \alpha}}_{\text{Independent of } \xi}$$

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- $D(\alpha, t)$  is related to the EMT (pressure and shear forces)

M.V. Polyakov PLB 555, 57-62 (2003)

# Dispersion relation and the D-term

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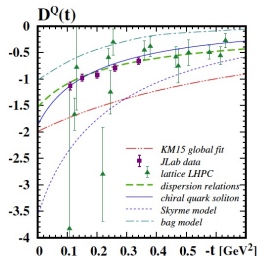
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M.V. Polyakov PLB 555, 57-62 (2003)



- First attempt from JLab 6 GeV data  
**Warning:** Systematic uncertainties are not reported on figure

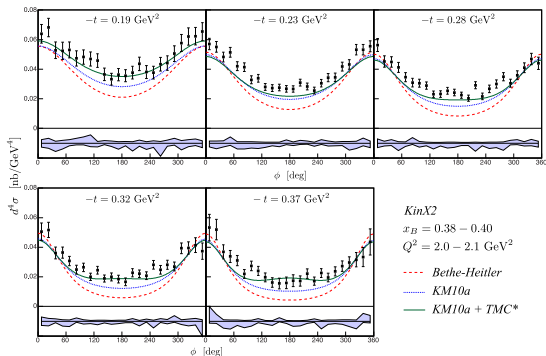
Burkert *et al.*, Nature 557 (2018) 7705, 396-399

- Tensions with other studies

K. Kumericki, Nature 570 (2019) 7759, E1-E2  
H. Moutarde *et al.*, Eur.Phys.J.C 79 (2019) 7, 614

- Model dependence, scheme/scale dependence

figure from M. Polyakov and P Schweitzer,  
IJMPA 33 (2018) 26, 1830025  
data from Burkert *et al.*, Nature 557 (2018)

Kinematical corrections in  $t/Q^2$  and  $M^2/Q^2$ V. Braun *et al.*, PRL 109 (2012), 242001M. Defurne *et al.*, PRC 92 (2015) 55202

- Sizeable even for  $t/Q^2 \sim 0.1$
- Not currently included in global fits.

- DVCS off the deuteron

F. Cano *et al.*, EPJA 19 (2004) 423

M. Benali *et al.*, Nature Phys. 16 (2020) 2, 191-198

- ▶ Incoherent scattering : DVCS off the quasi-free neutron  
→ significant step toward flavour separation

M. Cuic *et al.*, PRL 125 (2020) 23, 232005

- ▶ Coherent scattering : probing partons inside a deuteron  
→ Spin 1 target: richer spin structure → more GPDs  
→ Extraction more complicated



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F. Cano *et al.*, EPJA 19 (2004) 423

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→ Extraction more complicated

- DVCS off  $\text{He}^4$

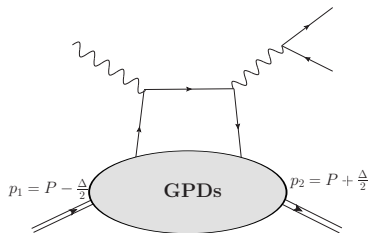
M. Hattawy *et al.*, PRL 119 (2017) 20, 202004

- ▶ Coherent scattering on a scalar target

→ Less spin structure → less GPDs

- ▶ Incoherent scattering: information on the structure of a bound nucleon

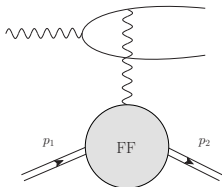
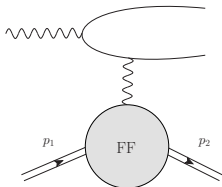
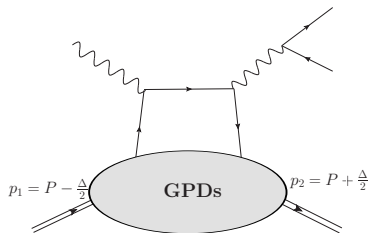
S. Fucini *et al.*, arXiv:2008.11437



- Amplitude related to the DVCS one ( $Q^2 \rightarrow -Q^2, \dots$ )  
→ theoretical development for DVCS can be extended to TCS

