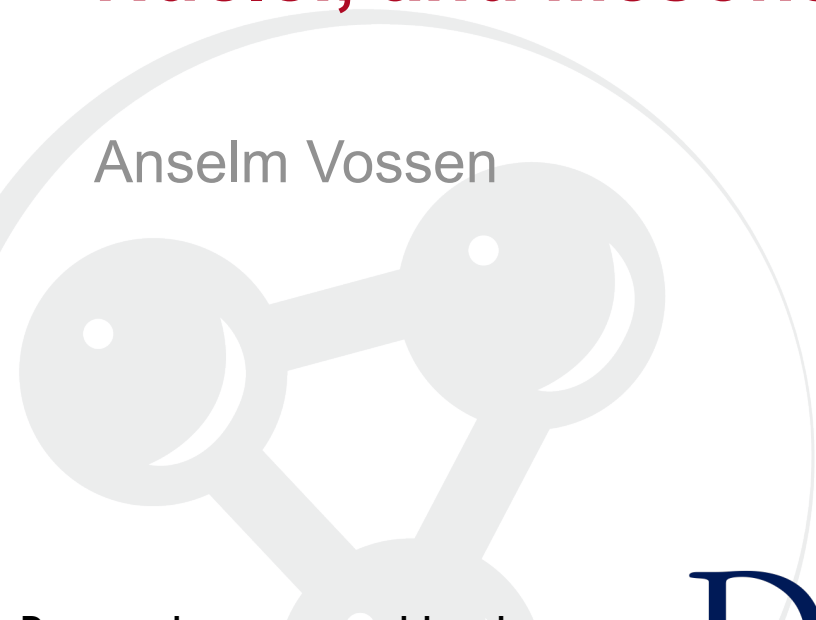


15+5

Multi-dimensional Imaging of Nucleons, Nuclei, and Mesons at the EIC

Anselm Vossen



Research supported by the



U.S. DEPARTMENT OF
ENERGY

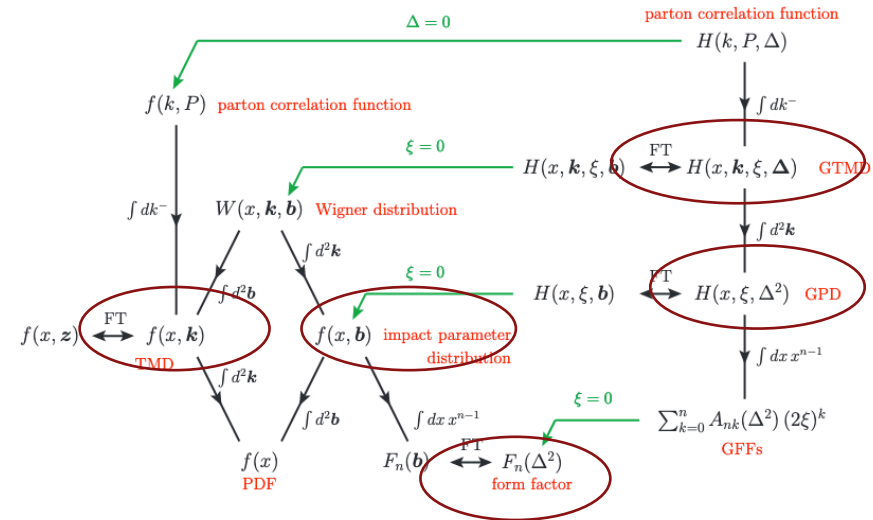
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UNIVERSITY

 **Jefferson Lab**

Overview

- Summarizes an impressive amount of work on
 - Nucleon and Meson Form Factors
 - Generalized Parton Distribution Functions (GPDs) from exclusive processes
 - Transverse Momentum Dependent Distribution Functions (TMDs) from Semi Inclusive Processes
 - Accessing to Wigner functions
 - Using light, polarized nuclei (d , ^3He , ^4He) as neutron targets, investigate nuclear effects and exploit the possibility of tensor polarized targets

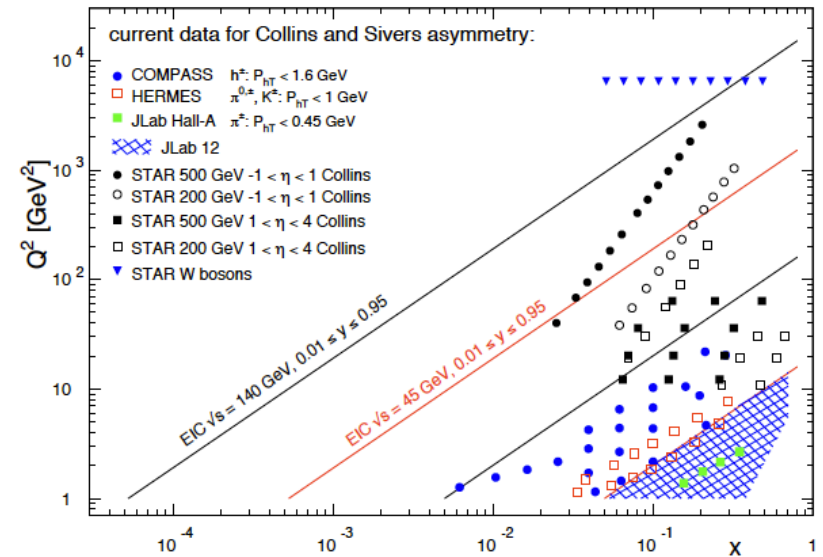
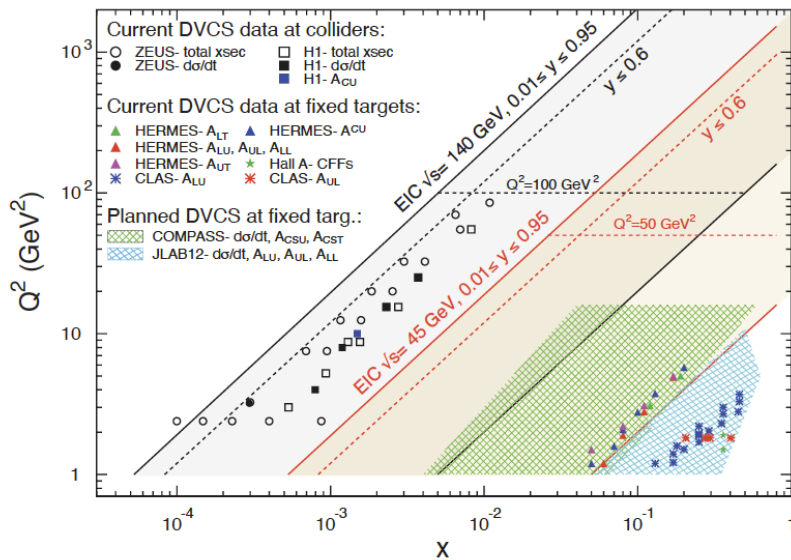


Diehl, 2003

Coverage

- Common theme on EIC impact
 - Extended **kinematic coverage** and **precision**, along with polarization and possible beam charge degrees of freedom allow multi-pronged approach → needed to extract multidimensional objects
 - TMD factorization is valid

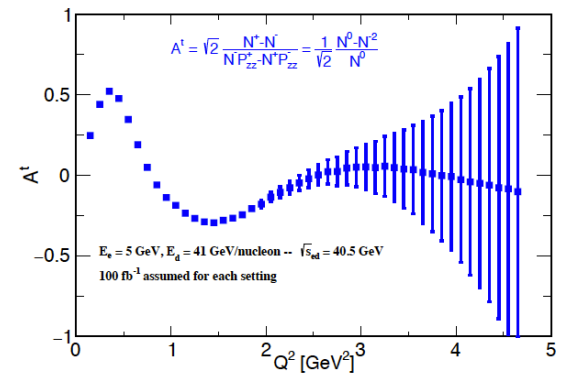
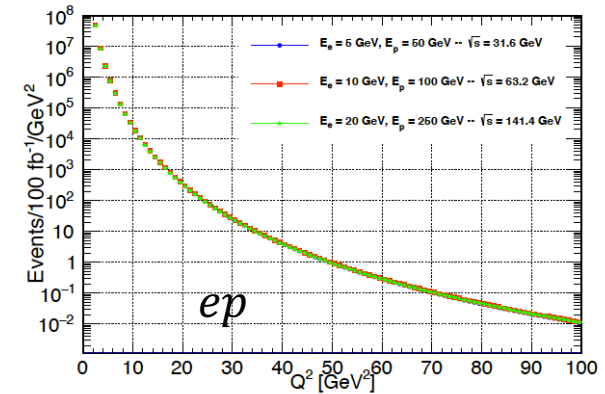
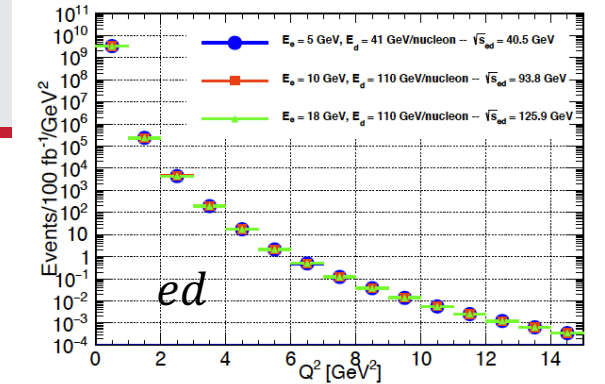
Large Q^2 lever arm: probe evolution, disentangle contributions to σ



