

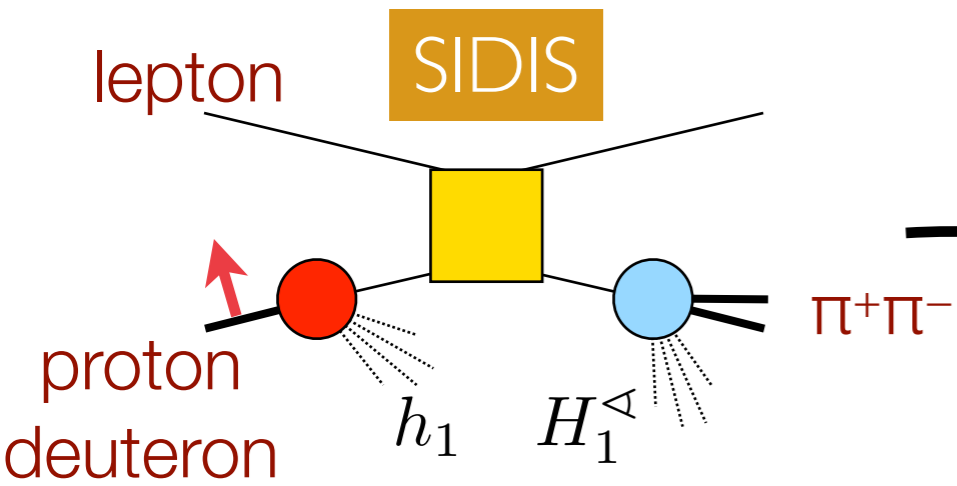
# Impact projections on uncertainty of transversity from EIC di-hadron channel

Marco Radici  
INFN - Pavia



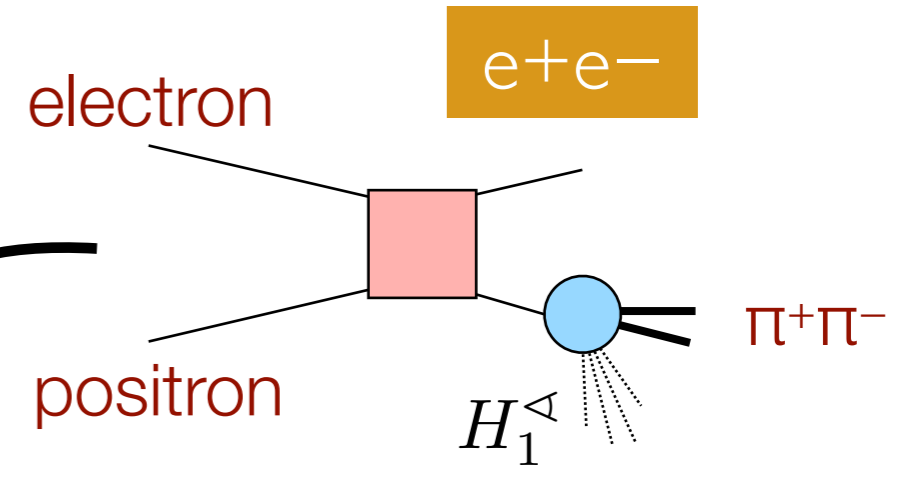
for the “Pavia group”