E. Berger *et al.*, EPJC 23 (2002) 675

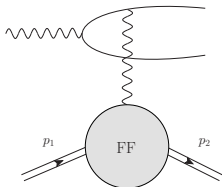
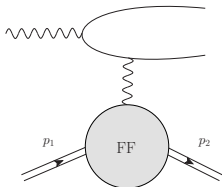
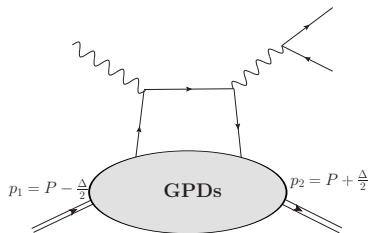
- Excellent test of GPD universality



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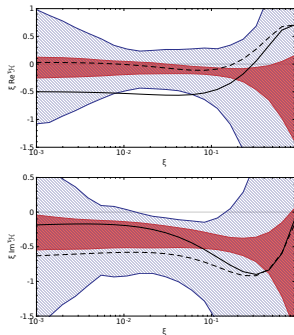
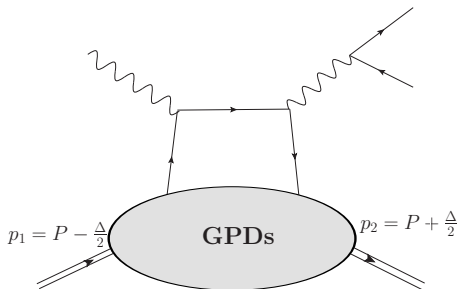
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E. Berger *et al.*, EPJC 23 (2002) 675

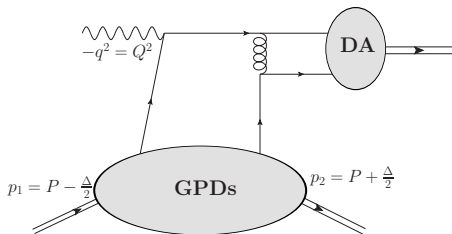
- Excellent test of GPD universality
- Interferes with the Bethe-Heitler (BH) process
- Same type of final states as exclusive quarkonium production



O. Grocholski *et al.*, EPJC 80, (2020) 61

- DVCS Data-driven prediction for TCS at LO and NLO
- First experimental measurement at JLab through forward-backward asymmetry (interference term)

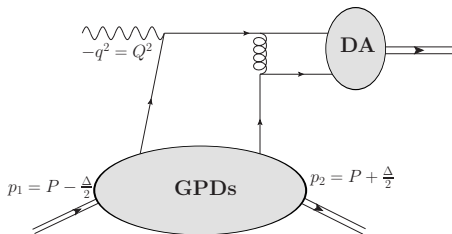
P. Chatagnon *et al.*, in preparation



- Factorization proven for  $\gamma_L^*$

J. Collins *et al.*, PRD 56 (1997) 2982-3006

- Same GPDs than previously
- Depends on the meson DA



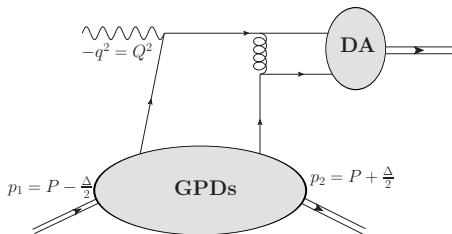
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- ▶ Select singlet ( $V_L$ ), non-singlet (pseudo-scalar mesons) contributions or chiral-odd distributions ( $V_T$ )
- ▶ Help flavour separation
- ▶ Leading-order access to gluon GPDs



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  - ▶ Help flavour separation
  - ▶ Leading-order access to gluon GPDs
- Factorisation proven  $\neq$  factorisation visible at achievable  $Q^2$ 
  - ▶ Leading-twist dominance at a given  $Q^2$  is process-dependent  
→ for DVMP it can change between mesons.
  - ▶ At JLab kinematics, higher-twist contributions are very strong  
→ hide factorisation of  $\sigma_L$



- $\pi^0$  electroproduction

- ▶  $\sigma_T > \sigma_L$  at JLab 6 and likely at JLab 12 kinematics ( $Q^2 = 8.3 \text{ GeV}^2$ )

