Università degli Studi
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INFN Istituto Nazionale di Fisica Nucleare

Precision extraction of MW from observables at hadron colliders

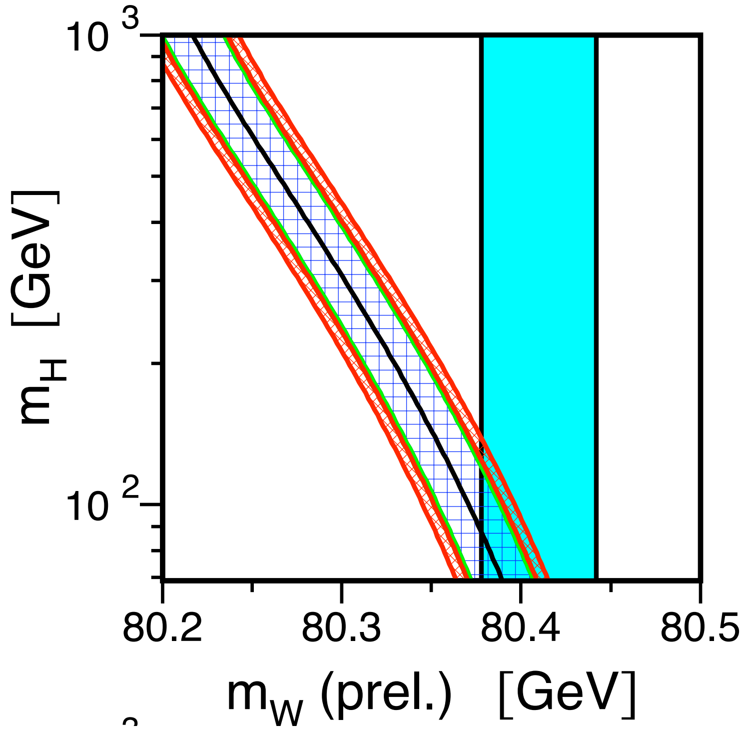
Alessandro Vicini
University of Milano, INFN Milano

The physics of W and Z bosons
Brookhaven, June 24th 2010

Thanks to: G.Bozzi, C.M.Carloni Calame,
G. Ferrera, S.Alioli, E. Re, A.Mueck, D.Wackeroth
all the other participants to the W mass workshop

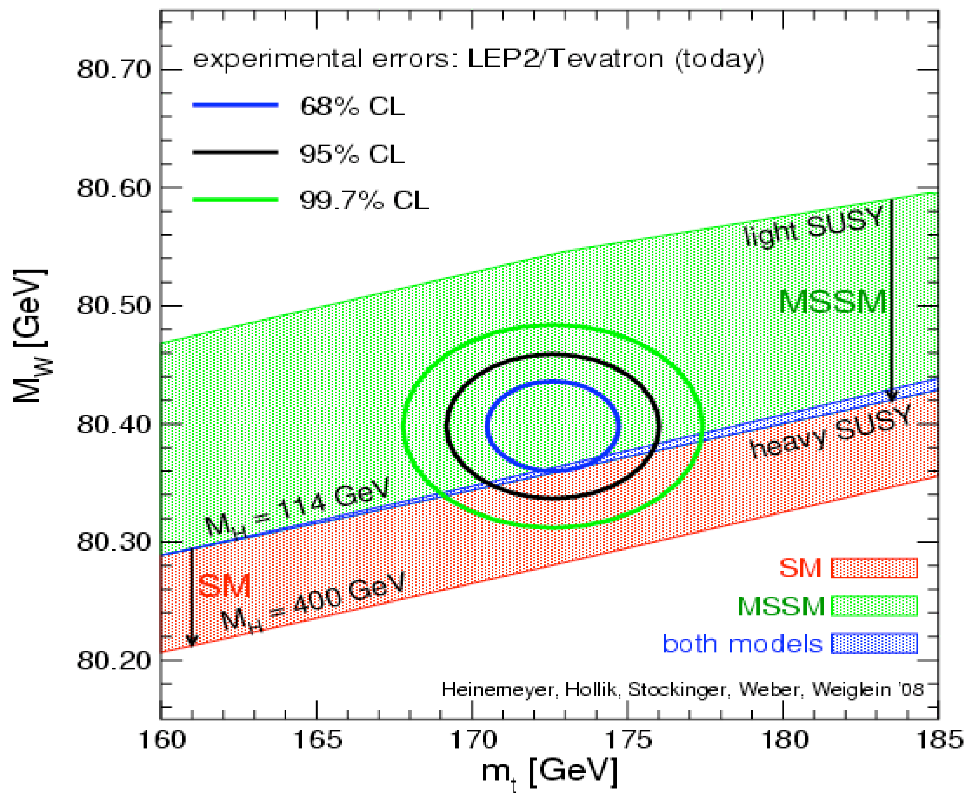
Relevance of a precise W mass measurement

Sensitivity to the precise value of the Higgs boson mass or e.g. to SUSY particles



Awramik, Czakon, Freitas, Weiglein   Degrassi, Gambino, Passera, Sirlin

$$M_W = M_W^0 - 0.0581\ \ln\left(\frac{M_H}{100\ \mathrm{GeV}}\right) - 0.0078\ln^2\left(\frac{M_H}{100\ \mathrm{GeV}}\right) - 0.085\ \left(\frac{\alpha_s}{0.118} - 1\right)$$
$$- 0.518\ \left(\frac{\Delta\alpha^{(5)}_{had}(M_Z^2)}{0.028} - 1\right) + 0.537\ \left(\left(\frac{m_t}{175\ \mathrm{GeV}}\right)^2 - 1\right)$$



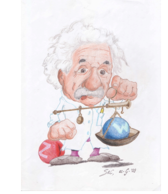
$$m_W = m_W\left(\Delta r^{SM,MSSM}\right)$$

$$\Delta r^{SM,MSSM} = \Delta r^{SM,MSSM}\left(m_t, m_H, m^{SUSY}, \ldots\right)$$

W mass workshop
Milano, March 17-18 2009

http://wwwteor.mi.infn.it/~vicini/wmass.html

Radiative corrections and simulation tools: QCD matching



ALPGEN
M.L.Mangano et al., JHEP **0307**, 001 (2003)

LO-QCD matched with HERWIG QCD Parton Shower MLM prescription

SHERPA
F. Krauss et al., JHEP **0507**, 018 (2005)

LO-QCD matched with QCD Parton Shower CCKW algorithm

MADGRAPH/MADEVENT
T.Stelzer, W.F.Long, Comp.Phys.Commun.81 (1994) 357, F.Maltoni, T.Stelzer, JHEP 02 (2003) 027

LO-QCD matched with QCD Parton Shower MLM prescription

Resbos
C.Balazs and C.P. Yuan, Phys.Rev. **D56** (1997) 5558

NLO-QCD matched with resummation of NLL and NNLL of log(p_T^W/m_W)

MC@NLO
S. Frixione and B.R.Webber., JHEP **0206**, 029 (2002)

NLO-QCD matched with the HERWIG QCD Parton Shower

POWHEG
P.Nason, JHEP **0411** 040 (2004) S.Frixione, P.Nason, C.Oleari, JHEP **0711** 070 (2007)

NLO-QCD matched with any vetoed QCD Parton Shower

BCDFG
G.Bozzi, S.Catani, D.De Florian, G.Ferrera, M.Grazzini, Nucl.Phys.**B815** (2009) 174

NLO-QCD matched with resummation of NLL of log(p_T^W/m_W)
(factorized prescription, explicit dependence on the resummation scale)

EW results and tools

$\mathcal{O}(\alpha_S^2) \approx \mathcal{O}(\alpha_{\rm em})$ → Need to worry about EW corrections

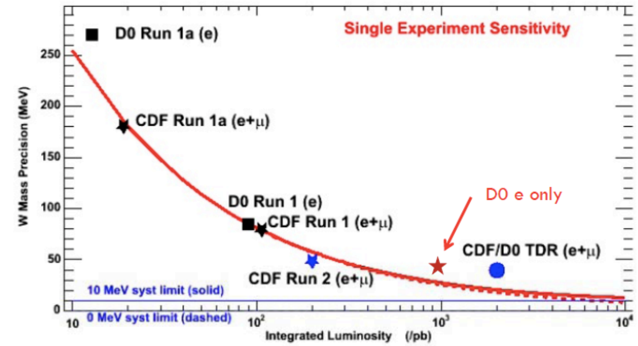
W production

Pole approximation	D.Wackeroth and W. Hollik, PRD 55 (1997) 6788	
	U.Baur et al., PRD 59 (1999) 013002	
Exact O(alpha)	V.A. Zykunov et al., EPJC 3 (2001) 9	
	S. Dittmaier and M. Krämer, PRD 65 (2002) 073007	DK
	U. Baur and D.Wackeroth, PRD 70 (2004) 073015	WGRAD2
	A. Arbuzov et al., EPJC 46 (2006) 407	SANC
	C.M.Carloni Calame et al., JHEP 0612:016 (2006)	HORACE
Photon-induced processes	S. Dittmaier and M. Krämer, Physics at TeV colliders 2005	
	A. B.Arbuzov and R.R.Sadykov, arXiv:0707.0423	
Multiple-photon radiation	C.M.Carloni Calame et al.,PRD 69 (2004) 037301, JHEP 0612:016 (2006)	HORACE
	S.Jadach and W.Placzek, EPJC 29 (2003) 325	WINHAC
	S.Brensing, S.Dittmaier, M. Krämer and M.M.Weber, arXiv:0708.4123	DK