Coverage to low x : access sea and gluon distributions

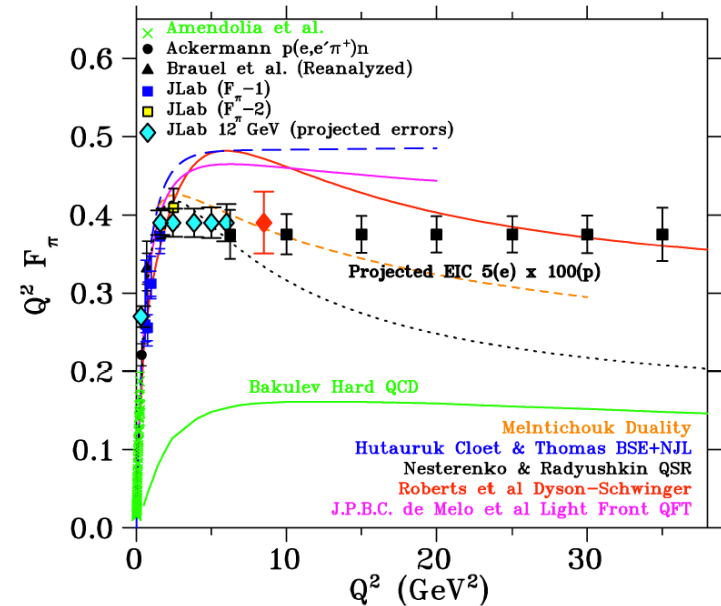
Nucleon

- Magnetic form factors up to the highest Q^2
- Nucleon FF up to $\sim 45 \text{ GeV}^2$
- Deuteron up to $\sim 5 \text{ GeV}^2$
- Tensor polarized up to $\approx 2.5 \text{ GeV}^2$



Meson Form Factors

- Interplay between emergent hadronic mass and Higgs-mass mechanism $\rightarrow \pi$ determined due to QCD, $K \frac{1}{3}$ from Higgs
- From factors $e + p \rightarrow e' + n + \pi$, at low $-t$ scattering off pion cloud (also can get $\frac{\sigma_L}{\sigma_T}$ from π^-/π^+ ratios)
- K form factor from $e + p \rightarrow e' + \Sigma^0/\Lambda + K^+$
 - Still under investigation if scattering from K cloud dominates at same kinematics and how σ_L/σ_T can be verified (probably from Σ^0/Λ)
 - Possibility for first quality F_K measurement at $Q^2 > 0.2$

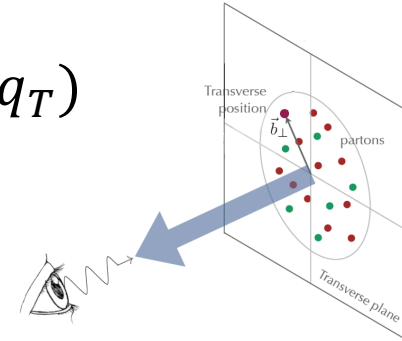


Using $20fb^{-1}, 5 \times 100$

Generalized Parton Distribution Functions

- Four chiral even ($H, E, \tilde{H}, \tilde{E}$), four chiral odd (q_T)
- Depend on x, Q^2, ξ, t
- Can be related to impact parameter

$$q(x, \vec{b}) = \int \frac{d^2 \vec{q}}{4\pi^2} e^{i\vec{b} \cdot \vec{q}} H^q(x, \xi = 0, t = -\vec{q}^2, \mu^2)$$



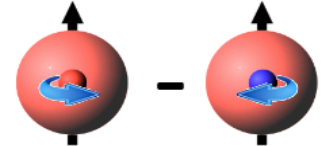
Energy Momentum Tensor Form Factors

- Need complete set of observables including spin and beam-charge asymmetries to meaningfully constrain EMT factors including d –term

$$\mathbf{H}^q(\mathbf{x}, \xi, t) \xrightarrow{t \rightarrow 0} q(\mathbf{x}) \text{ or } f_1(\mathbf{x})$$

“Elusive”

$$\mathbf{E}^q(\mathbf{x}, \xi, t) \leftrightarrow f_{1T}(\mathbf{x}, k_T)$$



Sivers: quark k_T & nucleon transv. spin

$$2J^q = \lim_{t \rightarrow 0} \int \mathbf{x} (\mathbf{H}^q(\mathbf{x}, \xi, t) + \mathbf{E}^q(\mathbf{x}, \xi, t)) d\mathbf{x}$$

$$\int_{-1}^1 dx \, x H^a(x, \xi, t) = A^a(t) + \xi^2 d_1^a(t)$$

mass & energy distribution

$$\int_{-1}^1 dx \, x E^a(x, \xi, t) = 2J^a(t) - A^a(t) - \xi^2 d_1^a(t)$$

Angular momentum distribution Force & Pressure distribution

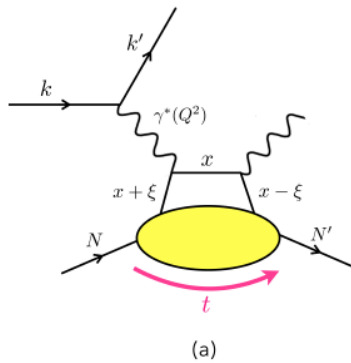
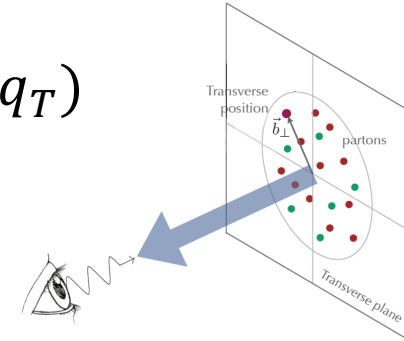
M. Polyakov, P. Schweitzer, Int.J.Mod.Phys. A33 (2018)

Slide from N d'Hose

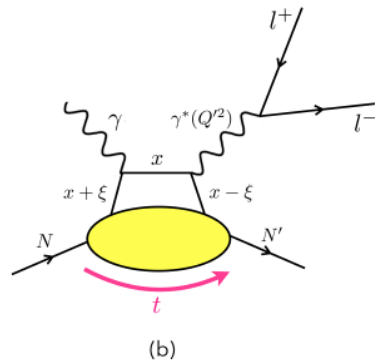
Generalized Parton Distribution Functions

- Four chiral even ($H, E, \tilde{H}, \tilde{E}$), four chiral odd (q_T)
- Depend on x, Q^2, ξ, t
- Can be related to impact parameter

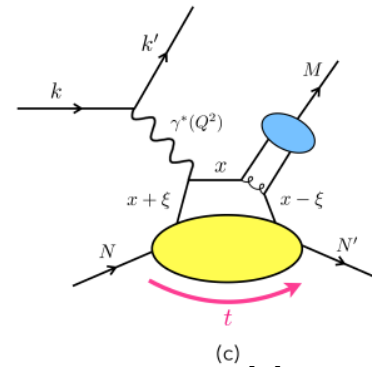
$$q(x, \vec{b}) = \int \frac{d^2 \vec{q}}{4\pi^2} e^{i\vec{b} \cdot \vec{q}} H^q(x, \xi = 0, t = -\vec{q}^2, \mu^2)$$
- Accessed in exclusive processes



