Many-body forces and nucleon clustering near the QCD critical point

- E. Shuryak and J. M. Torres-Rincon, Phys. Rev. C100, 024903 (2019), arXiv:1805.04444 [hep-ph].
- E. Shuryak and J. M. Torres-Rincon, *Phys. Rev.* C101, 034914 (2020),
- arXiv:1910.08119 [nucl-th].
- D. DeMartini and E. Shuryak, (2020), arXiv:2007.04863 [nucl-th].

Many-body forces and nucleon clustering near the QCD critical point D. DeMartini and E. Shuryak, e-Print: 2010.02785

BNL seminar, Nov.10,2020

expansion

- 4. Paradox: attractive binary forces near CP get huge O(N^2)
- 6. universal effective action for Ising universality class
- 7. Deformed universal effective action
- 8.Summing all effects near CP
- - **MAY be located?**

1.Introduction: suggestion of BES, critical event-by-event fluctuations 2.The main idea: preclusters may have size comparable to corr.length **3.Nucleon clustering, importance of 4 N systems, kurtosis and viral**

5. Repulsive manybody forces near CP, estimates in Landau model

9. EXPERIMENTAL OBSERVABLES: Kurtosis and t*p/d^2 plots: where CP





Introduction

- The original ideas:
- Look for event-by-event fluctuations
- Perform beam energy scan
- Watch for non-monotonous signals

Higher moments of the critical field

$$\kappa_2 = \langle \phi^2 \rangle, \ \kappa_3 = \langle \phi^3 \rangle, \ \kappa_4 = \langle \phi^4 \rangle - 3 \langle \phi^2 \rangle^2$$

Are sensitive to higher powers of the correlation length

M. A. Stephanov, K. Rajagopal, and E. V. Shuryak, Phys. Rev. Lett. 81, 4816 (1998), arXiv:hep-ph/9806219 [hep-ph].

M. A. Stephanov, Phys. Rev. Lett. 107, 052301 (2011), arXiv:1104.1627 [hep-ph].



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So far estimates relied on the assumption that nucleons are correlated ONLY due to near-CP fluctuations, which is of course not the case

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The main idea of this work:

Suppose the CP indeed exists, and is located in the part of the phase diagram near the freezeout line of BES program collisions. Furthermore, while scanning this line, for some specific beam energy one happens to be in a state in which the correlation length reaches a value $\xi max \sim 1.5$ -2fm. What observables are sensitive to such scale of ξ ?



Pre-clustering of nucleons create objects of the right scale ! Their energy - and therefore production yield is very sensitive to correlation length

As we will show, the interplay of attractive binary And repulsive manybody forces Will lead to non-monotonous signal





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Side remark: sound waves we observed, but with the wavelength much larger than 2 fm









Studies of few-nucleon pre-clustering at freezeout conditions

Classical molecular dynamics

Semiclassical approximation (fluctons) At finite temperatures

K-harmonics => radial Schreodinger equations in 3*(N-1) dimensions

• E. Shuryak and J. M. Torres-Rincon, Phys. Rev. C100, 024903 (2019), arXiv:1805.04444 [hep-ph].

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Direct Path Integral Monte Carlo (PIMC) Numerical simulations • E. Shuryak and J. M. Torres-Rincon, *Phys. Rev. C101, 034914 (2020)*, • arXiv:1910.08119 [nucl-th].





(the first time ever) testing the flucton method at finite T

Fluctons for anharmonic oscillator at $T \neq 0$

$$S_E = \oint d\tau \left(\frac{\dot{x}^2}{2} + \frac{x^2}{2} + \frac{g}{2}x^4\right)$$

the usual density matrix (line, 60 states)

$$P(x_0) = \sum_{i} |\psi_i(x_0)|^2 e^{-E_i/T}$$

$$P(x_0) \sim exp(-S_E[x_{flucton}(\tau)])$$

(points on the plot) so, the method works very well





FIG. 3: Top panel: Density matrix $P(x_0)$ vs x_0 for anharmonic oscillator with the coupling g = 1, at temperature T = 1, calculated via the definition (1) (line) and the flucton method (points). The line is based on 60 lowest state wave functions found numerically. Bottom panel: Comparison of the logarithmic derivative of the density matrix of the upper panel.