Z production

only QED	U.Baur et al., PRD 57 (1998) 199	
Exact O(alpha)	U.Baur et al., PRD 65 (2002) 033007	ZGRAD2
	V.A. Zykunov et al., PRD75 (2007) 073019	
	C.M.Carloni Calame et al., JHEP 0710:109 (2007)	HORACE
Multiple-photon radiation	C.M.Carloni Calame et al., JHEP 0505:019 (2005)	HORACE
	JHEP 0710:109 (2007)	

Outline



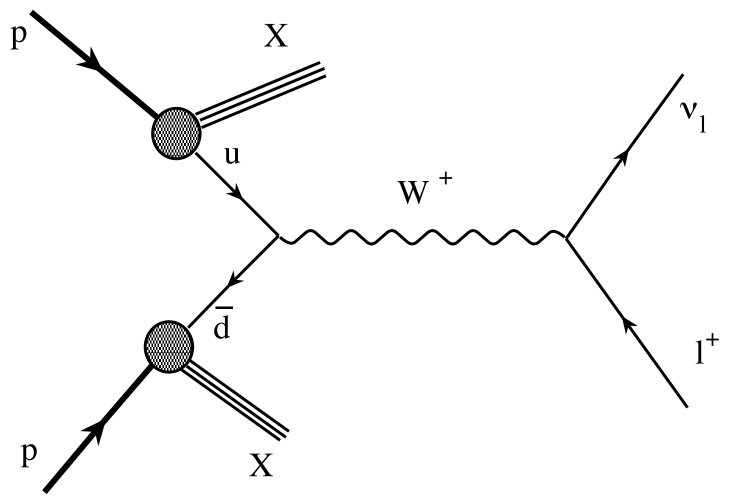
- measurement of MW (probably) at the 15 MeV level
  at the Tevatron
- measurement of this pseudo-observable heavily involves
  theoretical ingredients

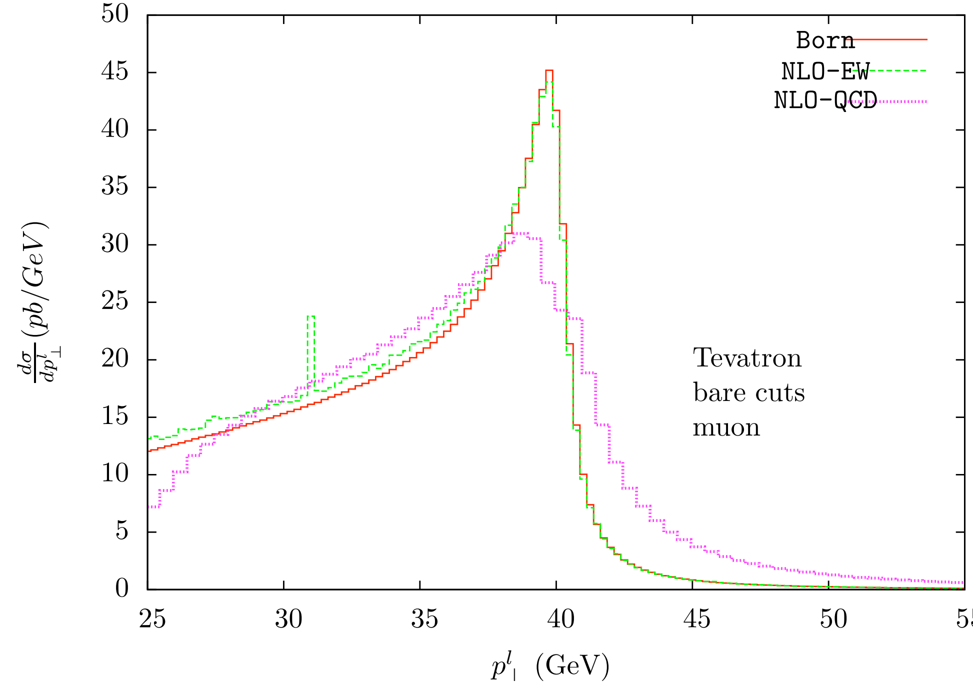
- classification of the impact of different classes of radiative corrections
  in terms of shifts of the final value of MW
- estimate of different sources of theoretical uncertainty
  to obtain a final theoretical systematic error on MW

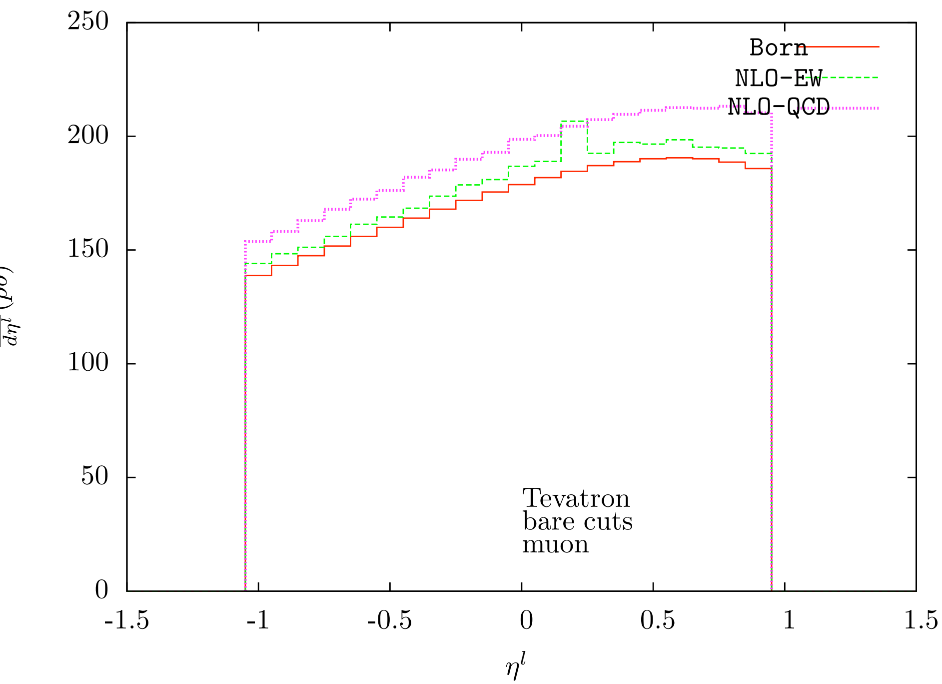
- fixed order calculations provide the first basic estimates
  but
  a realistic simulation shows which effects survive after e.g.
  convolution with multiple gluon/photon emission
  smearing of lepton momenta or photon recombination

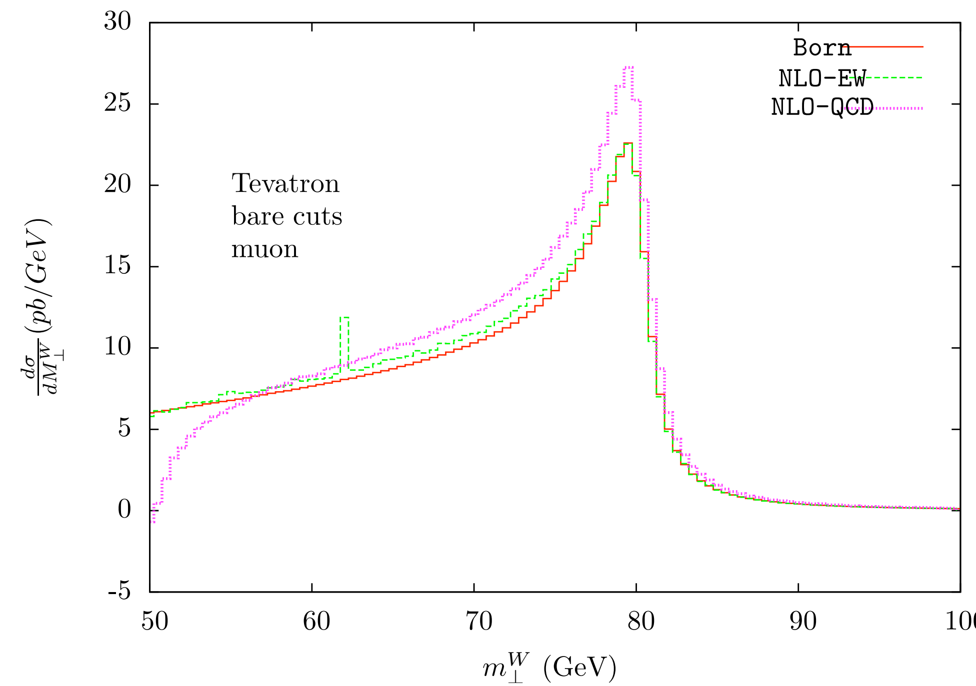
  - change of EW input scheme, use of factorized expressions, higher orders
  - combination of QCD+EW corrections
  - QCD corrections by different codes
  - PDF uncertainties

The Drell-Yan process at fixed (NLO) order (α_0 input scheme)