(a)
DVCS



(b)
TCS

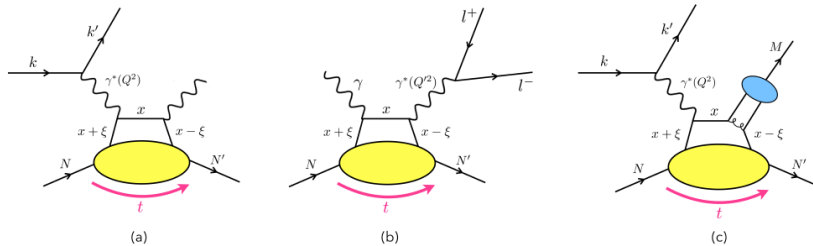
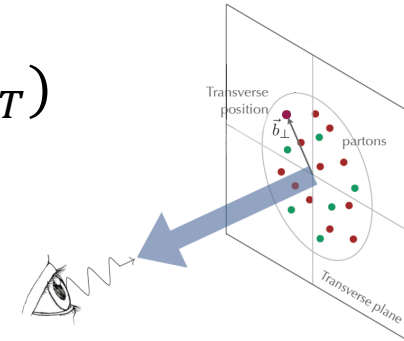


(c)
Meson Production

Generalized Parton Distribution Functions

- Four chiral even ($H, E, \tilde{H}, \tilde{E}$), four chiral odd (q_T)
- Depend on x, Q^2, ξ, t
- Can be related to impact parameter

$$q(x, \vec{b}) = \int \frac{d^2 \vec{q}}{4\pi^2} e^{i\vec{b} \cdot \vec{q}} H^q(x, \xi = 0, t = -\vec{q}^2, \mu^2)$$
- Accessed in exclusive processes

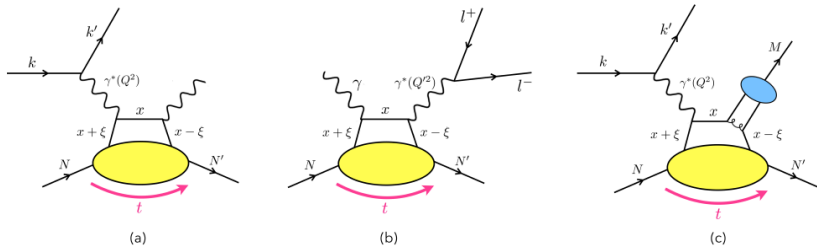
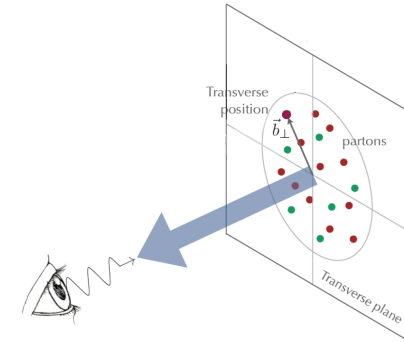


- Meson production channels at the EIC
 - Heavy: access to gluons
 - Vector : similar to DVCS but allows quark flavor separation
 - Light pseudoscalar: access to parity odd and chiral odd GPDs
 → connection to transversity

Generalized Parton Distribution Functions

- Four chiral even ($H, E, \tilde{H}, \tilde{E}$), four chiral odd (q_T)
- Depend on x, Q^2, ξ, t
- Can be related to impact parameter

$$q(x, \vec{b}) = \int \frac{d^2 \vec{q}}{4\pi^2} e^{i\vec{b} \cdot \vec{q}} H^q(x, \xi = 0, t = -\vec{q}^2, \mu^2)$$
- Accessed in exclusive processes



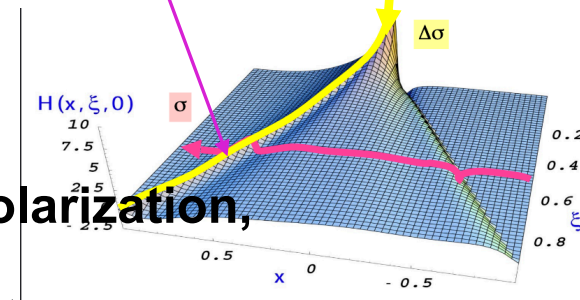
$$T_{\text{DVCS}} \sim \int_{-1}^1 dx \frac{\text{GPD}(x, \xi, t)}{x \pm \xi - i\epsilon} + \mathcal{O}\left(\frac{t}{Q^2}\right)$$

$$\sim \text{PV} \int_{-1}^1 dx \frac{\text{GPD}(x, \xi, t)}{x \pm \xi} \pm i\pi \text{GPD}(\mp \xi, \xi, t) + \mathcal{O}\left(\frac{t}{Q^2}\right)$$

- Measured amplitudes contain complex convolutions of GPDs
- Cross section also contains contributions from competing processes and interferences

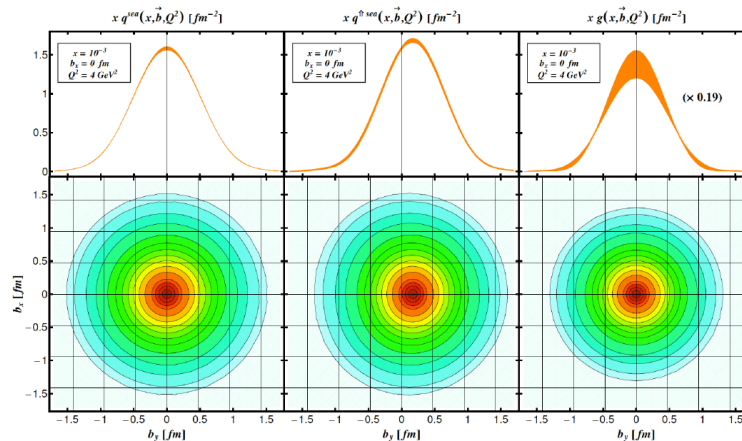
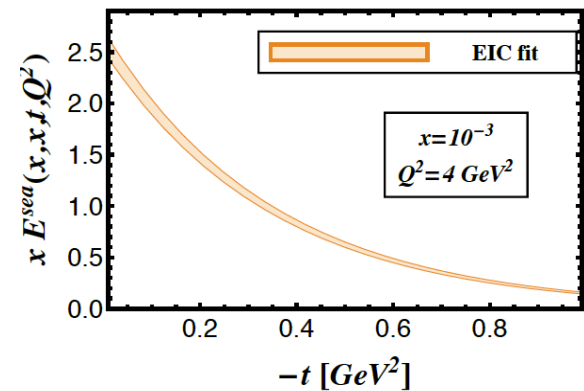
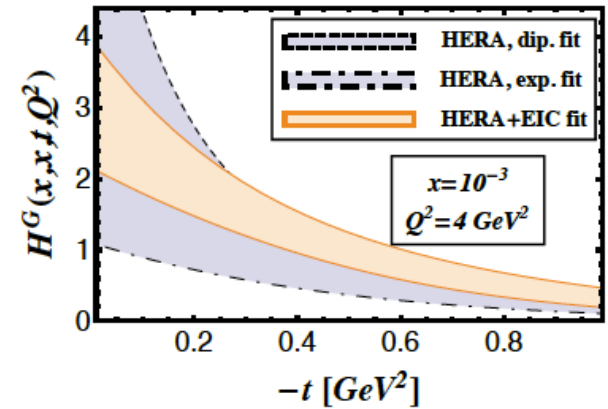
→ Need many degrees of freedom and long kinematic lever arms to disentangle GPDs from measured cross-section

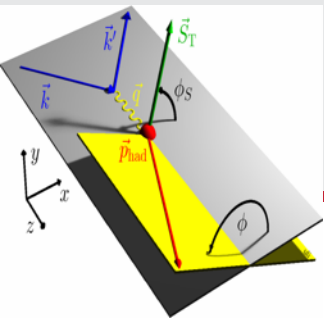
- **Flexibility of EIC ideal with wide coverage in Q^2, t , polarization, possibly beam charge + high precision**
- **Everything can be measured at the same experiment**



EIC kinematic lever arm

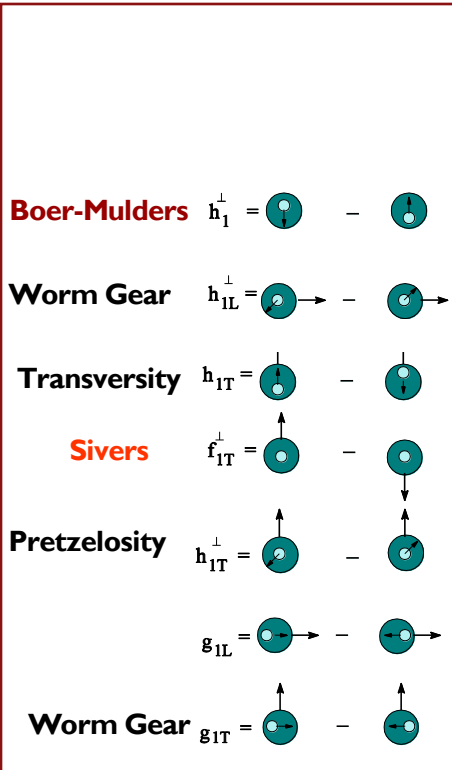
- EIC impact on sea quarks
- Extraction of E needs polarized beams
 → no constraints from Hera data
 → E crucial in ingredient in Ji sum rule
- EIC with good forward acceptance will cover a large lever arm in t → needed for spatial imaging