# (published) reference situation



hermes  
Airapetian et al.,  
JHEP **0806** (08) 017

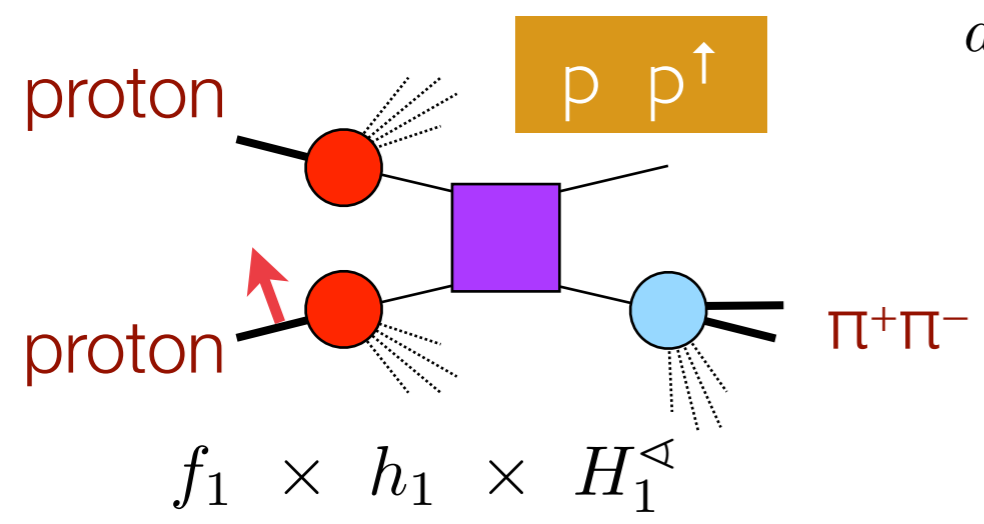
COMPASS  
Adolph et al., P.L. **B713** (12)  
Braun et al.,  
E.P.J. Web Conf. **85** (15) 02018



BELLE  
Vossen et al., P.R.L. **107** (11) 072004

$$A_{\text{SIDIS}}^{\sin(\phi_R + \phi_S)}(x, z, M_h^2) \sim - \frac{\sum_q e_q^2 h_1^q(x) \frac{|\mathbf{R}_T|}{M_h} H_{1,q}^{\triangleleft}(z, M_h^2)}{\sum_q e_q^2 f_1^q(x) D_{1,q}(z, M_h^2)}$$