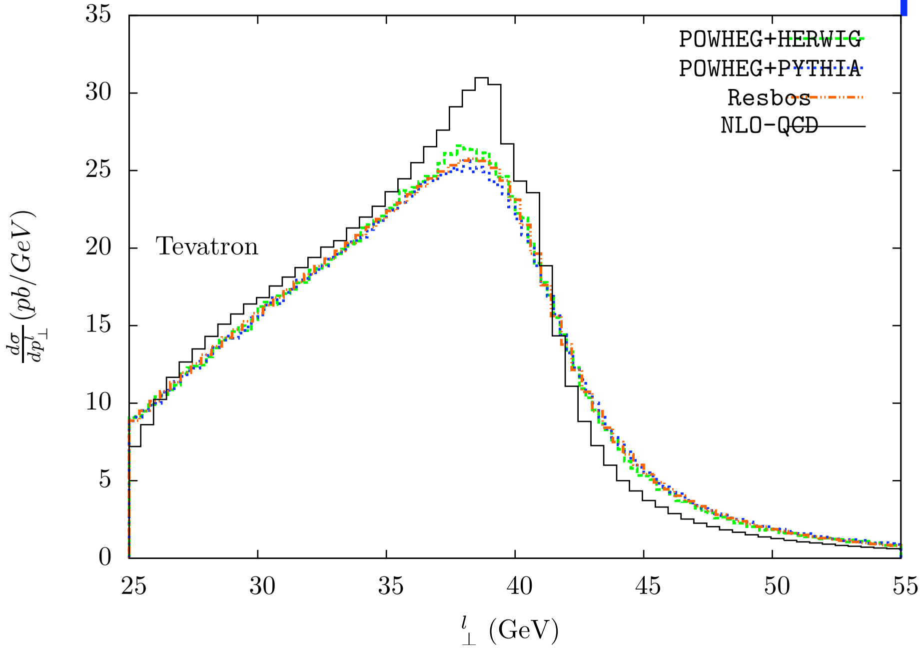


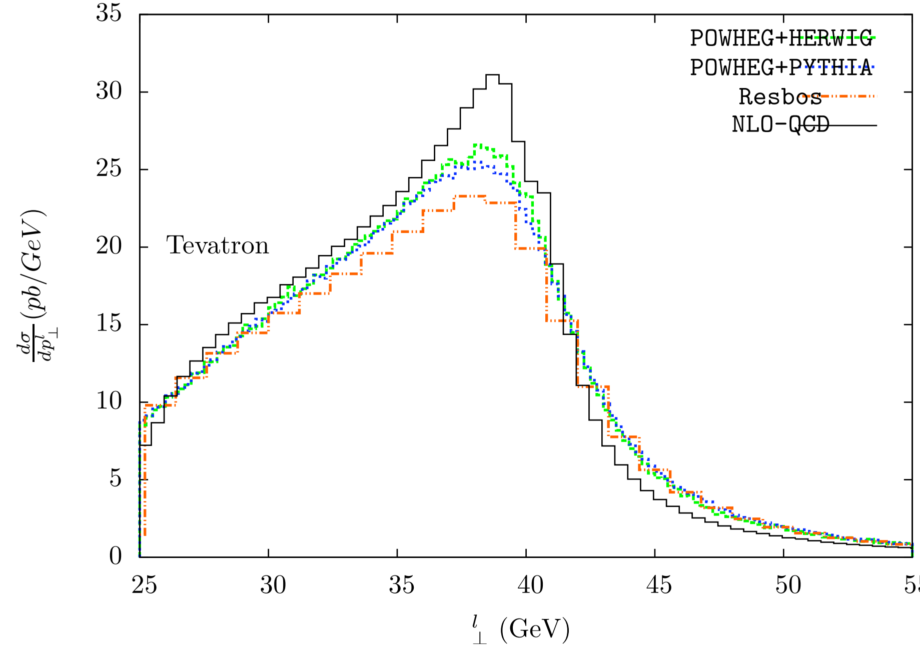


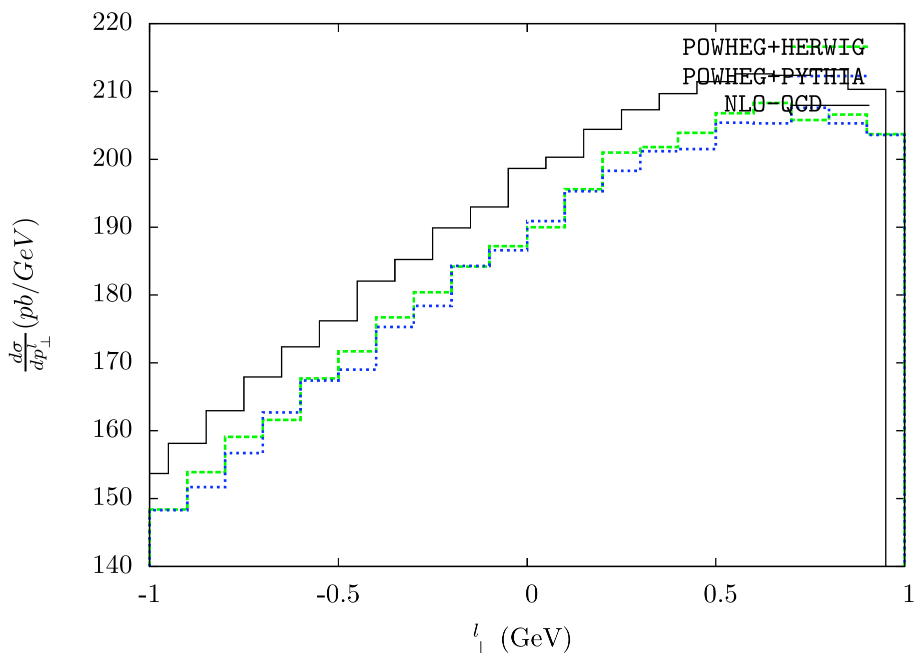


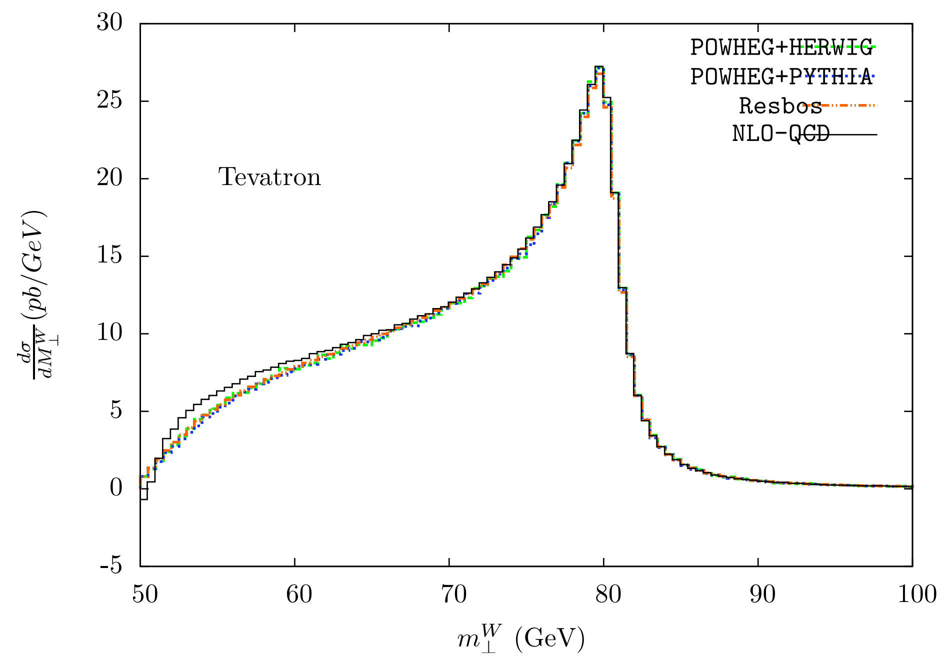


The effect of initial state multiple gluon emission

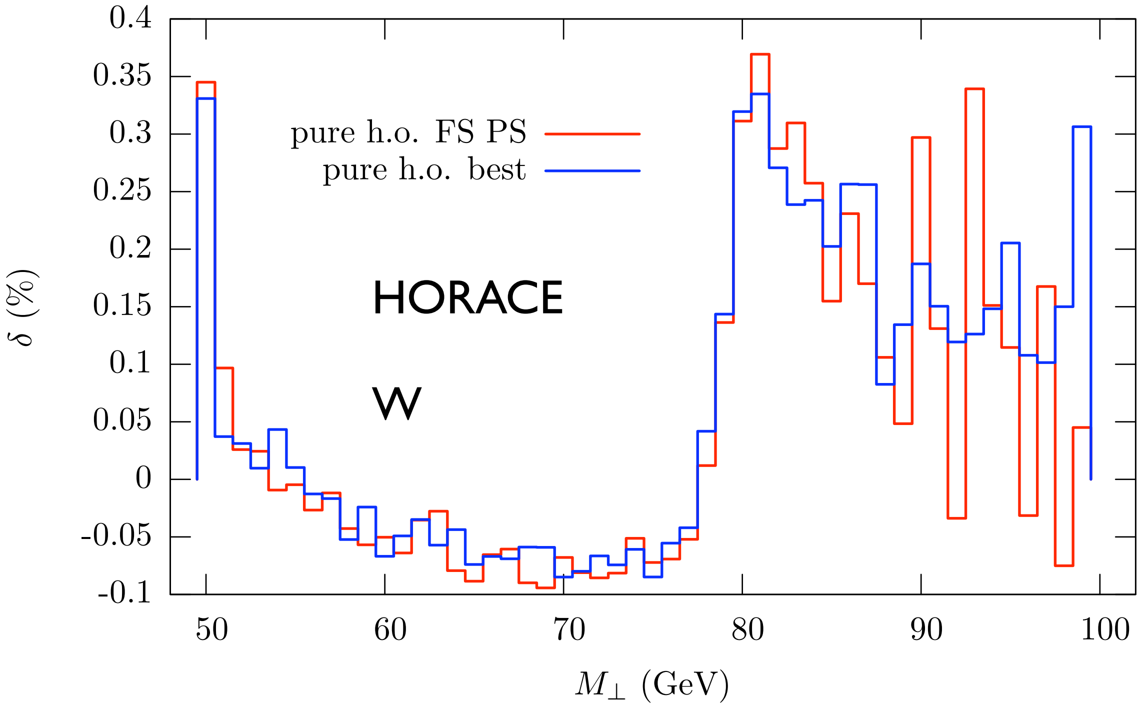








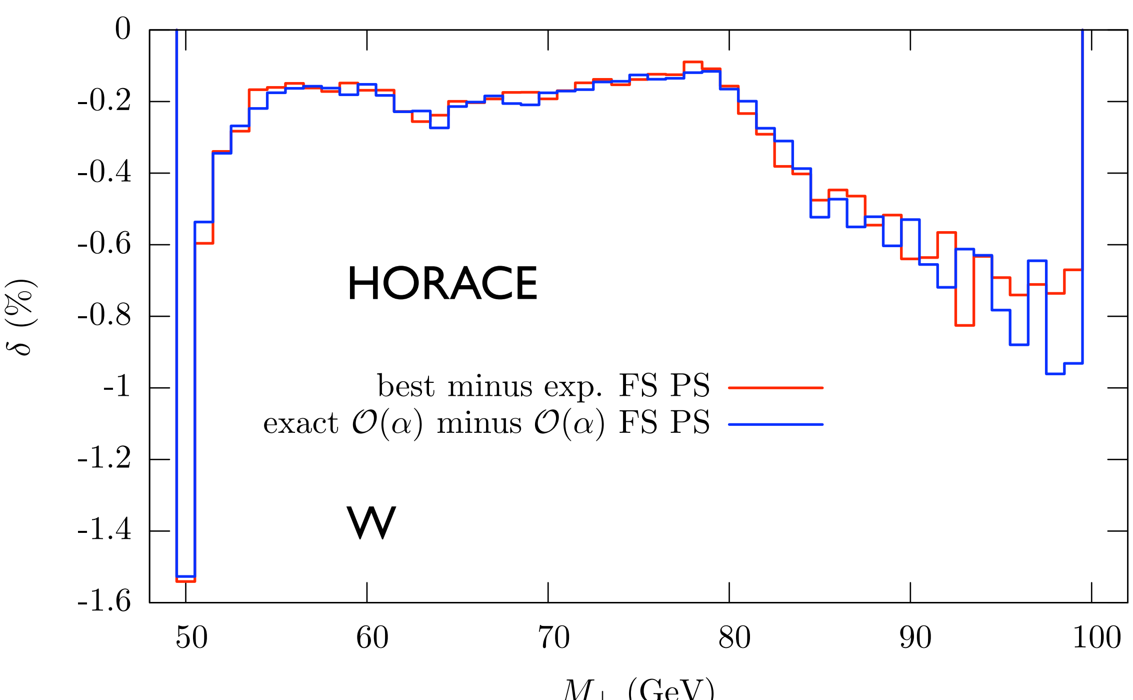
The effect of multiple photon emission and of subleading EW terms

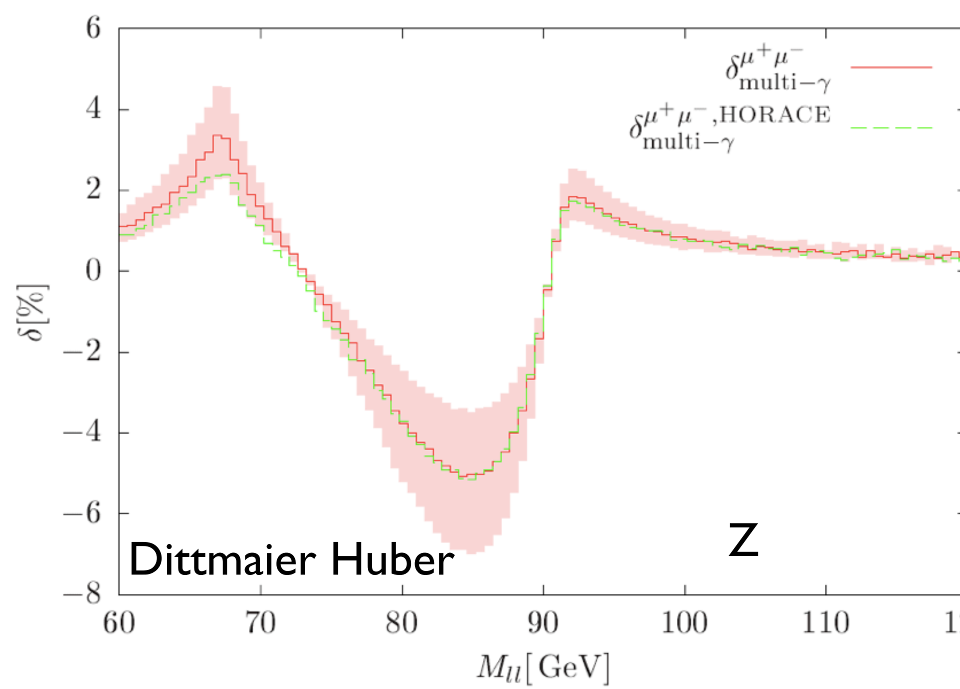


Effects of multiple photon emission studied

HORACE : full all orders QED Parton Shower

W-ZGRAD, Dittmaier-Huber:
final state structure function approach





The W mass as pseudo-observable

The W mass is not a property of measured (final state) particles, but
it is rather an input parameter of the Lagrangian which can be chosen
to maximize the agreement theory-data for some given distributions.

If we want to measure MW, in the SM, in the gauge sector, it is possible to use as inputs
(α, m_W, m_Z) (G_μ, m_W, m_Z) but not (α, G_μ, m_Z)

The W mass is defined starting from the pole, in the complex plane, of the W propagator

Since the final state neutrino escapes detection, it is not possible to reconstruct all the components of the W momentum (and therefore its virtuality).
It is possible to infer the value of the transverse components of the neutrino
provided one has an excellent understanding of initial state QCD+QED radiation

The lepton and the missing transverse momentum and transverse mass distributions