TMD PDFs from SIDIS

	q	U	L	T
N				
U		f_1		h_1^\perp
L			g_1	h_{1L}^\perp
T		f_{1T}^\perp	g_{1T}	h_1 h_{1T}^\perp



$$d^6\sigma = \frac{4\pi\alpha^2 sx}{Q^4} \times$$

$$\{ [1 + (1-y)^2] \sum e_q^2 f_1^q(x) D_1^q(z, P_{h\perp}^2) + (1-y) \frac{P_{h\perp}^2}{4z^2 M_N M_h} \cos(2\phi_h^\perp) \sum_{q,\bar{q}} e_q^2 h_1^{\perp(1)q}(x) H_1^{\perp q}(z, P_{h\perp}^2) - |S_L| (1-y) \frac{P_{h\perp}^2}{4z^2 M_N M_h} \sin(2\phi_h^\perp) \sum_{q,\bar{q}} e_q^2 h_{1L}^{\perp(1)q}(x) H_1^{\perp q}(z, P_{h\perp}^2) + |S_T| (1-y) \frac{P_{h\perp}}{zM_h} \sin(\phi_h^\perp + \phi_S^\perp) \sum_{q,\bar{q}} e_q^2 h_1^q(x) H_1^{\perp q}(z, P_{h\perp}^2) + |S_T| (1-y + \frac{1}{2}y^2) \frac{P_{h\perp}}{zM_N} \sin(\phi_h^\perp - \phi_S^\perp) \sum_{q,\bar{q}} e_q^2 f_{1T}^{\perp(1)q}(x) D_1^q(z, P_{h\perp}^2) + |S_T| (1-y) \frac{P_{h\perp}^3}{6z^3 M_N^2 M_h} \sin(3\phi_h^\perp - \phi_S^\perp) \sum_{q,\bar{q}} e_q^2 h_{1T}^{\perp(2)q}(x) H_1^{\perp q}(z, P_{h\perp}^2) + \lambda_e |S_L| y (1 - \frac{1}{2}y) \sum_{q,\bar{q}} e_q^2 g_1^q(x) D_1^q(z, P_{h\perp}^2) + \lambda_e |S_T| y (1 - \frac{1}{2}y) \frac{P_{h\perp}}{zM_N} \cos(\phi_h^\perp - \phi_S^\perp) \sum_{q,\bar{q}} e_q^2 g_{1T}^q(x) D_1^q(z, P_{h\perp}^2) \}$$

$$+ (1-y) \frac{P_{h\perp}^2}{4z^2 M_N M_h} \cos(2\phi_h^\perp) \sum_{q,\bar{q}} e_q^2 h_1^{\perp(1)q}(x) H_1^{\perp q}(z, P_{h\perp}^2)$$

$$- |S_L| (1-y) \frac{P_{h\perp}^2}{4z^2 M_N M_h} \sin(2\phi_h^\perp) \sum_{q,\bar{q}} e_q^2 h_{1L}^{\perp(1)q}(x) H_1^{\perp q}(z, P_{h\perp}^2)$$

$$+ |S_T| (1-y) \frac{P_{h\perp}}{zM_h} \sin(\phi_h^\perp + \phi_S^\perp) \sum_{q,\bar{q}} e_q^2 h_1^q(x) H_1^{\perp q}(z, P_{h\perp}^2)$$

$$+ |S_T| (1-y + \frac{1}{2}y^2) \frac{P_{h\perp}}{zM_N} \sin(\phi_h^\perp - \phi_S^\perp) \sum_{q,\bar{q}} e_q^2 f_{1T}^{\perp(1)q}(x) D_1^q(z, P_{h\perp}^2)$$

$$+ |S_T| (1-y) \frac{P_{h\perp}^3}{6z^3 M_N^2 M_h} \sin(3\phi_h^\perp - \phi_S^\perp) \sum_{q,\bar{q}} e_q^2 h_{1T}^{\perp(2)q}(x) H_1^{\perp q}(z, P_{h\perp}^2)$$

$$+ \lambda_e |S_L| y (1 - \frac{1}{2}y) \sum_{q,\bar{q}} e_q^2 g_1^q(x) D_1^q(z, P_{h\perp}^2)$$

$$+ \lambda_e |S_T| y (1 - \frac{1}{2}y) \frac{P_{h\perp}}{zM_N} \cos(\phi_h^\perp - \phi_S^\perp) \sum_{q,\bar{q}} e_q^2 g_{1T}^q(x) D_1^q(z, P_{h\perp}^2)$$

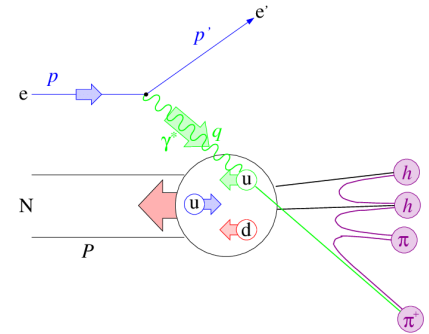
Unpolarized

Polarized target

Polarized beam and target

S_L and S_T : Target Polarizations; λ_e : Beam Polarization
 x : momentum fraction carried by struck quark, z : fractional energy of hadron

Evolution of TMDs



$$F_{UT}^{\sin(\phi-\phi_s)} = \sum_q e_q^2 |C_V(Q)|^2 [R(Q, \mu_0) \otimes f_{1T,q}^\perp(x; \mu_0) \otimes D_{1,q}(z; \mu_0)](p_T),$$

Evolution Kernel

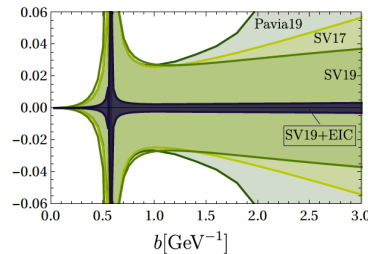
TMD PDF

TMD FF

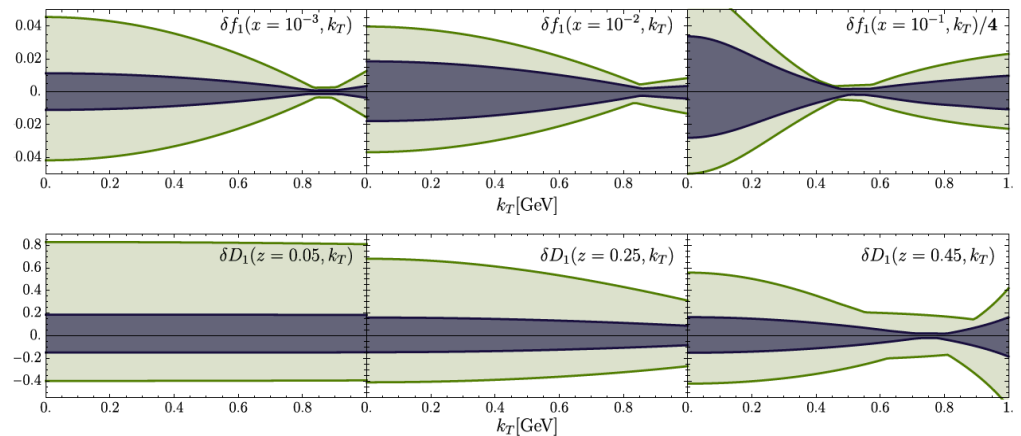
- Need larger lever arm in Q^2, x, k_T to determine evolution kernel, TMDs
- EIC will have large Q^2, x coverage → **pin down evolution kernel, TMDs@low x**
- Large p_T coverage → larger b coverage, where TMDs are unconstrained
- TMD factorization on more solid ground at EIC than at other high precision facilities (small $\frac{p_T}{Q} < \approx 1 \text{ GeV}$)