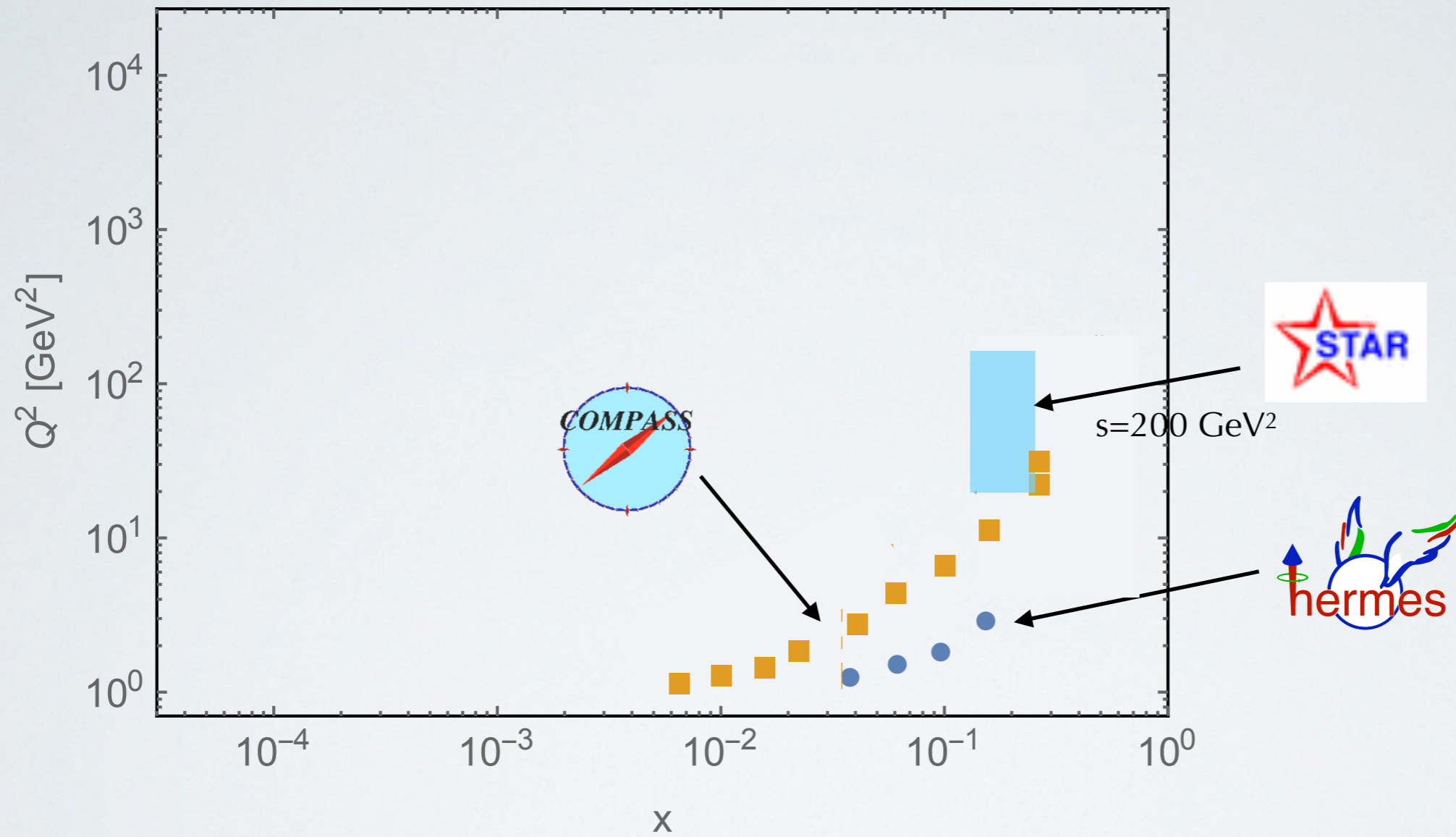
$$\frac{d\sigma_{UT}}{d\sigma_{UU}} \propto \frac{\sum_{a,b,c,d} \int \frac{dx_a dx_b}{8\pi^2 \bar{z}} f_1^a(x_a) h_1^b(x_b) \frac{d\hat{\sigma}_{ab\uparrow \rightarrow c\uparrow d}}{d\hat{t}} H_1^{\triangleleft c}(\bar{z}, M_h)}{\dots f_1^a f_1^b \frac{d\hat{\sigma}_{ab \cdot \rightarrow c \cdot d}}{d\hat{t}} D_1^c}$$