M. Dlamini *et al.*, arXiv:2011.11125

- ▶ No extraction of  $\sigma_L$  at JLab 12 yet

- ▶ Model-dependent treatment of  $\sigma_T$  using higher-twist contributions

S. V. Goloskokov and P. Kroll, EPJC 65, 137 (2010)

G. Goldstein *et al.*, PRD 91 (2015) 11, 114013

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- ▶  $\sigma_T = \sigma_L$  for  $Q^2 \simeq 1.5\text{GeV}^2$  and  $\frac{\sigma_L}{\sigma_T}$  increases with  $Q^2$   
see e.g. L. Favart, EPJA 52 (2016) 6, 158
- ▶  $\sigma_T \neq 0$  though  $\rho_{0,T}$  production vanishes at leading twist  
→ No LT access to chiral-odd GPDs.  
M. Diehl *et al.*, PRD 59 (1999) 034023
- ▶ Sizeable higher-twist effects need to be understood  
I. Anikin *et al.*, PRD 84 (2011) 054004

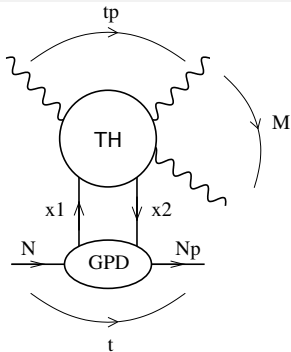
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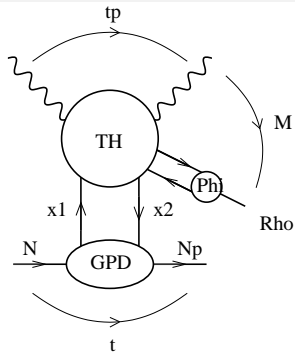
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DVMP is as interesting as challenging  
Higher  $Q^2$  data would be more than welcome

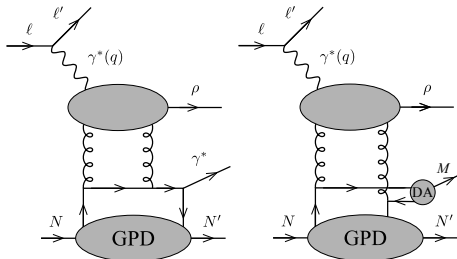


A. Pedrak *et al.*, PRD 96 (2017) 7, 074008



R. Boussarie *et al.*, JHEP 02 (2017) 054

- New combination of CFFs  $\rightarrow$  welcome in global fits.
- LT access to chiral-odd GPDs in the  $(\gamma, \rho)$  case.
- Electroproduction done for  $\gamma\gamma$ .
- Additional particle in the final state  $\rightarrow$  more luminosity



D. Ivanov *et al.*, PLB 550 (2002) 65  
 B. Pire *et al.*, PRD 101 (2020) 7, 074005  
 W. Cosyn *et al.*, PRD 102 (2020) 5, 054003

- Rapidity gap between the  $\rho$  and the  $(\gamma^*, N)$  or  $(M, N)$  system
- Only sensitive to the  $-\xi < x < \xi$  region of the GPDs
- No gluon GPDs (discrete symmetries)
- On-going evaluations of observables at the EIC kinematics

## PARTONS

partons.cea.fr



B. Berthou *et al.*, EPJC 78 (2018) 478

## Gepard

calculon.phy.hr/gpd/server/index.html



K. Kumericki, EPJ Web Conf. 112 (2016) 01012

- Similarities : NLO computations, BM formalism, ANN, ...
- Differences : models, evolution, dissemination, ...

### Physics impact

These integrated softwares are the mandatory path toward reliable multichannel analyses.

- Phenomenological parametrisations (KM, GK, VGG, MSW, ...)
- Extension of the relation between CFF and observables

B. Kriesten *et al.* PRD 101 (2020) 054021

- New modelling efforts

N. Chouika *et al.*, EPJC 77, (2017) 906  
S. Rodini, B. Pasquini *et al.*, in preparation

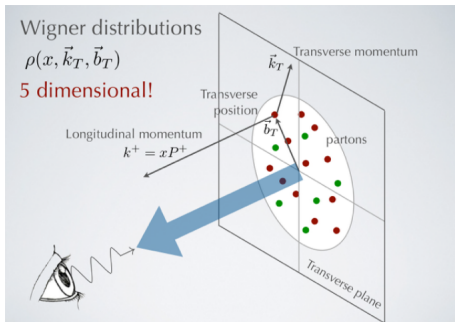
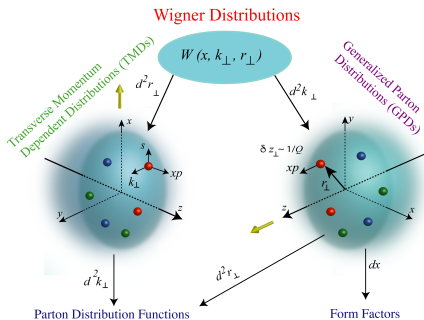
- Forthcoming Lattice and Continuum QCD computations