have a jacobian peak about the W mass.
The peak of distributions provides a strong sensitivity to the value of MW.

$$M_\perp^W = \sqrt{2 p_\perp^l p_\perp^\nu \, (1 - \cos\phi_{l\nu})}$$

The template-fitting procedure

A distribution computed with a given set of radiative corrections and
with a given value MW_0
is treated as a set of pseudo-data

The templates are prepared in Born approximation, using 100 values of MW_i
Each template is compared to the pseudo-data and a distance is measured

$$\chi_i^2 = \sum_{j=1}^{N_{bins}} \frac{\left(O_j^{data} - O_j^{templ=i}\right)^2}{\left(\sigma_j^{data}\right)^2} \qquad i = 1, \ldots, N_{templ}$$

The template that minimizes the distance is considered as the "preferred one"
and the value of MW, used to generate it, is the "measured" MW

The difference $MW-MW_0$ represents the shift induced on the measurement of the W mass
by including that specific set of radiative corrections

The distributions used in the evaluation of χ^2_i in general do not have the same normalization.
It is also possible to compare distributions that have been normalized to their respective xsecs,
to appreciate the role of the shape differences

Validation of the template-fitting procedure

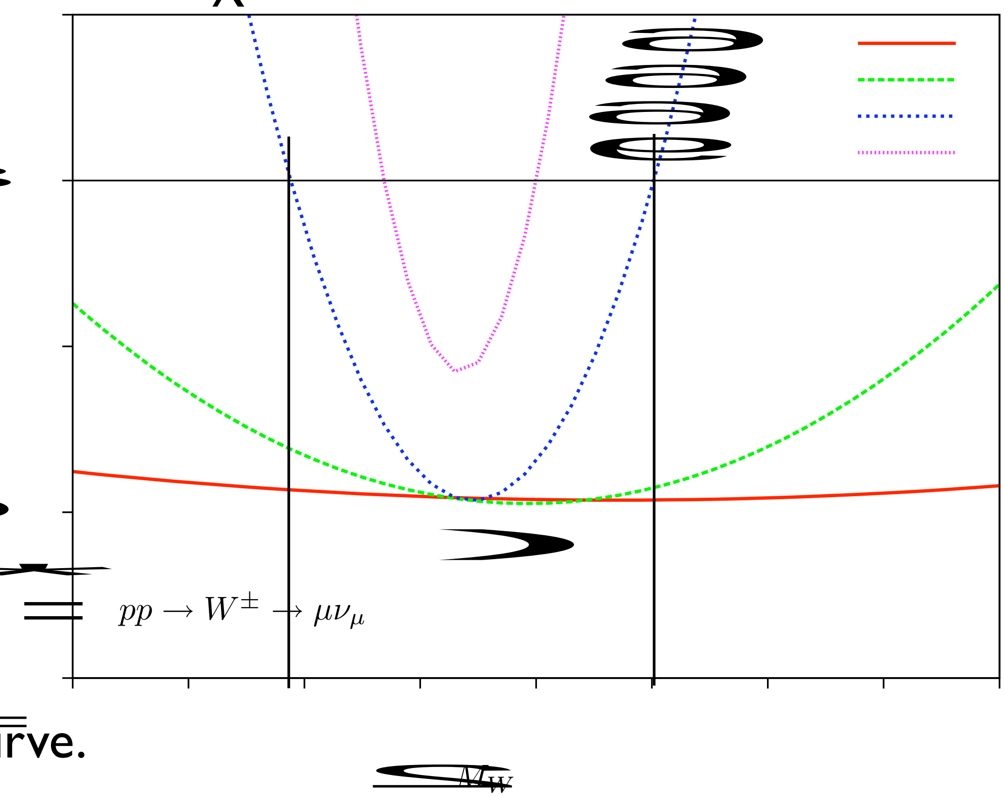
In this template-fitting procedure,
the reduced χ^2 is never close to one because the distributions are "by construction" different