Impact of EIC on TMD measurements

- Results from SV19 refit with EIC pseudodata ($10 fb^{-1}$), results from Pavia19 consistent
- As expected, biggest reduction in kernel \rightarrow independent of TMD
- TMD PDF and FF uncert reduction mostly at low x , low z



q \ N	U	L	T
U	f_1		h_1^\perp
L		g_1	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

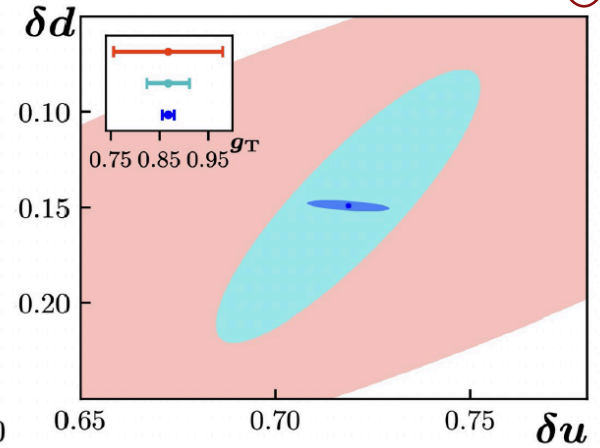
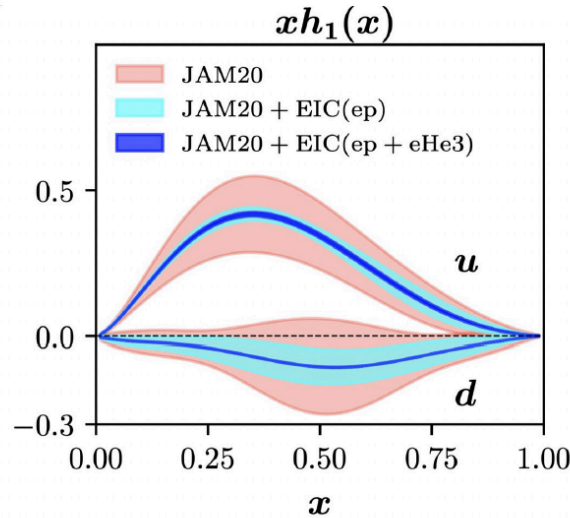


TMD PDF f^u (top) and FF D^{π^+} (bottom)

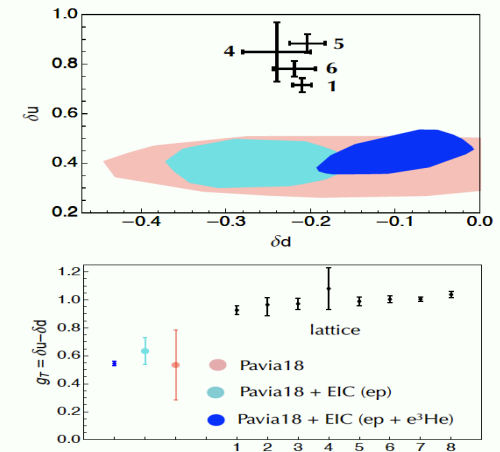
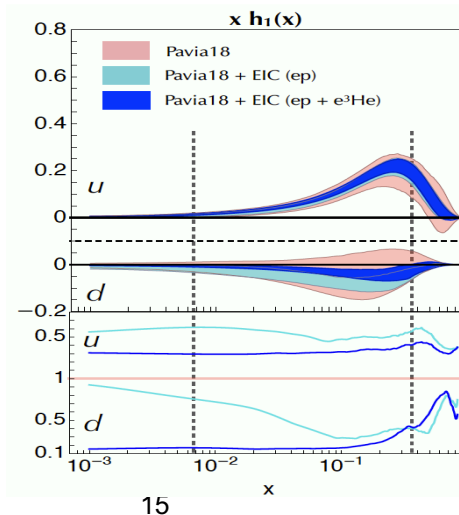
Impact on transversity and Tensor charge

N \ q	U	L	T
U	f_1		h_1^+
L		g_1	h_{1L}^+
T	f_{1T}^+	g_{1T}^+	h_1^+ h_{1T}^+

- Chiral-odd transversity $h(x)$ can be accessed single and di-hadron measurements (complementary)



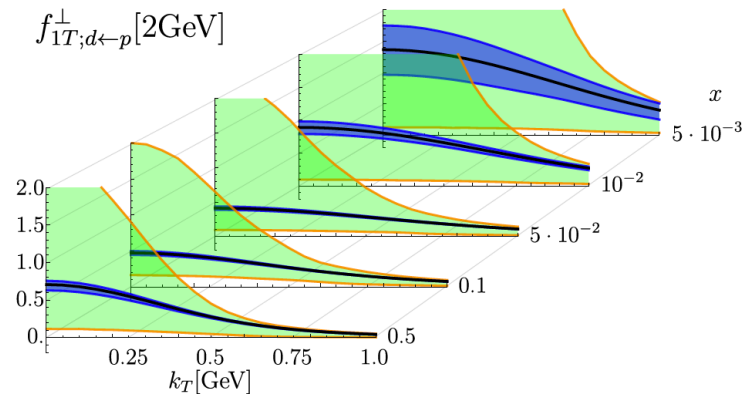
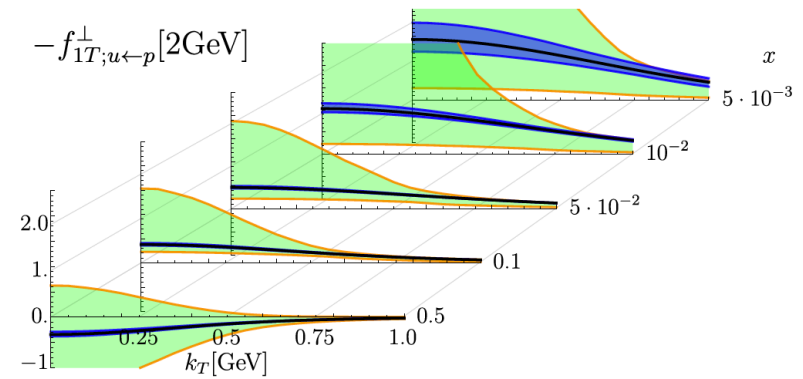
- $\int h(x) dx \propto g_T$ (tensor charge) \rightarrow can be compared to lattice, needed to estimate coupling to certain new physics interactions



Constraints on T-odd Sivers

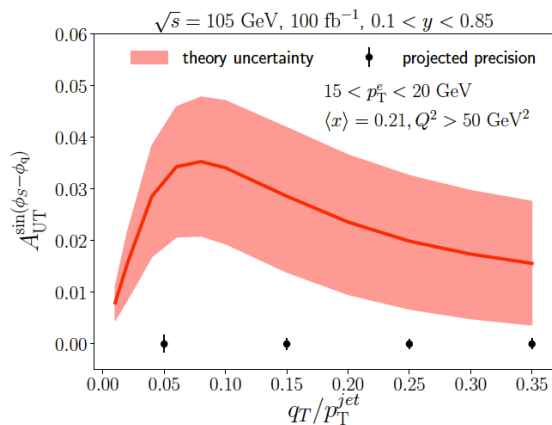
N \ q	U	L	T
U	f_1^\perp		h_1^\perp
L		g_1	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1^\perp, h_{1T}^\perp

- Sivers function is one of the “original” TMDs
- T-odd, vanishes if there is no OAM
- Modified universality
- Can be precisely determined in single spin asymmetries
- Impact of EIC data will be enormous
- Impact on f_d^\perp from He^3 data in particular noteworthy

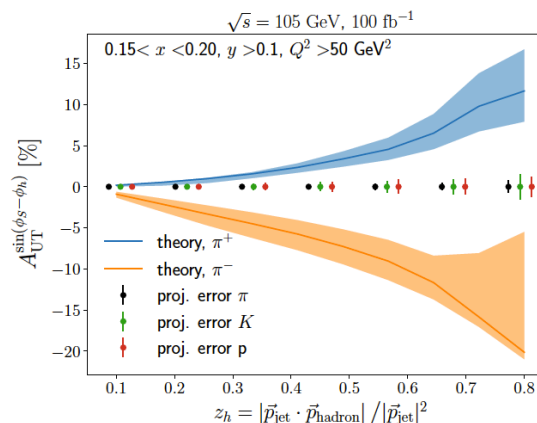


Accessing TMD PDFs and FFs with Jets

- Jets can be used as proxy for outgoing parton
 - Decouple PDF and Fragmentation function (FF)
 - breaks convolution of transverse momenta
- Enables to
 - measure TMD w/o FF contribution
 - FF w/o TMD contribution