K-harmonics applied to He4 (not a new method, and yet we found something new with it...)

9 Jacobi coordinates for 4 particles

hyperdistance

in 9 dimensional space Is sum of squares of all 6 Distances

redefining the wave function and the radial Schreodinger eqn Note, the first derivative is gone but some new repulsive potential remains (not orbital!)

 $\frac{d^2\chi}{d\rho^2}$

Solving the eigenvalue problem in App. A we have obtained 40 lowest eigenstates for Eq. (A3) using the simplest potential V_1 from Ref. [17] and the Coulomb term between the two protons. The ground state energy we find is $E_0 = -27.8$ MeV, very close to the experimental value of -28.3 MeV.

Rather unexpectedly, we also find a second bound state (missed in [17]) with energy $E_1 = -2.8$ MeV. To determine whether this state is physical, we show in Table ?? the excited states of ⁴He. Among them there is just one 0^+ state, with a binding energy of

B = -28.3 MeV + 20.2 MeV = -8.1 MeV

$$\vec{\xi}[1] = \frac{\vec{x}[1] - \vec{x}[2]}{\sqrt{2}}, \quad \vec{\xi}[2] = \frac{\vec{x}[1] + \vec{x}[2] - 2\vec{x}[3]}{\sqrt{6}}$$
$$\vec{\xi}[3] = \frac{\vec{x}[1] + \vec{x}[2] + \vec{x}[3] - 3\vec{x}[4]}{2\sqrt{3}}$$
$$\rho^2 = \sum_{m=1}^{3} \vec{\xi}[m]^2 = \frac{1}{4} \left(\sum_{i \neq j} (\vec{x}[i] - \vec{x}[j])^2\right)$$

$$\psi(\rho) = \chi(\rho)/\rho^4$$

$$\frac{12}{\rho^2}\chi - \frac{2M}{\hbar^2}(W(\rho) + V_C(\rho) - E)\chi = 0$$



here are experimentally observed excited states of He4 the first one fits well to our second bound state

Now, getting convinced that we understand quantum mechanics of 4 nucleons in He4 At zero T, we proceed to calculate the density matrix at finite T and check how it changes when the nuclear potential changes

So, people doing stat models For light nuclei Were missing about 50 states!

TABLE I: Low-lying resonances of ⁴He system, from BNL properties of nuclides listed in nndc.bnl.gov web page. J^P is total angular momentum and parity, Γ is the width. The last column is the decay channel branching ratios, in percents. p, n, d correspond to emission of proton, neutron or deuterons.

Г				
	E (MeV)	J^P	Γ (MeV)	decay modes, in $\%$
	20.21	$ 0^+ $	0.50	p =100
	21.01	0^{-}	0.84	n = 24, p = 76
	21.84	$ 2^{-} $	2.01	n = 37, p = 63
	23.33	2^{-}	5.01	n = 47, p = 53
	23.64	$ 1^{-} $	6.20	n = 45, p = 55
	24.25	$ 1^{-} $	6.10	n = 47, p = 50, d=3
	25.28	$ 0^{-} $	7.97	n = 48, p = 52
	25.95	$ 1^{-} $	12.66	n = 48, p = 52
	27.42	$ 2^+ $	8.69	n = 3, p = 3, d = 94
	28.31	$ 1^+ $	9.89	n = 47, $p = 48$, $d = 5$
	28.37	$ 1^{-} $	3.92	n = 2, p = 2, d = 96
	28.39	$ 2^{-} $	8.75	n = 0.2, p = 0.2, d = 99.6
	28.64	0^{-}	4.89	d=100
	28.67	$ 2^+ $	3.78	d=100
	29.89	2^+	9.72	n = 0.4, $p = 0.4$, $d = 99.2$

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ls to last p, n

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Now they are being included: About half of d,t,he3 Come from them!