Fit pseudo-data computed in Born approximation reduced $\chi^2 \sim 1$
The fit should exactly find the nominal value MW_0
used to generate the Born pseudo-data

The accuracy of the fit depends on the error
associated to each bin of the pseudo-data

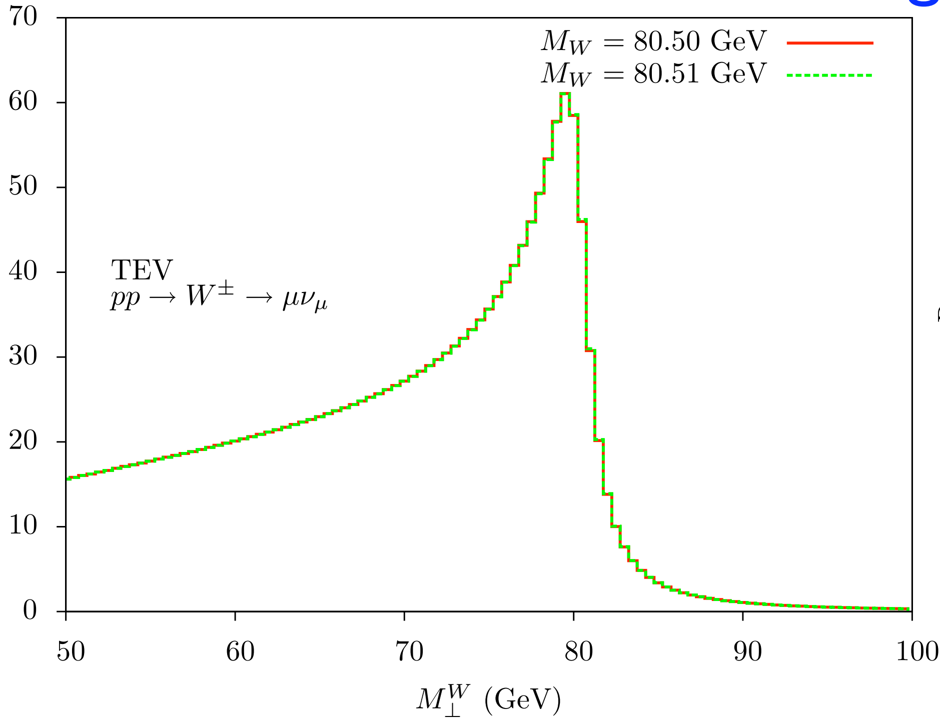
In the case of Born pseudo-data,
the $\Delta\chi^2 = 1$ MW points fix the 68% C.L. interval
associated to the estimate of the preferred MW.

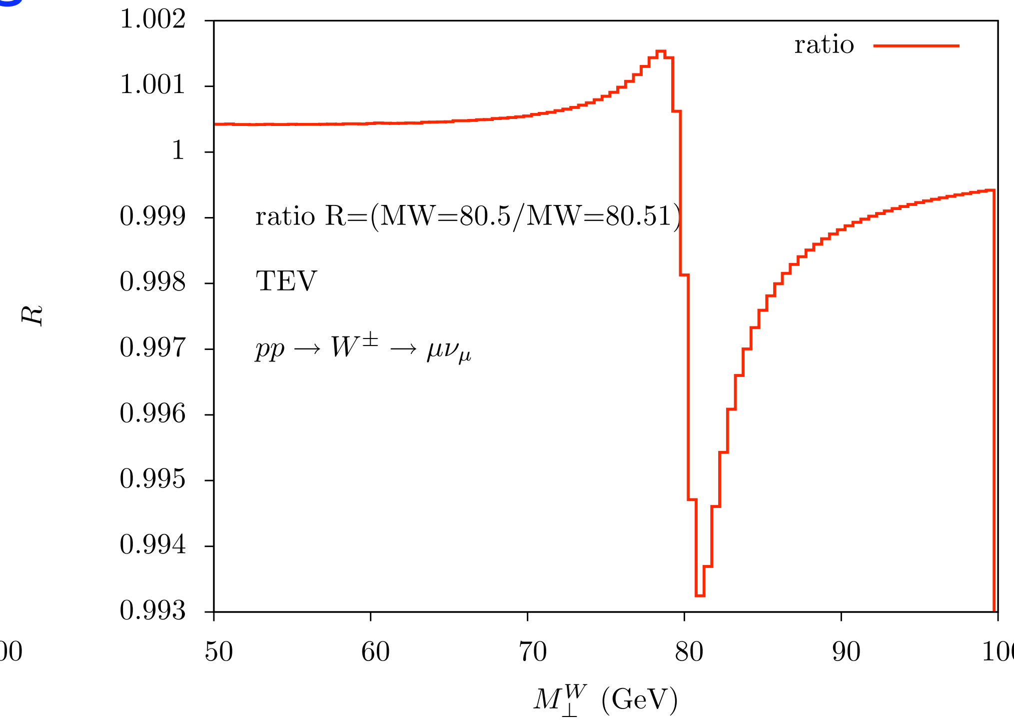
A larger number of pseudo-data events increases
the accuracy of the prediction, shrinking the χ^2 curve.



The templates are not smooth functions, but are generated with a Montecarlo
They also suffer of statistical fluctuations.
We can not arbitrarily increase the number of pseudo-data events,
because we are limited by the number of events used to generate the templates

Estimate of MW shift due to higher order corrections in the fit





The ratio of two distributions generated with nominal MW which differ by 10 MeV shows a deviation from unity at the level of few per mil, with non trivial shape

If we aim at measuring MW with 10-15 MeV of error, are we able to control the shape of the distributions and the theoretical uncertainties at the few per mil level?

Not all the radiative corrections have the same impact on the MW measurement
not all the uncertainties are equally bad on the final error

The HORACE formula and the input-scheme dependence

$$d\sigma^{\infty}_{matched} = \Pi_S(Q^2) F_{SV} \sum_{n=0}^{\infty} d\hat{\sigma}_0 \frac{1}{n!} \prod_{i=0}^{n} \left(\frac{\alpha}{2\pi} P(x_i)\, I(k_i)\, dx_i\, d\cos\theta_i\, F_{H,i} \right)$$

$$F_{SV} = 1 + \frac{d\sigma^{\alpha,ex}_{SV} - d\sigma^{\alpha,PS}_{SV}}{d\sigma_0} \qquad F_{H,i} = 1 + \frac{d\sigma^{\alpha,ex}_{H,i} - d\sigma^{\alpha,PS}_{H,i}}{d\sigma^{\alpha,PS}_{H,i}}$$

The matched HORACE formula is based on the all-orders QED Parton Shower structure

The presence of the overall Sudakov form factor guarantees the "semi-classical" limit
The Sudakov form factor contains the (IR) LL virtual corrections

The exact O(α) accuracy is reached by adding
- finite (no IR-div) soft+virtual effect in the overall factor F_SV
- exact (vs. eikonal) hard matrix element effects to every photon emission F_H,i

This formula has to be compared with a fixed order expression, where the precise sharing of 0- and 1-photon events can be slightly different

$$\alpha_0 \quad : \qquad \sigma = \alpha_0^2 \sigma_0 + \alpha_0^3 (\sigma_{SV} + \sigma_H)$$