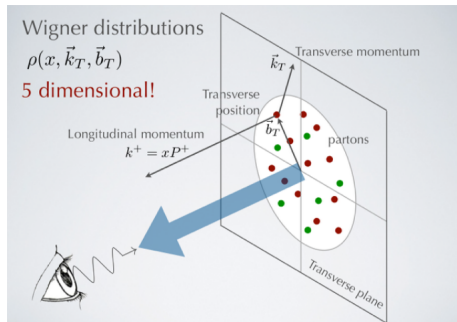
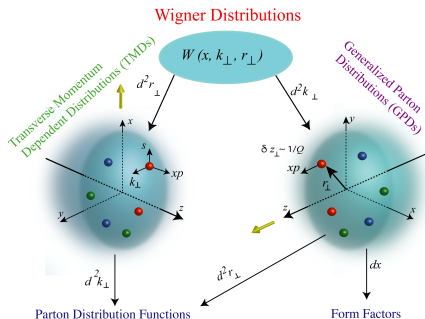
see e.g. M. Constantinou *et al.*, arXiv:2006.08636  
Jin-Lin Zhang *et al.*, arXiv:2009.11384  
A. Freese *et al.*, Phys.Rev.C 101 (2020) 3, 035203

- Exclusive charmonium production
- Transition GPDs
- ...

# A glimpse at the nucleon 5D structure?

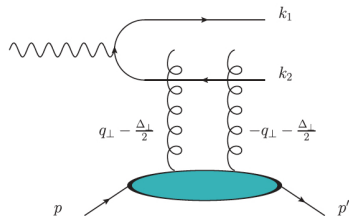






- Not probability density
  - Encode more information than TMDs and GPDs (correlations between  $b_{\perp}$  and  $k_{\perp}$ )
- important for Orbital Angular Momentum

X. Ji, PRL 91(2003)-62001  
 C. Lorcé and B. Pasquini, PRD84(2011)014015  
 C. Lorcé *et al.*, PRD85 (2012) 114006  
 Hatta, PLB708 (2012) 186

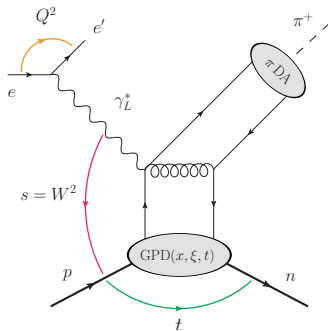


- $\Delta_{\perp} \sim -(k_{\perp,1} + k_{\perp,2})$
- $k_{\perp} \sim P_{\perp} = -\frac{k_{\perp,1} - k_{\perp,2}}{2}$
- $|P_{\perp}| \gg |k_{\perp,1} + k_{\perp,2}|$

Hatta, Xiao, Huan, PRL 116, 2016, 202301

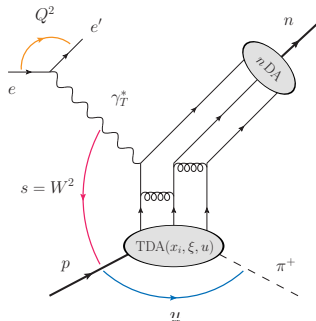
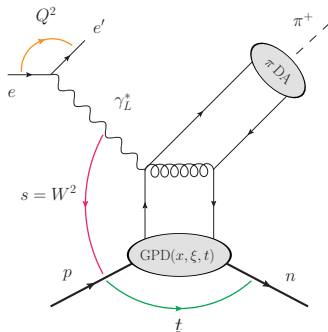
- **Not** standard exclusive process
- Reconstruction of full dijet kinematics and measure the azimuthal modulations in the angle between  $P_{\perp}$  and  $\Delta_{\perp}$
- At small  $x$ : sensitivity to gluon GTMDs
- With proton polarization one may access  $F_{1,4}^g$