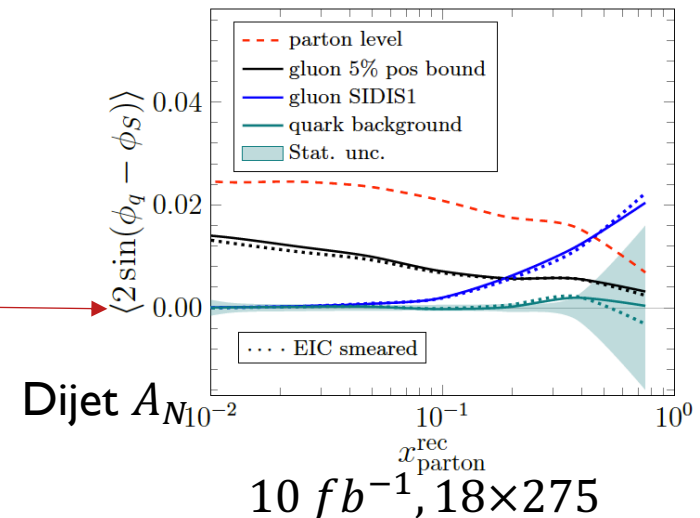
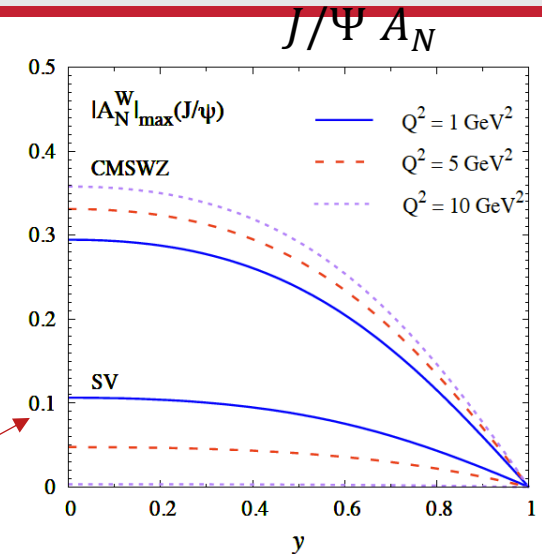
Sivers asymmetry



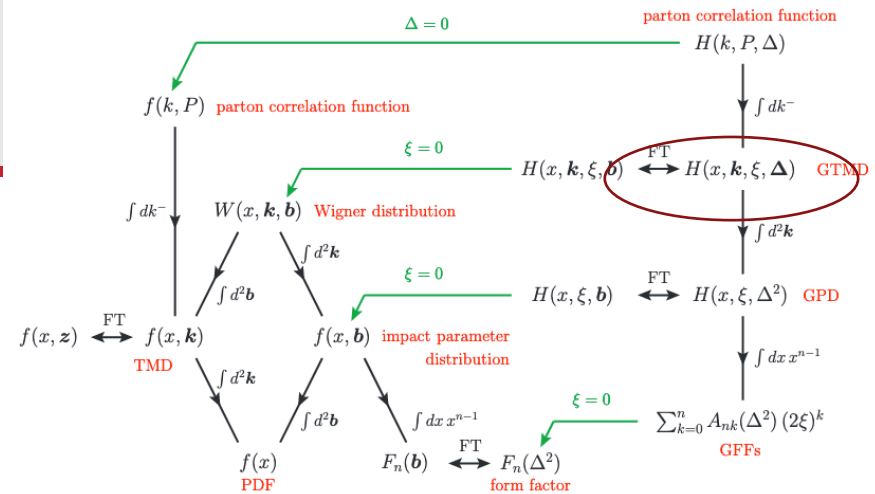
Collins asymmetry

Access to Gluon TMDs with dijets

- Gluon TMDs structure more involved than quark sector
 - 8 TMDs, two types: Weizsacker-Williams (WW) and dipole
 - SIDIS unique for WW type
 - Very little known about unpolarized and polarized gluon TMDs
 - Heavy quarkonium ideal channel, but relation of asymmetries to gluon TMDs model dependent
 - Open heavy quark (e.g. D meson pairs) also good, but large uncertainties
 - dijet/dihedron most promising
- Example: Gluon Sivers via dijet asymmetries



Wigner/GTMDs



- GTMDs \neq TMDs +GPDs \rightarrow encode additional correlations between k_T and b_T
- Can e.g. extract orbital angular momentum in intuitive way

$$L_{q,g}^z = \int dx \int d^2\mathbf{k}_\perp d^2\mathbf{b}_\perp (\mathbf{b}_\perp \times \mathbf{k}_\perp)^z W_{LU}^{q,g}(x, \mathbf{k}_\perp, \mathbf{b}_\perp, \mathcal{W}).$$

Gluon GTMD at small x from diffractive dijets \rightarrow two momentum vectors, sum and difference of jet momenta: Measure azimuthal modulations between both \rightarrow related to b_\perp, k_\perp correlation

- Asymmetries of \approx a few percent expected
- More processes? (also to access quark GTMD, currently only in πN scattering)

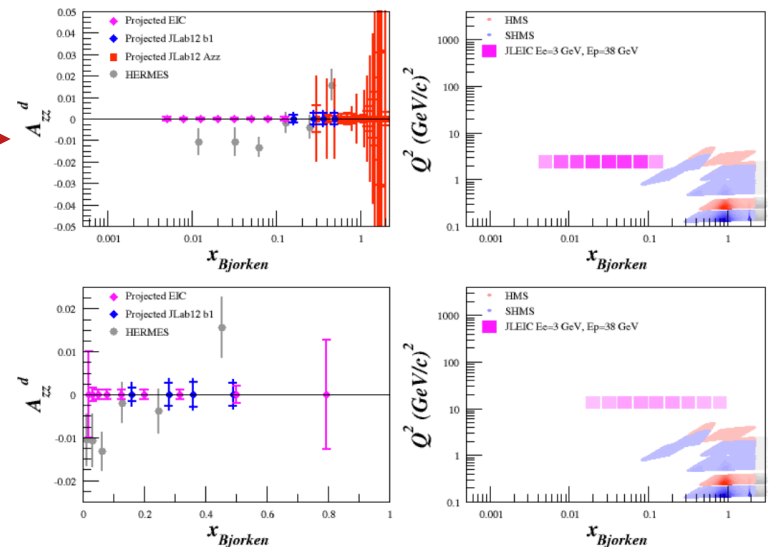
Light Nuclei

Coherent DVCS

- Possible due to EIC ability to detect recoiling nucleon (much easier in collider)
- Nuclear tomography, e.g. EMC effect
- EMT of nucleus, e.g. “d term” → pressure & forces inside the nucleon
- Deuteron, 3He, 4He complimentary in binding energies and spin complexity. (D: spin 1: more complex structure 3He spin 1/2: same as proton, structure the same 4He, spin 0 Simpler)

Tensor polarized deuteron

- 4 additional structure functions b_{1-4}
- b_1 has partonic interpretation and is explicitly dependent on surrounding nucleon
- In quasi elastic regime sensitive to S/D components of deuteron wavefunction
- Asymmetries significant with spectator tagging



Medium Modification of Azimuthal Asymmetries

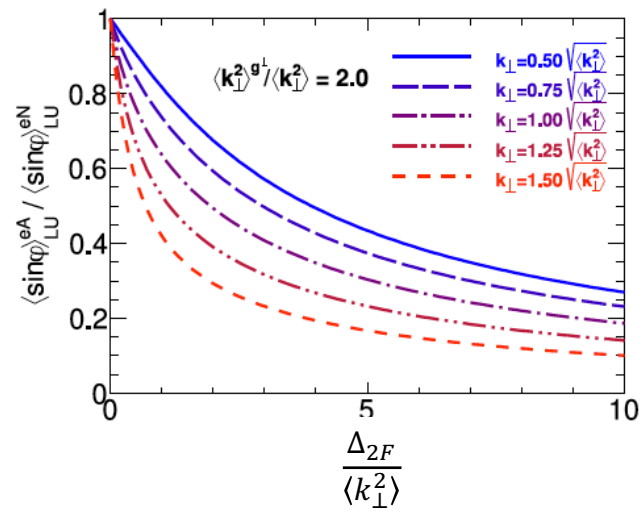
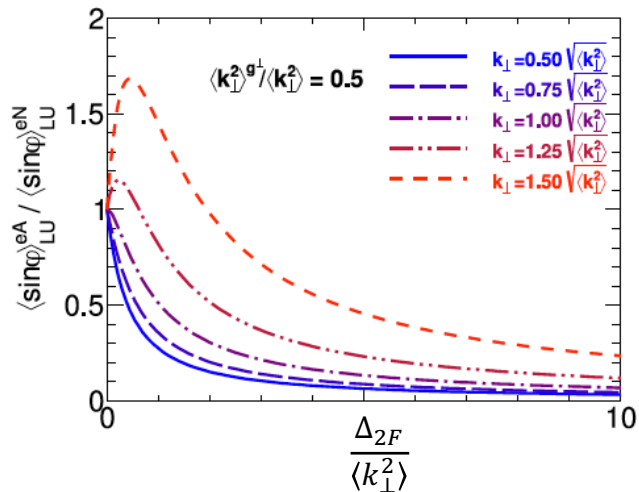
- In gaussian approximation

$$f_1^A(x, k_\perp) \approx \frac{A}{\pi\alpha} f_1^N(x) e^{-\frac{\vec{k}_\perp^2}{\alpha}}, \text{ with } \alpha = \langle k_\perp^2 \rangle + \Delta_{2F}$$