The HORACE formula and its impact on the MW measurement

$$d\sigma^{\infty}_{matched} \; = \; \Pi_S(Q^2) F_{SV} \sum_{n=0}^{\infty} d\hat{\sigma}_0 \, \frac{1}{n!} \prod_{i=0}^{n} \left(\frac{\alpha}{2\pi} P(x_i) \, I(k_i) \, dx_i \, d\cos\theta_i \, F_{H,i} \right)$$

$$F_{SV} = 1 + \frac{d\sigma^{\alpha,ex}_{SV} - d\sigma^{\alpha,PS}_{SV}}{d\sigma_0} \qquad F_{H,i} = 1 + \frac{d\sigma^{\alpha,ex}_{H,i} - d\sigma^{\alpha,PS}_{H,i}}{d\sigma^{\alpha,PS}_{H,i}}$$

in the matched HORACE formula the change of input scheme affects:

the overall couplings of the Born cross-section $d\sigma_0$ and

the F_SV factor

in both cases it modifies the overall normalization of the cross section

the sharing of 0-, 1-, 2-,.... photon events remains the same in all the input schemes

and therefore the shape of the distributions (relevant for MW) remains the same

The input scheme changes differ at $O(\alpha^2)$ and

modify mostly the normalization of the cross section,

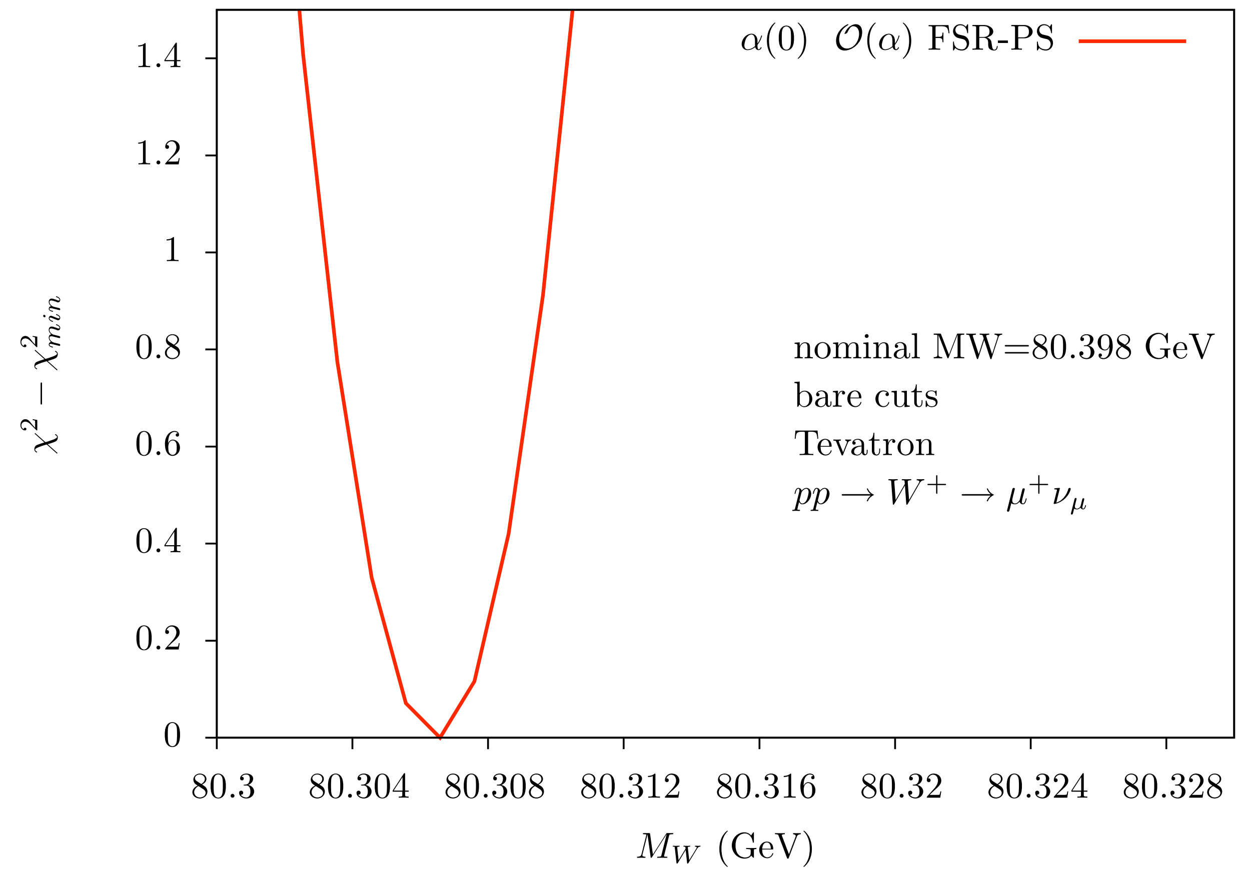
Therefore the χ^2 of the fit that exhibits a corresponding variation,

but also the precise MW determination is affected.

EW higher orders in the α_0 scheme

Born templates with 10 billions of events: maximal accuracy 2 MeV

The FSR QED Parton Shower
truncated at O(α)
yields a change of MW of -92 MeV



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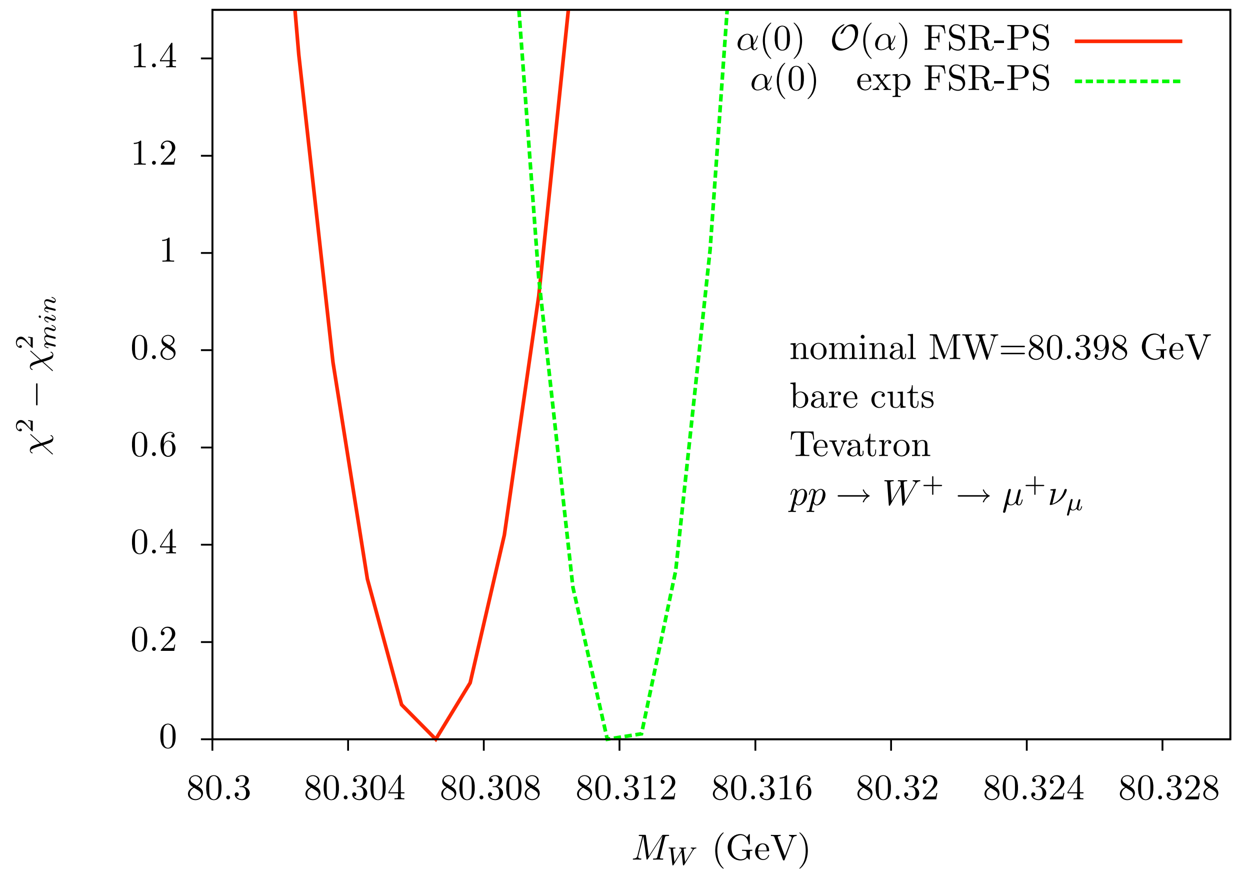
The FSR QED Parton Shower
to all orders
yields an additional shift of +6 MeV