# New perspective on hadron structure through backward exclusive processes



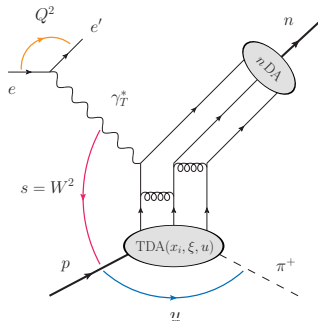
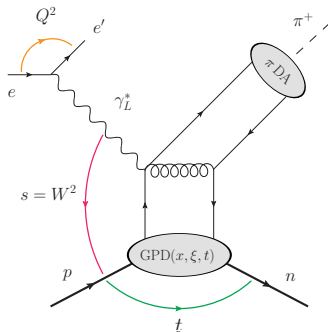
figures from K. Park *et al.*, PLB 780 (2018) 340-345

- $|t|$  small  $\rightarrow$  pion produced in the forward direction w.r.t to the photon ( $\gamma^*$   $p$  center of mass frame)



figures from K. Park et al., PLB 780 (2018) 340-345

- $|t|$  small  $\rightarrow$  pion produced in the forward direction w.r.t to the photon ( $\gamma^* p$  center of mass frame)
- $|u|$  small  $\rightarrow$  pion produced in the backward direction



figures from K. Park *et al.*, PLB 780 (2018) 340-345

- $|t|$  small  $\rightarrow$  pion produced in the forward direction w.r.t to the photon ( $\gamma^* p$  center of mass frame)
- $|u|$  small  $\rightarrow$  pion produced in the backward direction
- New type of physics: explore meson content of the proton with TDA

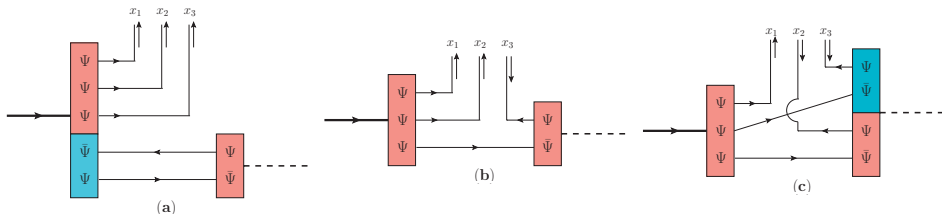
L. Frankfurt *et al.*, PRD 60 (1999) 014010

B. Pire and L. Szymanowski, PRD 71, 111501 (2005)

- They depend on five variables  $(x_1, x_2, \xi, u; \mu)$

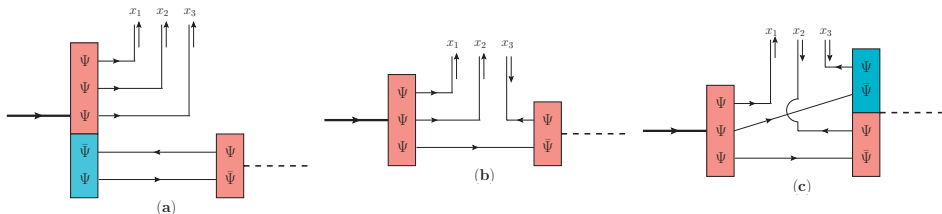


- They depend on five variables ( $x_1, x_2, \xi, u; \mu$ )
- They present interesting interpretations in terms of lightfront wave functions



J.-P. Lansberg *et al.*, PRD 85 (2012) 054021

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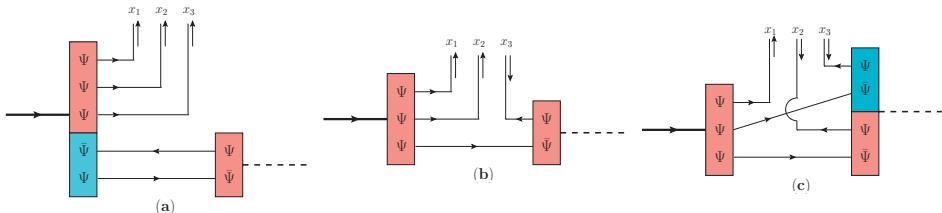


J.-P. Lansberg *et al.*, PRD 85 (2012) 054021

- They obey polynomiality property in  $\xi$  and support properties  
 → spectral representation (DD à la Radyushkin)