STAR  
run 2006  
(s=200 GeV<sup>2</sup>)  
Adamczyk et al. (STAR),  
P.R.L. **115** (15) 242501

efficient fit requires  
Mellin transform

# the phase space





# functional form fulfills Soffer bound

functional form whose Mellin transform can be computed analytically and complying with Soffer Bound at any  $x$  and scale  $Q^2$

$$h_1^{qv}(x; Q_0^2) = F^{qv}(x) \left[ SB^q(x) + \overline{SB}^{\bar{q}}(x) \right]$$

Soffer Bound

$$2|h_1^q(x, Q^2)| \leq 2 SB^q(x, Q^2) = |f_1^q(x, Q^2) + g_1^q(x, Q^2)|$$

MSTW08

DSSV

$$F^{qv}(x) = \frac{N_{qv}}{\max_x [|F^{qv}(x)|]} x^{A_{qv}} [1 + B_{qv} \text{Ceb}_1(x) + C_{qv} \text{Ceb}_2(x) + D_{qv} \text{Ceb}_3(x)]$$

Ceb<sub>n</sub>(x) Chebyshev polynomial

10 fitting parameters

constrain parameters

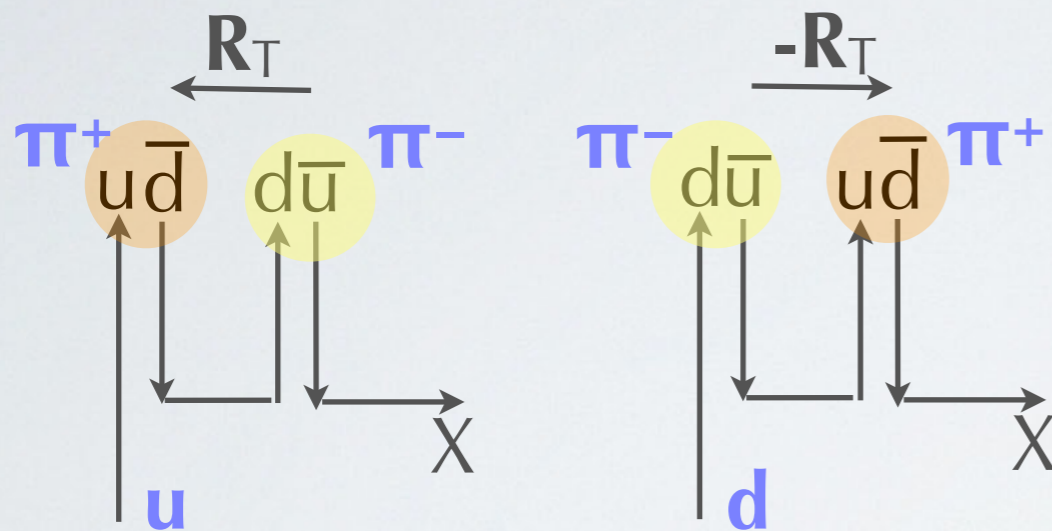
$$|N_{qv}| \leq 1 \Rightarrow |F^{qv}(x)| \leq 1 \quad \text{Soffer Bound ok at any } Q^2$$

$$h_1^q(x) \stackrel{x \rightarrow 0}{\approx} x^{A_q + \text{const}} \quad \text{such that tensor charge is finite}$$

# currently, only LO analysis

$$A_{UT}^{\sin(\phi_R+\phi_S)}(x, z, M_h^2) \propto -\frac{|\mathbf{R}|}{M_h} \frac{\sum_q e_q^2 h_1^q(x) H_1^{\triangleleft q}(z, M_h^2)}{\sum_q e_q^2 f_1^q(x) D_1^q(z, M_h^2)}$$

$\pi^+\pi^-$   
tree level



$$\left. \begin{aligned} H_1^{\triangleleft u} &= -H_1^{\triangleleft d} \\ H_1^{\triangleleft q} &= -H_1^{\triangleleft \bar{q}} \\ D_1^q &= D_1^{\bar{q}} \end{aligned} \right\} \begin{array}{l} \text{isospin symmetry} \\ \text{charge conjugation} \end{array}$$

access only  $q-\bar{q} = q_v$ ,  $q=u,d$   
valence flavors in SIDIS  $A_{UT}$

# theoretical uncertainties

## unpolarized Di-hadron Fragmentation Function $D_1$

- **quark**  $D_1^q$  is **well** constrained by  $e^+e^- \rightarrow (\pi^+\pi^-) X$  (Montecarlo)
- **gluon**  $D_1^g$  is **not** constrained by  $e^+e^- \rightarrow (\pi^+\pi^-) X$  (currently, LO analysis)
- **no data** available yet for  $p p \rightarrow (\pi^+\pi^-) X$

we don't know anything about the gluon  $D_1^g$

our choice:

set  $D_1^g(Q_0) =$

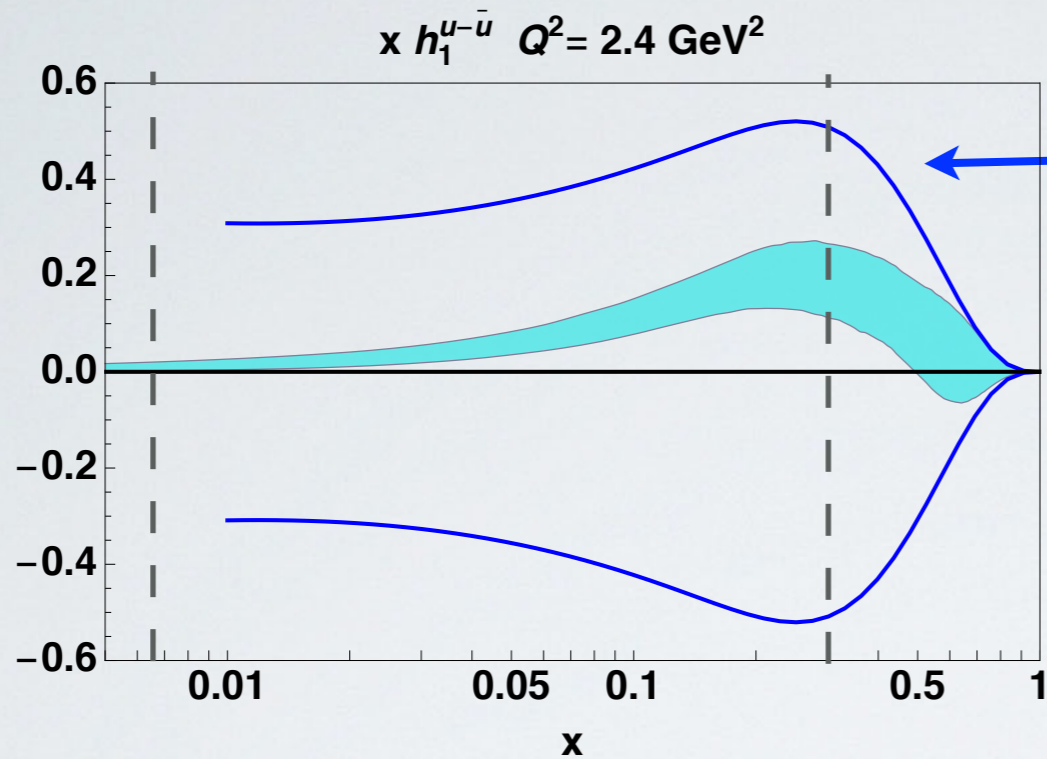
$$\begin{cases} 0 \\ D_1^u(Q_0) / 4 \\ D_1^u(Q_0) \end{cases}$$