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The FSR QED Parton Shower
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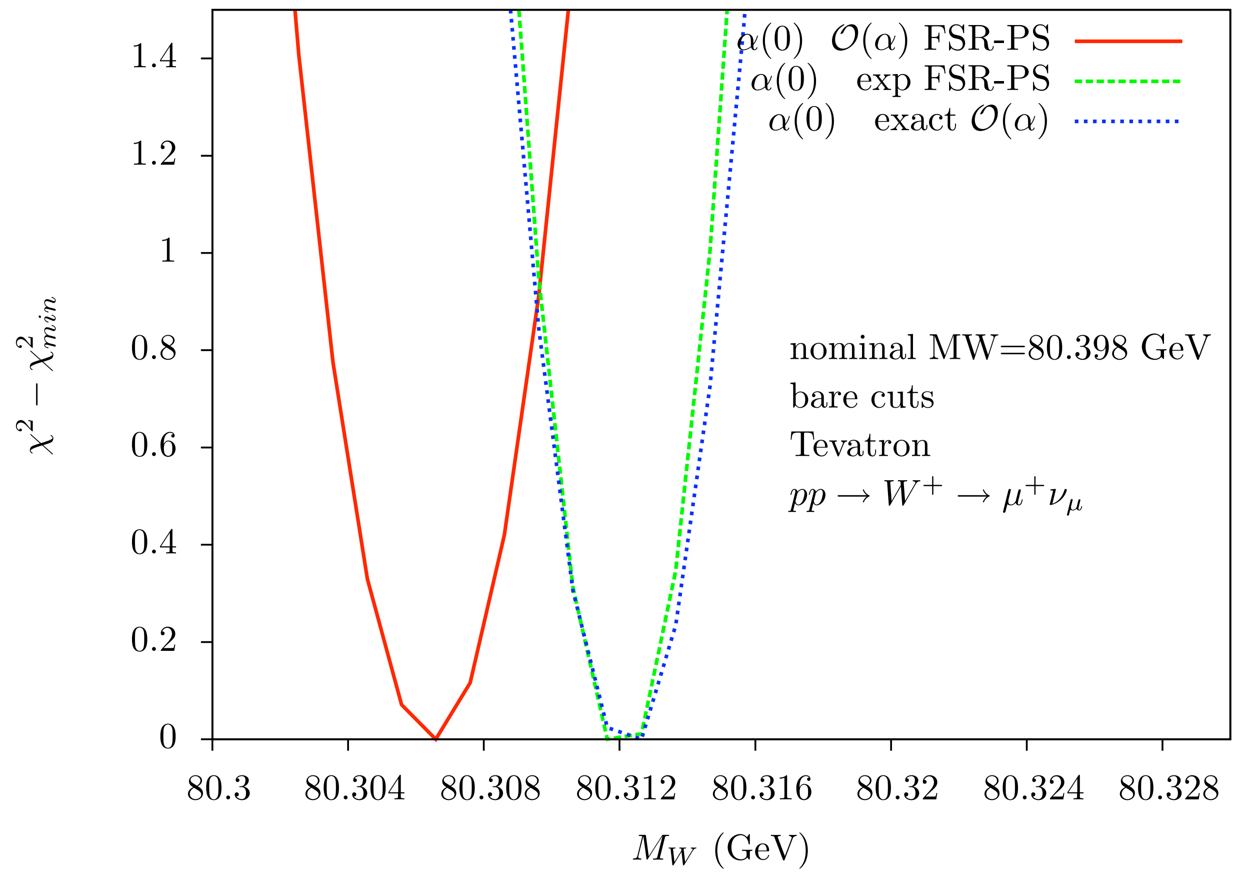
The exact matrix element at O(α)
and
O(α) FSR QED PS prediction
differ by +6 MeV (subleading EW)



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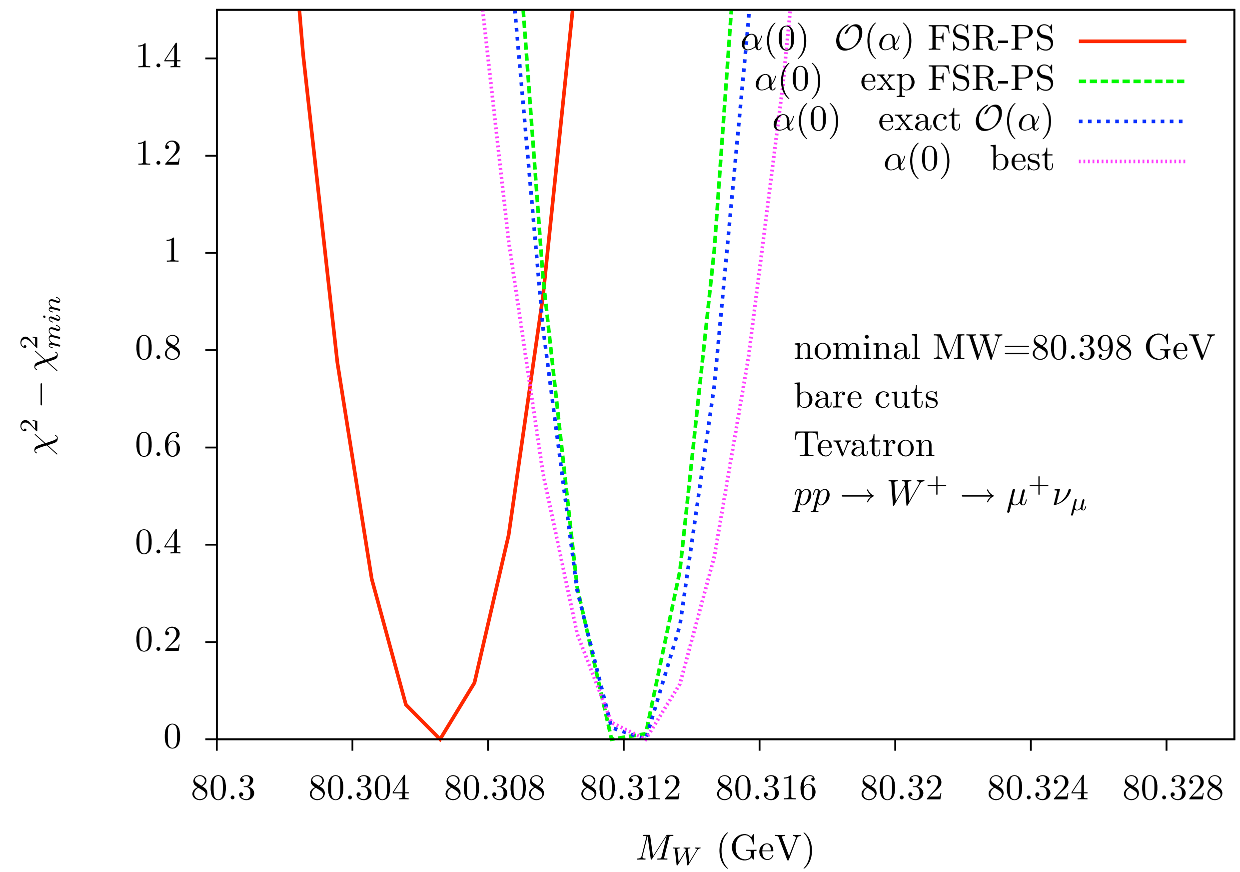
The exact matrix element at O(α)
and
O(α) FSR QED PS prediction
differ by +6 MeV (subleading EW)

The best matched results
O(α) + full QED Parton Shower
yields no shift (0 MeV)
w.r.t. the fixed order exact O(α)
(which is based on a different formula)
This results is true in the α_0 scheme



EW input schemes

$$\frac{G_\mu}{\sqrt{2}} = \frac{g^2}{8m_W^2}\left(1+\Delta r\right)$$

$$\begin{aligned}\alpha_\mu^{tree} &= \frac{\sqrt{2}}{\pi} G_\mu m_W^2 \sin^2\theta_W \\ \alpha_\mu^{1l} &= \frac{\sqrt{2}}{\pi} G_\mu m_W^2 \sin^2\theta_W \left(1-\Delta r\right)\end{aligned}$$

$$\begin{aligned}\alpha_0 \;:&\quad \sigma = \alpha_0^2\sigma_0 + \alpha_0^3(\sigma_{SV}+\sigma_H) \\ G_\mu\ I \;:&\quad \sigma = (\alpha_\mu^{tree})^2\sigma_0 + (\alpha_\mu^{tree})^2\alpha_0(\sigma_{SV}+\sigma_H) - 2\Delta r(\alpha_\mu^{tree})^2\sigma_0 \\ G_\mu\ II \;:&\quad \sigma = (\alpha_\mu^{1l})^2\sigma_0 + (\alpha_\mu^{1l})^2\alpha_0(\sigma_{SV}+\sigma_H)\end{aligned}$$

the three input schemes differ by $O(\alpha^2)$ terms

the change of scheme yields a different overall normalization
but also
the sharing of 0- and of 1-photon events is different in the 2 Gmu schemes
the same in α_0 and Gmu-II schemes

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the three input schemes differ by $O(\alpha^2)$ terms