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I did PIMC simulation of He4 in 1980 already, and managed to put it to NPB

0.0010

0.4

0.3

0.2

0.1

0.3

0.2

Path integral simulations of the few-nucleon clustering at heavy ion collisions freezeot,

(with Dallas DeMartini, SB student)

hyperdistance definition



4 particles, 6 distances

Paths of 4 nucleons in a Matsubara time In a periodic box Only tau discretized But very many steps needed

> The density and temperature values correspond to kinetic Freezeout conditions at BES 1 energies

0.0010



FIG. 6: Ground state and precluster for 19.6 GeV.



Calculation with Conventional nuclear forces

$$Z_{pot} = 1 + \frac{1}{V^N} \int d^3 x_1 \dots \int d^3 x_N \left[e^{\left(-\sum_{i>j} V(\vec{x}_i - \vec{x}_j)/T \right)} \right]$$

$$Z_{pot} = 1 + \frac{N(N-1)(N-2)(N-3)}{4!} \left(\frac{V_{cor}}{V^3} \right) \approx 1 + n^3 V_{cor}^{(9)}$$

$$V_{cor}^{(9)} = \frac{32}{105} \pi^4 \int d\rho \rho^8 \left(P(\rho) - 1 \right).$$

$$V_{cor}^{(9)}(7.7) \approx 4.3 \cdot 10^4 \ fm^9 \ \text{From PIMC}$$

$$n_{cl} \equiv \frac{4}{\left(V_{cor}^{(9)} \right)^{1/3}} \approx 0.114 \ /fm^3$$

about 3 times the density of ambient matter $n_{I}(7.7) \approx 0.037/\text{fm}^3$.

$$R_{amb} \equiv n_B^{-1/3} \approx 3.0 \, fm, \quad R_{cl} \equiv n_{cl}^{-1/3} \approx 2.0 \, fm$$

Will be reached first by the correlation length





 $0\,fm$

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Although 4-clusters contain only fraction of a percent of nucleons In kurtosis it is O(1) at the lowest BES energies



 $0\,fm$

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FIG. 10: The 4th cumulant deviation (Eq. (15)) versus \sqrt{s} , using the 9-dimensional correlated volume $V_{cor}^{(9)}$ determined $0\,fm$ from the PIMC simulations.

Calculation with Modified nuclear forces reduced sigma mass Predicted by chiral transition produce huge unrealistic effect

E_B (MeV)

Predicted for Chiral transition by RG

the effect of binary forces induced by the critical mode at CP, where $\xi \rightarrow \infty$ must be catastrophic. Indeed, if all N (N – 1)/2 ~ 104 pairs of nucleons in the fireball be attracted to each other, with a Newton-like long-range potential, the fireball would implode, similar to a gravitational collapse.



FIG. 8: Binding energy E_B of the 4N system as a function of the σ mass m_{σ}





If nucleons are uncorrelated They are easy to calculate. But they are correlated!

$$\frac{g_c^2}{4\pi} \langle \phi(\vec{r})\phi(0) \rangle = -\frac{g_c^2}{4\pi} \frac{\exp(-r/\xi)}{r}$$