←  $\sim$  1-hadron  $D_1^g(Q_0)$



# Hermes + Compass + STAR

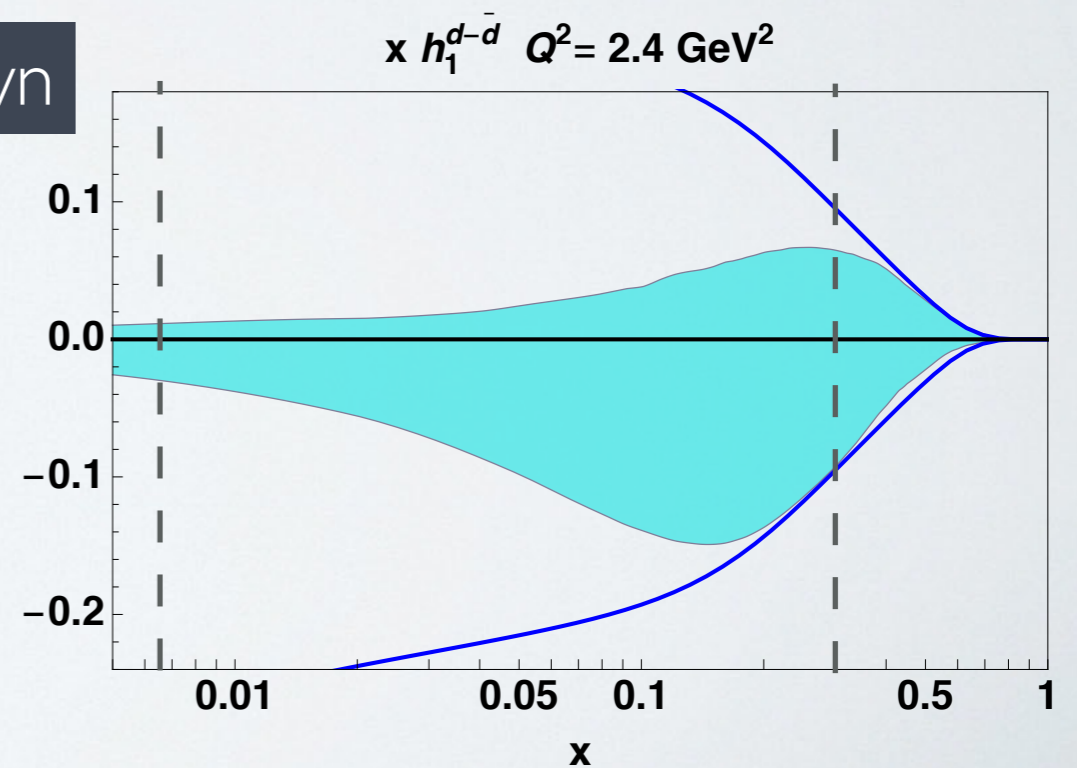
up



Soffer  
bound

uncertainty band from  
90% of 600 replicas =  
max uncertainty on  $D_{1^g}(Q_0)$

down



# assumptions for fit of EIC pseudodata

SIDIS

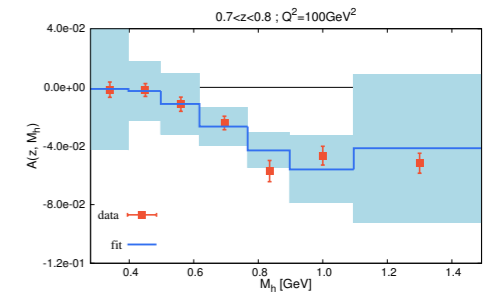
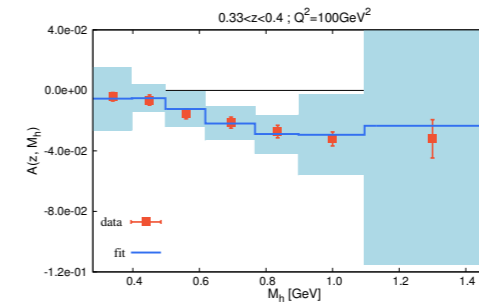
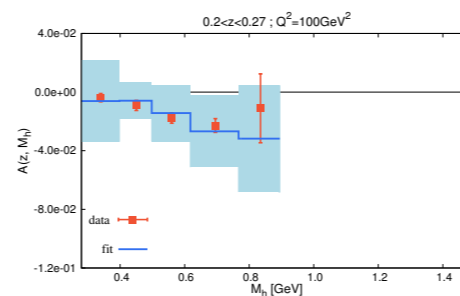
$$A_{\text{SIDIS}}^{\sin(\phi_R+\phi_S)}(x, z, M_h^2) \sim - \frac{\sum_q e_q^2 h_1^q(x) \frac{|\mathbf{R}_T|}{M_h} H_{1,q}^{\leftarrow}(z, M_h^2)}{\sum_q e_q^2 f_1^q(x) D_{1,q}(z, M_h^2)}$$

- full analysis would require simultaneous fit of  $h_1$  and  $D_1, H_1^{\leftarrow}$  : **not enough time** by the Yellow Report deadline !

## Alternative

- insert  $D_1, H_1^{\leftarrow}$  from published fit, interpolated in the  $(Q, z, M_{\pi^+\pi^-})$  EIC grid, and fit EIC pseudodata with a variable functional form for  $h_1$  only
- assume  $\Delta f_1 = \Delta D_1 \sim 0$  ( $D_1$  obtained by fitting Belle MC => unlimited precision) hence  $\Delta h_1 \propto \Delta H_1^{\leftarrow}$
- assume that precision of EIC pseudodata would reduce  $\Delta H_1^{\leftarrow} \Rightarrow 1/3 \Delta H_1^{\leftarrow}$  and compute projections on reduction of  $\Delta h_1$