Quark transport parameter Δ_{2F} related to gluon density (due to interaction with gluons)

- Jets are sensitive to TMD PDF k_T only

$$\frac{\langle \sin \phi \rangle_{LU}^{eA}}{\langle \sin \phi \rangle_{LU}^{eN}} \approx \frac{\langle k_\perp^2 \rangle_A}{\langle k_\perp^2 \rangle} \left(\frac{\langle k_\perp^2 \rangle^{g^\perp}}{\langle k_\perp^2 \rangle_A^{g^\perp}} \right)^2 \exp \left[\left(\frac{1}{\langle k_\perp^2 \rangle_A} - \frac{1}{\langle k_\perp^2 \rangle} - \frac{1}{\langle k_\perp^2 \rangle_A^{g^\perp}} + \frac{1}{\langle k_\perp^2 \rangle^{g^\perp}} \right) \vec{k}_\perp^2 \right].$$



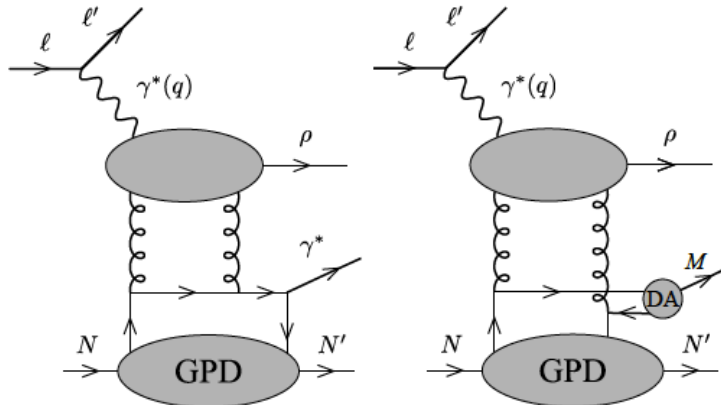
Summary

- Thank you all for your contributions!

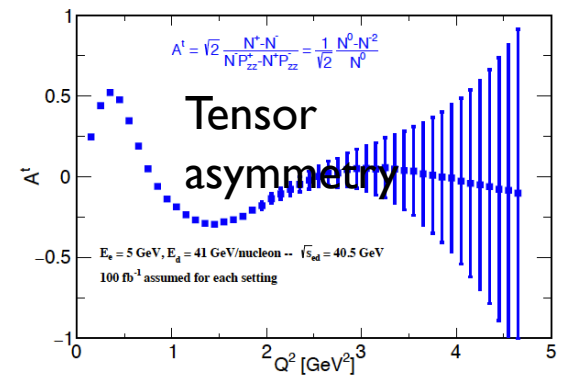
Backup

Diffractive DVCS and photoproduction of $\gamma\gamma$ / $\gamma\rho$

- New processes to be explored
- Diffractive DVCS and meson production
 - Diffractive processes make up large part of the x-section
 - Covers different regime in ξ , decorrelates from x
- Photoproduction of $\gamma\gamma$ and $\gamma\rho$ probe different kinematics in ξ
- Chiral odd GPDs can be accessed using decay distribution of ρ
 - Connection to transversity



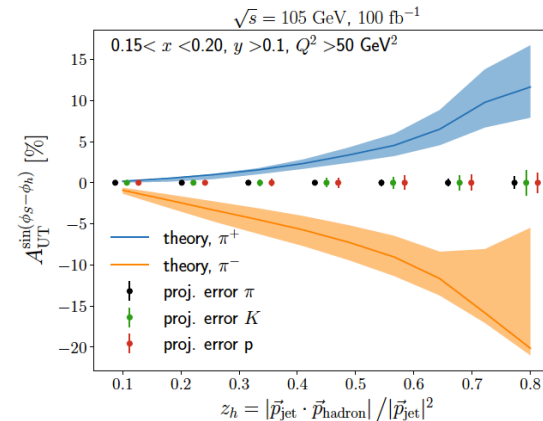
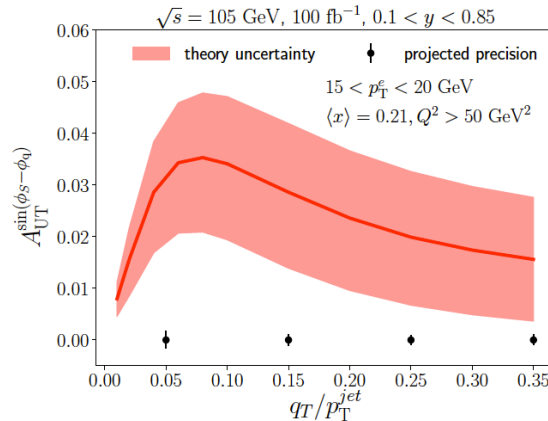
Tensor polarized up to $\approx 2.5 \text{ GeV}$



Di-hadron and jets

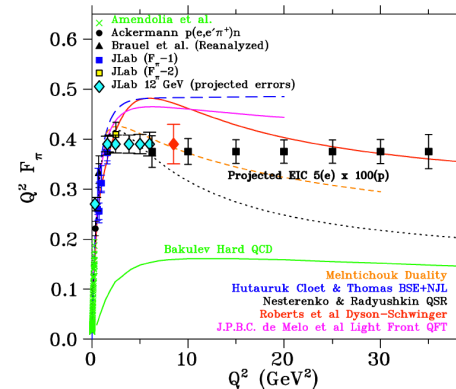
Quark transport parameter Δ_{2F} related to gluon density (interaction with gluons)

$$d^2\ell_{\perp} e^{-(\vec{k}_{\perp} - \vec{\ell}_{\perp})^2 / \Delta_{2F}} f_q^N(x, \ell_{\perp}),$$



Meson form factors

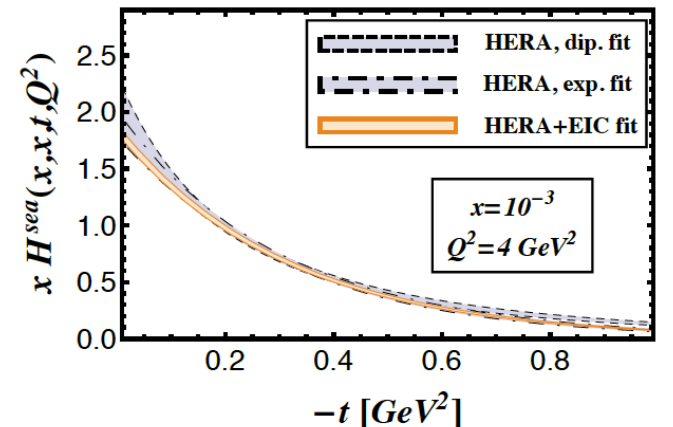
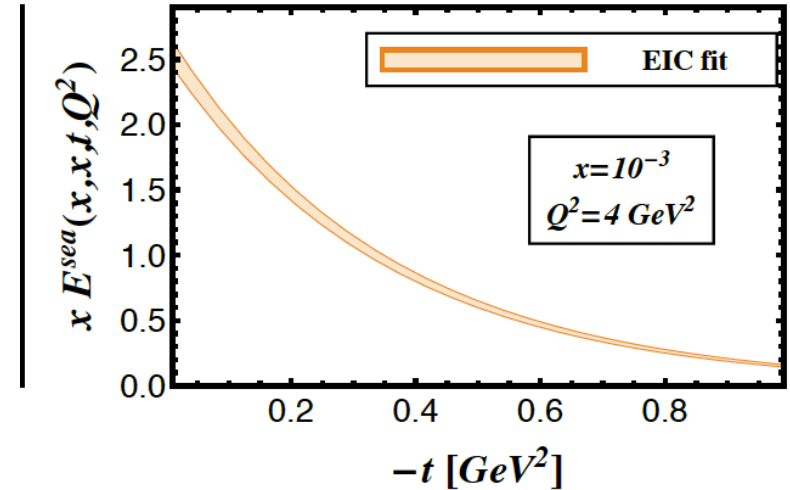
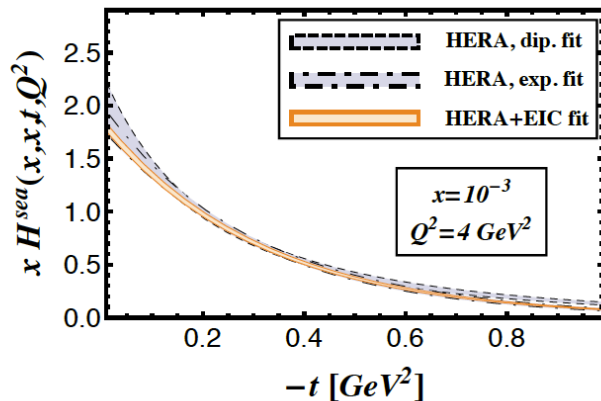
- Elucidating in vis a vis mass generation (see also discussion about mass generation in 7.1) (kaon 1/3 higgs, pion almost 100% QCD)
- (how is F extracted again?)
- Kaon cloud unclear, to be verified by Jlab
 → σ_0/λ ratio to g_e
 σ_L/σ_T