We introduce the following objects

$$\begin{split} \vec{x}_{1}, \vec{x}_{2}, \vec{x}_{3} &\equiv \int d^{3}u D(\vec{x}_{1} - \vec{u}) D(\vec{x}_{2} - \vec{u}) D(\vec{x}_{3} - \vec{u}) \\ (\vec{x}_{2}, \vec{x}_{3}, \vec{x}_{4}) &\equiv \int d^{3}u D(\vec{x}_{1} - \vec{u}) D(\vec{x}_{2} - \vec{u}) D(\vec{x}_{3} - \vec{u}) D(\vec{x}_{3} - \vec{u}) \\ (\vec{x}_{2}, \vec{x}_{3}, \vec{x}_{4}) &\equiv \int d^{3}u d^{3}v D(\vec{x}_{1} - \vec{u}) D(\vec{x}_{2} - \vec{u}) D(\vec{u} - \vec{v}) D(\vec{x}_{3} - \vec{v}) D(\vec{x}_{4} - \vec{u}) \\ D(r) &= exp(-r/\xi)/r \end{split}$$

the factor $1/4\pi$ present in 3d propagator will be included later with the couplings.

These functions depend on 3 or 4 points should be averaged over manybody density matrix of the clusters.





How diagrams depend on the cluster shape and the correlation length?



FIG. 3. text.

At small correlation length very strong dependence on xi But it is moderate at xi/rho>1

(Color online) Interactions V_b (left), V_c (center), and V_d (right) corresponding to diagrams (b,c,d) of Fig. 2, respectively, as a function of the correlation-length-to-hyperdistance ratio ξ/ρ for both the tetrahedral and square configurations. The curve is an interpolation of the tetrahedral data points. The distinction between the 'same' and 'opposite' square configurations for diagram (d) is explained in the

Rather weak dependence on shape if rho is the same



Averaging diagrams over snapshots from PIMC simulation



FIG. 6. Distribution of values of the multibody interactions V_b (left), V_c (center), and V_d (right) corresponding to diagrams (b,c,d) of Fig. 2, respectively, in 5000 configurations each for the cluster ($\rho < 3$ fm) and ambient nucleon matter ($\rho > 3$ fm) generated in PIMC simulation. Calculation performed with $\xi = 2$ fm.

Diagrams are significantly larger for clusters

Tails to the right are due to very small clusters: but those will be killed

Preliminary estimate: Landau phi⁴ model

$$V_{tet} = -6\frac{g_c^2}{4\pi} \langle V_a \rangle_{tet} + 4!\lambda_4 (\frac{g_c}{4\pi})^4 \langle V_c \rangle_{te}$$
$$\frac{g_{\sigma}^2}{4\pi} = 6.04, \quad \frac{g_{\omega}^2}{4\pi} = 15.17.$$

Walecka model of **Relativistic mean field For nuclear matter**

Critical mode is their mixture Stephanov used 10 as some round average And so do we

But we do not know The value of The quartic coupling



FIG. 4. Energy of four-nucleon tetrahedral cluster (in GeV) as a function of correlation length ξ (fm) The critical mode-nucleon coupling is taken to be equal to nucleon-sigma meson coupling of the Waleck model (20), and the values of quartic coupling $\lambda_4 = 1.5$ (upper curve) and $\lambda_4 = 1$ (lower curve).



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THE UNIVERSAL EFFECTIVE ACTION FOR ISING-TYPE CRITICAL **FLUCTUATIONS**

The Landau model, used as an initial approximation, does *not* however represent correct behavior near Ising-like critical points. Wilson's epsilon expansion – in $\epsilon = 4 - d$ where d is space dimension– has found that under the renormalization group flow the Landau model goes into the fixed-point regime in infrared, with small coupling at small ϵ . While Wilson famously calculated approximate values of the critical indices, one might still doubt whether ϵ -expansion gives an accurate account at $\epsilon = 1, d = 3$.

Three arguments suggesting that at the critical point $\Omega \sim \Phi 6$.

$$\frac{d\Omega}{d\phi} = J. \qquad \langle \phi \rangle(J) \sim J^{1/\delta}, \ \delta = \frac{d+2-\eta}{d-2+\eta} \in$$

2. including a φ6 term – but not higher powers – can be justified because this term is the renormalizable one, in d = 3 case

 ≈ 4.78 Much closer to 5 than to 3

3. there are numerical studies showing this ansatz for Ω gives good fits of lattice data.