$\Delta H_1^{\leftarrow}(M_{\pi^+\pi^-})$  for various  $z$  bins

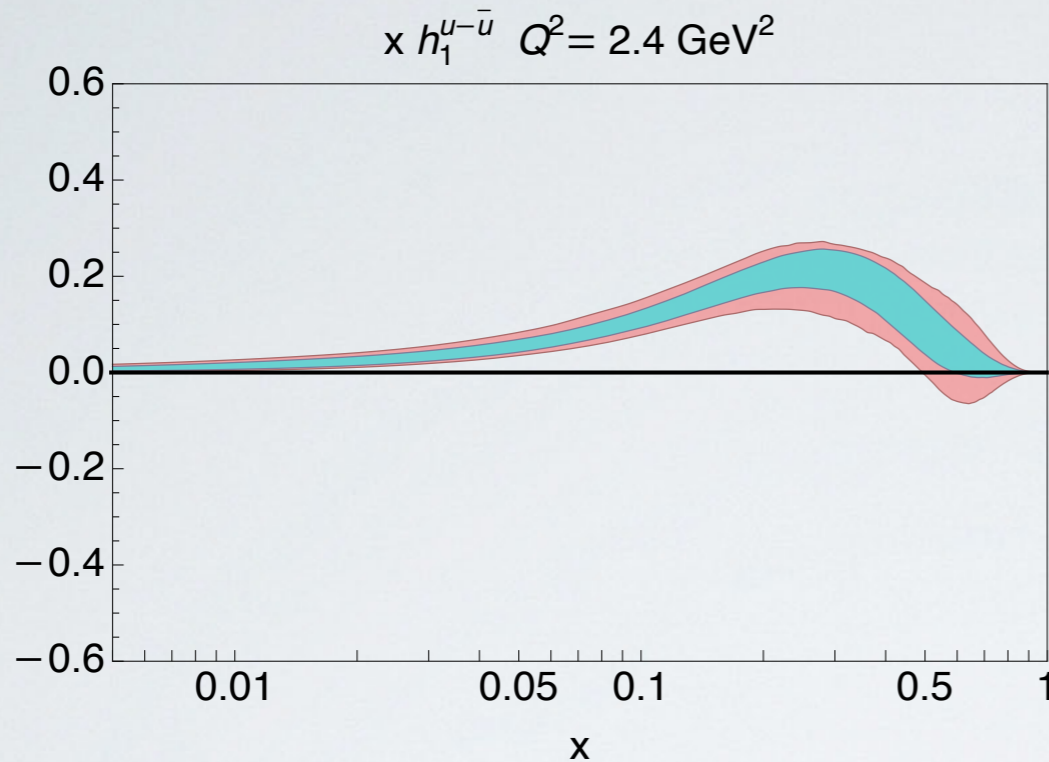


*Courtoy et al., P.R. D85 (12) 114023*



# Hermes + Compass + STAR + EIC 10x100 proton

up



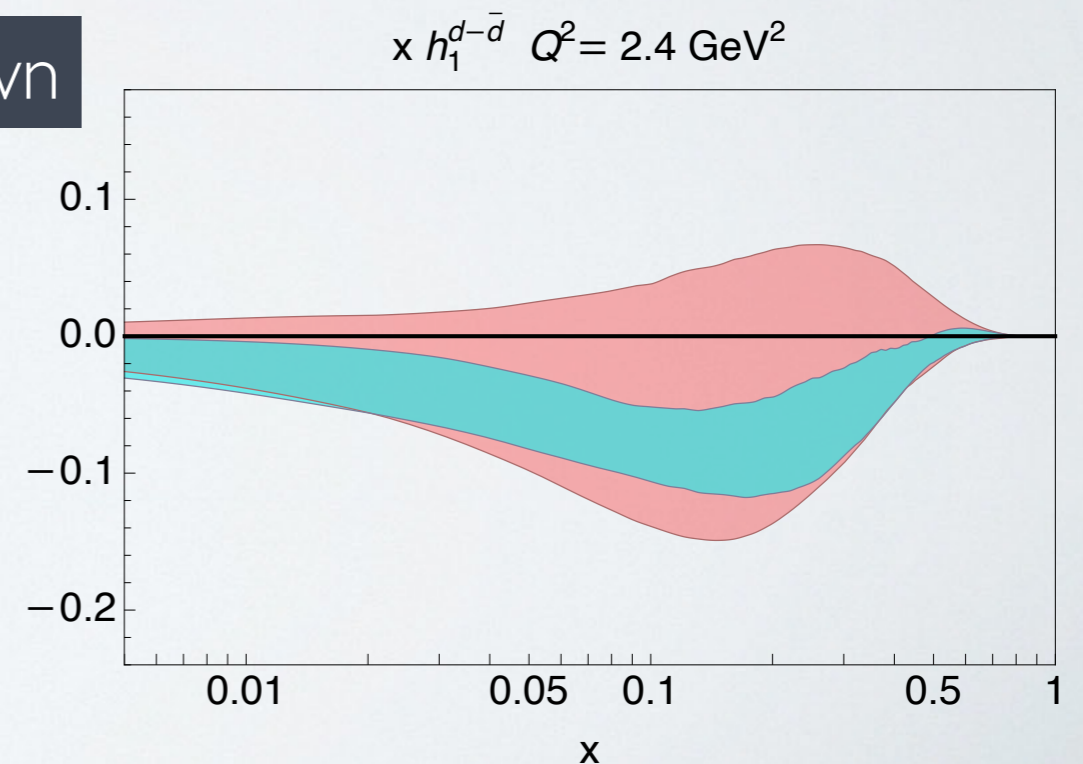
uncertainty band from  
90% of 600 replicas =  
max uncertainty on  $D_{1g}(Q_0)$