B. Pire *et al.*, PRD 82 (2010) 094030

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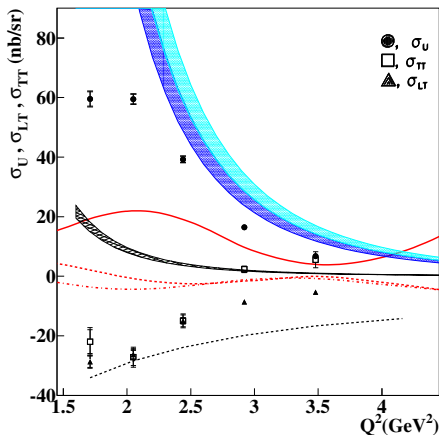
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B. Pire *et al.*, PRD 82 (2010) 094030

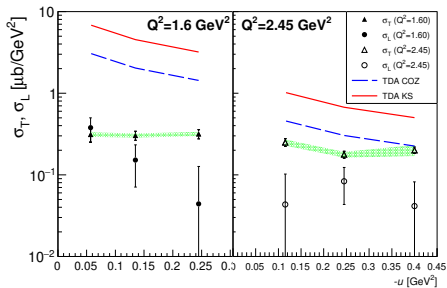
- In the limit  $\xi \rightarrow 1$  they yield the nucleon distribution amplitude (soft pion theorem)

B. Pire *et al.*, PRD84, 074014



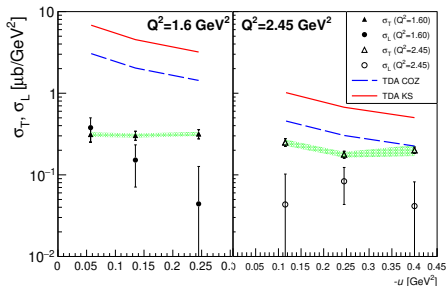
K. Park et al., PLB 780 (2018) 340-345

- nucleon to pion TDA
- $\sigma_T \gg \sigma_L$ 
  - ▶ Complete rosenbluth separation not possible here
  - ▶ Hint:  $\sigma_{TT}$  and  $\sigma_{LT}$  sizeable
- Dependence in  $\sigma_T \sim \frac{1}{Q^8}$ 
  - ▶ Strong dependence in  $Q^2$
  - ▶ More data necessary



W.B. Li *et al.*, PRL 123 (2019) 18, 182501

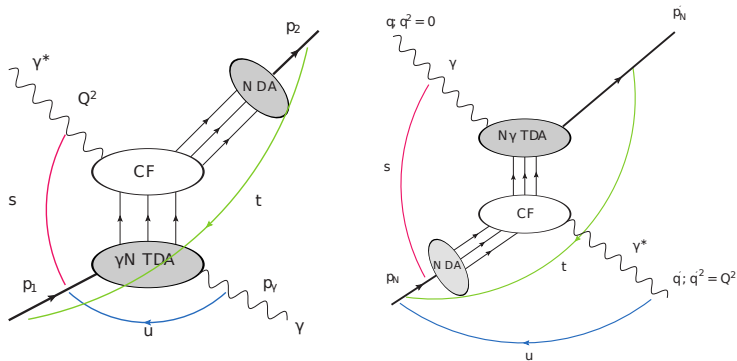
- nucleon to  $\omega$  TDA
- $\sigma_T \gg \sigma_L$ 
  - ▶ Rosenbluth separation performed
  - ▶ For  $Q^2 = 2.45 \text{ GeV}^2$ ,  $\sigma_T$  dominates
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  - ▶ More data necessary



W.B. Li *et al.*, PRL 123 (2019) 18, 182501

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More data required to validate the TDA framework



## Backward Compton Scattering

Spacelike and timelike backward (large  $|t|$ , small  $|u|$ ) Compton scattering possible

→ New kind of information on the nucleon brightness!

## Summary

- Deep exclusive processes are challenging to measure...
- .. but worth the effort !
- Many theory progresses, but not all are taken advantage of yet
- Until now, the lack of data has been a limiting factor

## Perspectives

- Future high-luminosity facilities will improve our knowledge of exclusive processes
- Higher  $Q^2$  measurements are strongly desirable
- There is interesting physics in higher-twist correlation functions



Thank you for your attention