Probing effective action at large phi is done by doing simulations with different J At critical line parameterized by t=T/Tc-1

$$\Omega(\phi) = \int d^3x \left[\frac{(\phi_{,\mu})^2}{2} + \frac{m^2\phi^2}{2} + mg_4\phi^4 + g_6\phi^6\right]$$

Note that at $m \to 0, \xi \to \infty$ it indeed has only the last ϕ^6 term.



at CP, $\xi = \infty$, t = 0, only the last term survives. Only one dimensional parameter M Which we take to be sigma mass

 $Z = \int D\phi e^{-(\Omega(\phi) + J(x)\phi(x))V_3/T}$ g4=0.97, g6-2.05 from fit M. M. Tsypin, (1994), arXiv:hep-lat/9401034 [hep-lat]. Agrees also with RG calculation by Heidelberg group

P=exp(-VM^3 Omega)







DEFORMED EFFECTIVE POTENTIAL NEAR THE CRITICAL LINE

$$\frac{\partial\Omega}{\partial\tilde{\phi}}(\tilde{\phi}_0) = J$$

As example we use dimensionless J =1/100 Then solve the 5-th order eqn for maximum Then re-center the distribution by

$$\tilde{\phi}_0(t=0.01) \approx 0.224, \ \tilde{\phi}_0(t=0.41) \approx 0.224$$

And get new action in terms of delta Which has all powers of it except the first

$$\tilde{\phi} = \tilde{\phi}_0 + \delta$$

 $\Omega_{def}(t=0.01) \approx -0.0017 + 0.095\delta^2 + 0.51\delta^3 + 1.60\delta^4 + 2.75\delta^5 + 2.05\delta^6$

No linear term, small quadratic one => \xi not infinite even at t=0

Six curves, top to bottom, correspond to values of t = 0.01, 0.09, 0.19, 0.29, 0.39, 0.49, 0.59.



DEFORMED EFFECTIVE POTENTIAL NEAR THE CRITICAL LINE

Triple and Quartic couplings Strongly grow Near CP, t->0

m=1/xi does not vanish Near CP but remains small



Taking all effects together









Plotting exp(-V/T) One gets dramatic non-monotonous signal for cluster formation

Perhaps the nucleon coupling to critical mode Is not that large as assumed **But qualitative shape** is now clear

One needs to look for a dip In clustering

Older STAR data have shown large effect



Two dips for central bins large at 2 and smaller at 20 GeV? Errors still large => BESII • e-Print: 2001.02852

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Let us now look at light nuclei production: the tritium ratio

In this ratio the main driver — fugacity exp(mu/T) -Cancels out

Wenbin Zhao,^{1, 2, 3, 4} Chun Shen,^{5, 6} Che Ming Ko,⁷ Quansheng Liu,^{1, 2} and Huichao Song^{1, 2, 3}

feeding

Summary

- •Multi-body repulsive forces step in and will generate explosion instead
- clusters
- •So, watching the clusters (which are very sensitive) is a better signal than ambient EOS
- •We calculated main diagrams for different shapes and sizes of clusters
- •We used universal Ising fluctuation potential,
- deformed because freeze out is away from critical line
- •The results predict strong dip of clustering near TC
- observables, kurtosis and tritium ratio

•Paradox (ES,2006) at CP is not there even at xi->infinity there is no implosion •Before xi reaches inter-nucleon distances in ambient matter, it does so for

And get temperature dependence of effective triple and quartic couplings

•Experimental data hint for TWO (?) correlated dips in TWO (very different)

Now at fixed t=0.077, xi=2 fm but as a function of cluster size rho

rho=2 very strongly suppressed Does it mean clusters have Size rho=4 fm?

Now at fixed t=0.077, xi=2 fm but as a function of cluster size rho

rho=2 very strongly suppressed Does it mean clusters have Size rho=4 fm?

No, it makes no sense since then density is the same as ambient matter