published fit

+ EIC 10x100 proton

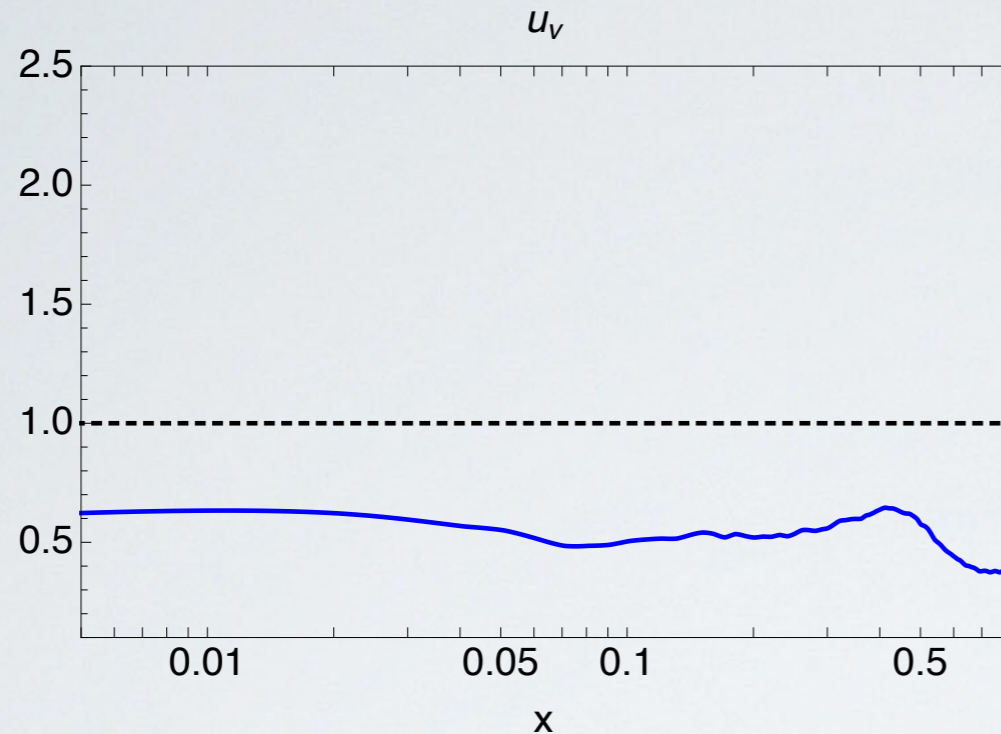
EIC 10x100  $^3\text{He}$   
is running...

down



# Hermes + Compass + STAR + EIC 10x100 proton

up



$$\Delta H_1^* \Rightarrow 1/3 \Delta H_1^*$$



$$\Delta h_1 \Rightarrow \sim 1/2 \Delta h_1$$

width (+ EIC 10x100 proton)

width (published fit)

down