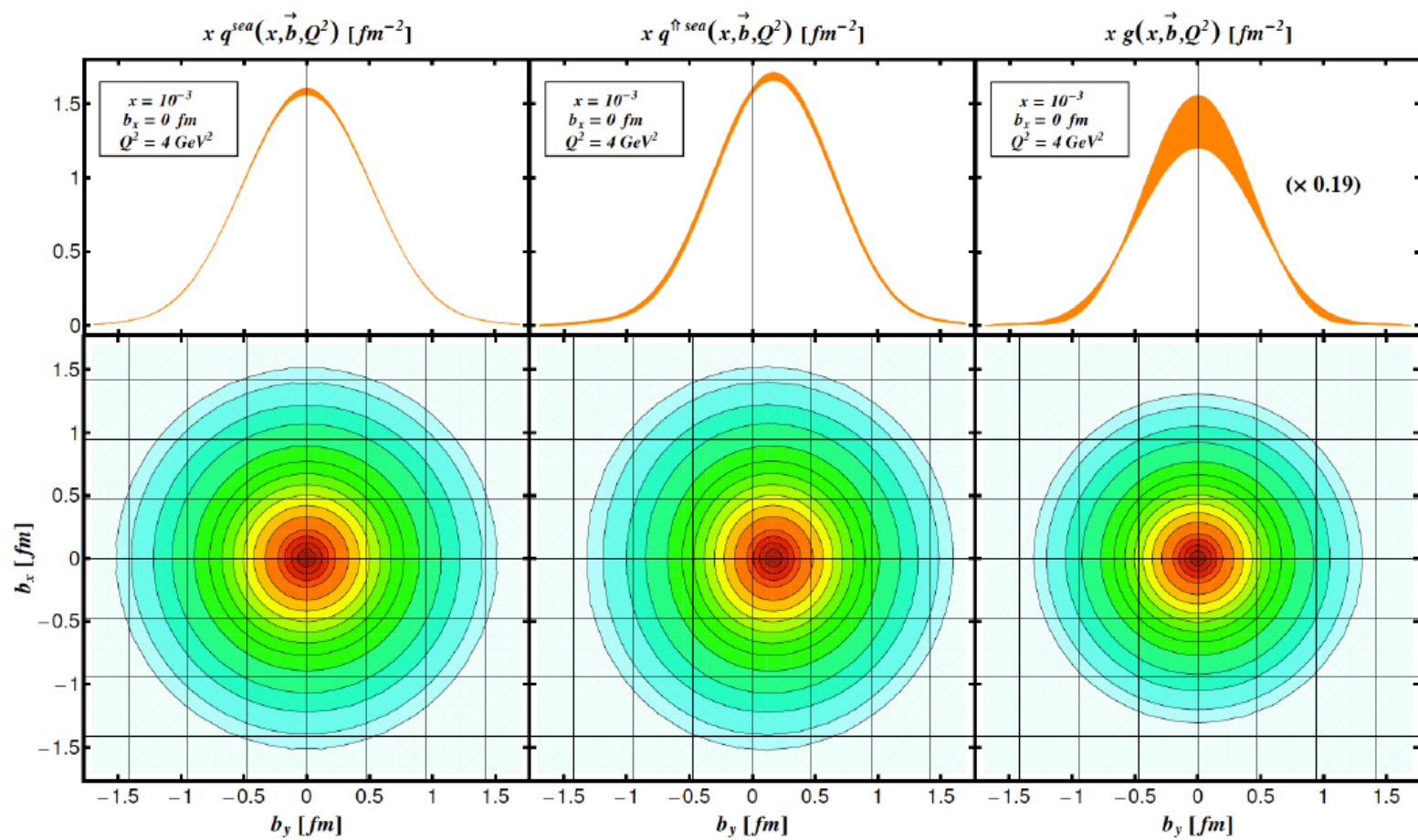


-
- f

GPD

- GPDs are related to CFF which in general contain convolutions
- Impact picture is FT of t dependence
- \rightarrow large kinematic coverage essential





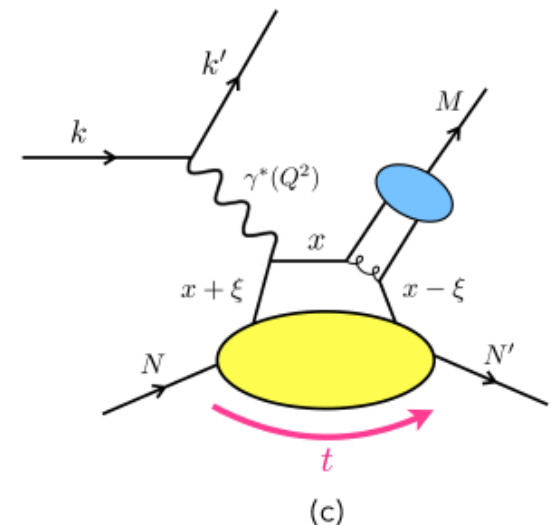
TMD

$$F_{UT}^{\sin(\phi-\phi_s)} = \sum_q e_q^2 |C_V(Q)|^2 \int \frac{d^2b}{(2\pi)^2} e^{i(bp_T)/z} R(Q, b, \mu_0) f_{1T,q}^\perp(x, b; \mu_0) D_{1,q}(z, b; \mu_0)$$

-
- EMT \rightarrow D term (with positron beam)

GPD measurements in meson production

- Heavy: access to gluons
- Vector : similar to DVCS but allows quark flavor separation
- Light pseudoscalar: access to parity odd and chiral odd GPDs, connection to transversity



- "Golden channels" ... ::?
- TMDs,
 - Precision in x, k_T
 - Evolution (\leftarrow strong suite of the EIC)
- Collins/Sivers \rightarrow Tensor charge
- Gluon TMDs \rightarrow di-hadrons, jets, heavy quarks
- Di-hadron
- Jets
- Wigner

Light nuclei

- Coherent DVCS by detecting recoiling nucleon
- Deuterium \rightarrow tensor polarization
- Medium Modification azimuthal modulation
-

Outline

- Imaging in position space and GPDs
- TMDs
- Wigner functions
- Nuclei

Imaging in Position Space

- Form factor
 - → probe magnetic form factors to highest Q^2 (I guess at low Q^2 one loses sensitivity anyways...)
 - At $\epsilon \approx 1$ (unlike fixed target) → I guess that means no G_E ?
 - $Q^2 > 1.0$ (acceptance for $Q^2 < 1.0$ not there for electron), proton will need far forward detectors for low Q^2
 - No double spin asymmetries (too small)
 - Adding positron beam will help with studying two-photon processes
- e-d possible up to $Q^2 = 5 \text{ GeV}^2$
- Tensor polarization measurements up to 2.5 GeV^2

- Nuclei
 - Tensor polarization possible at EIC?

GPDs

- [306][309],[310]
- See pub in [306]
- Form factor of EMT