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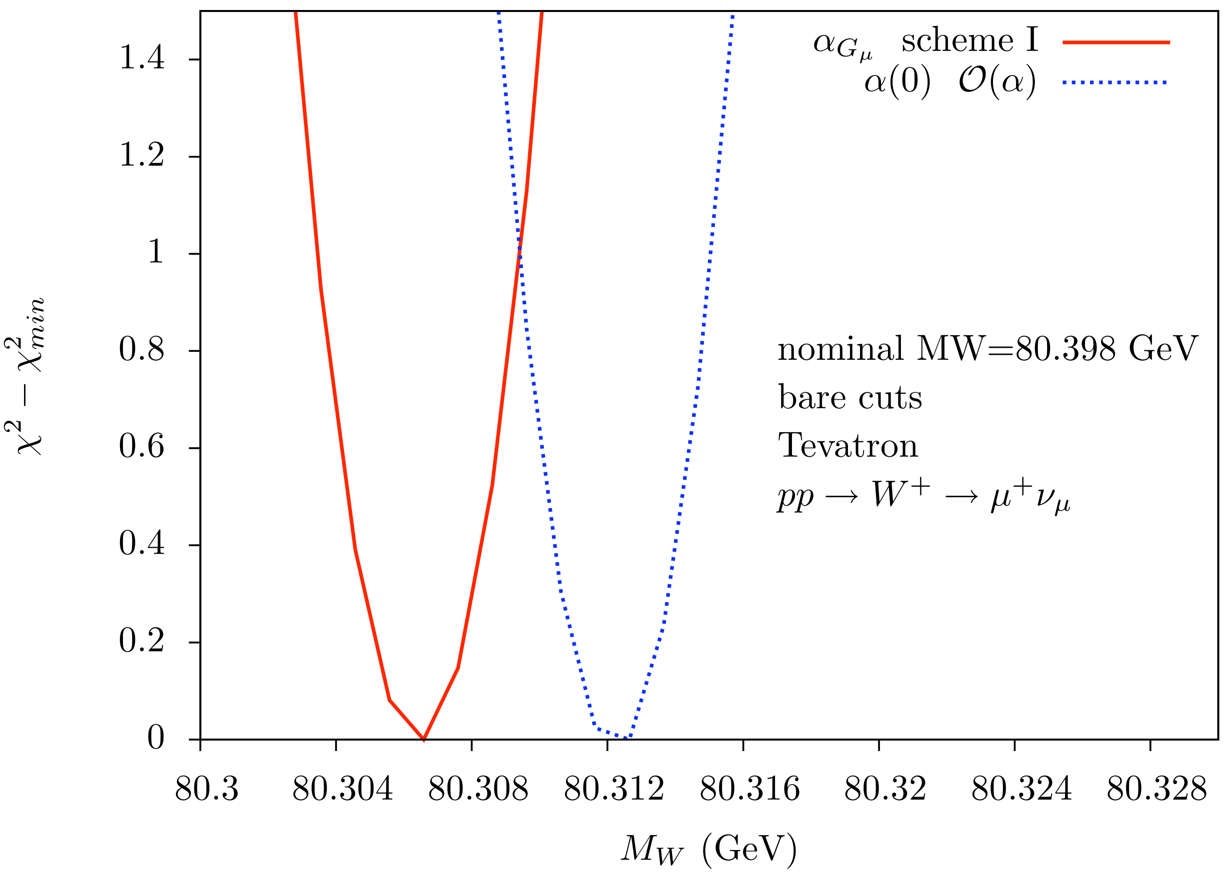
the same in α_0 and Gmu-II schemes

EW input schemes

Born templates with 10 billions of events: maximal accuracy 2 MeV



At O(α)

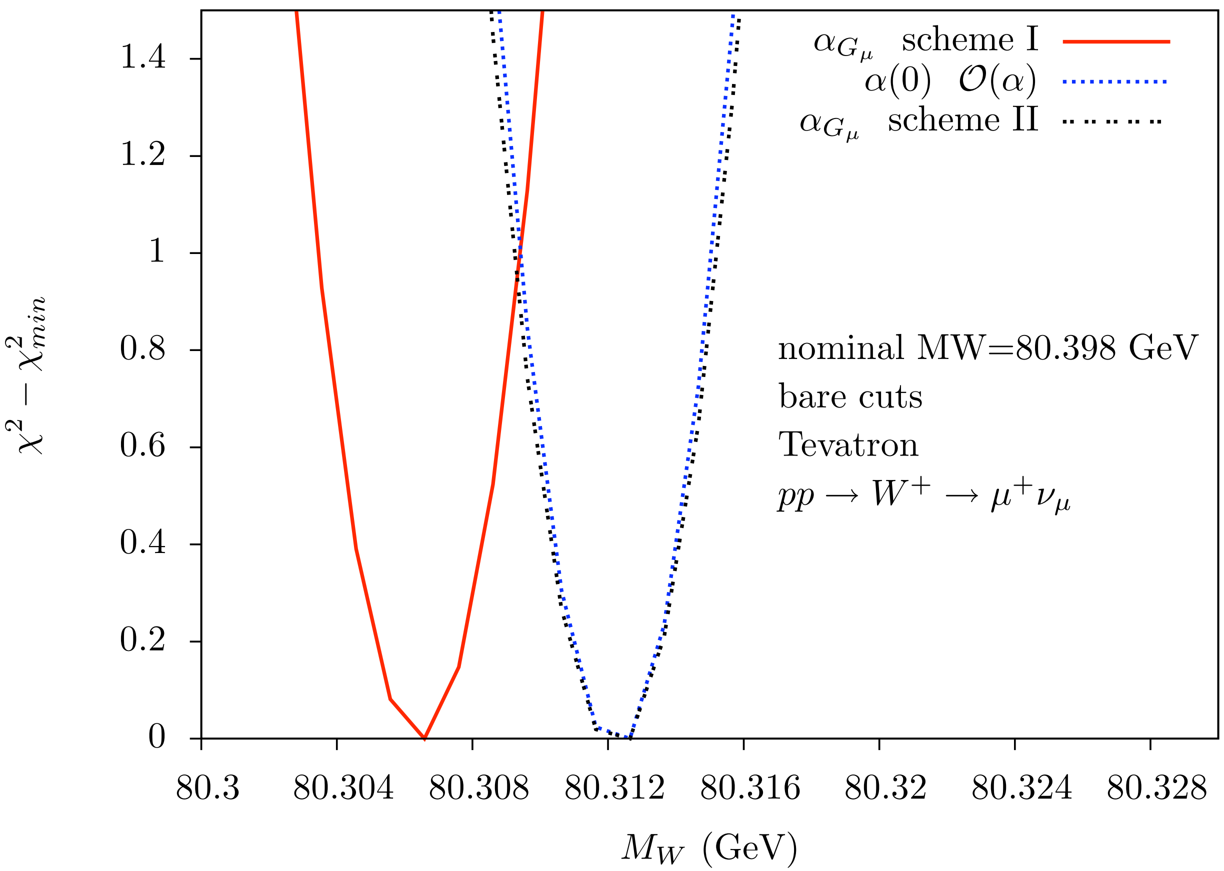
using α_0 or Gmu-I schemes

(different 0- and 1-photon sharing)

yields a change of MW of 6 MeV

EW input schemes

Born templates with 10 billions of events: maximal accuracy 2 MeV



At O(α)

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At O(α)

using α_0 or Gmu-II scheme

(same 0- and 1-photon sharing as α_0)

there is no extra shift in MW

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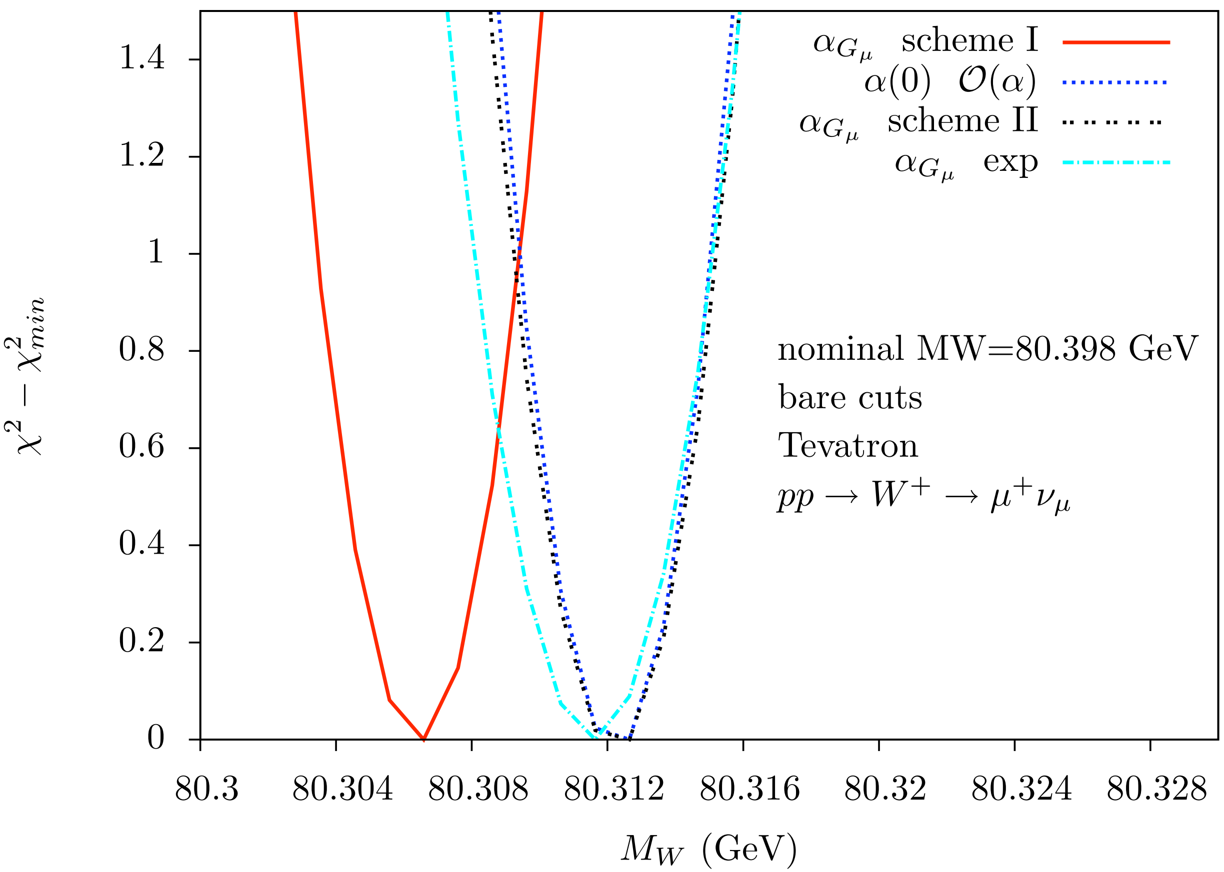

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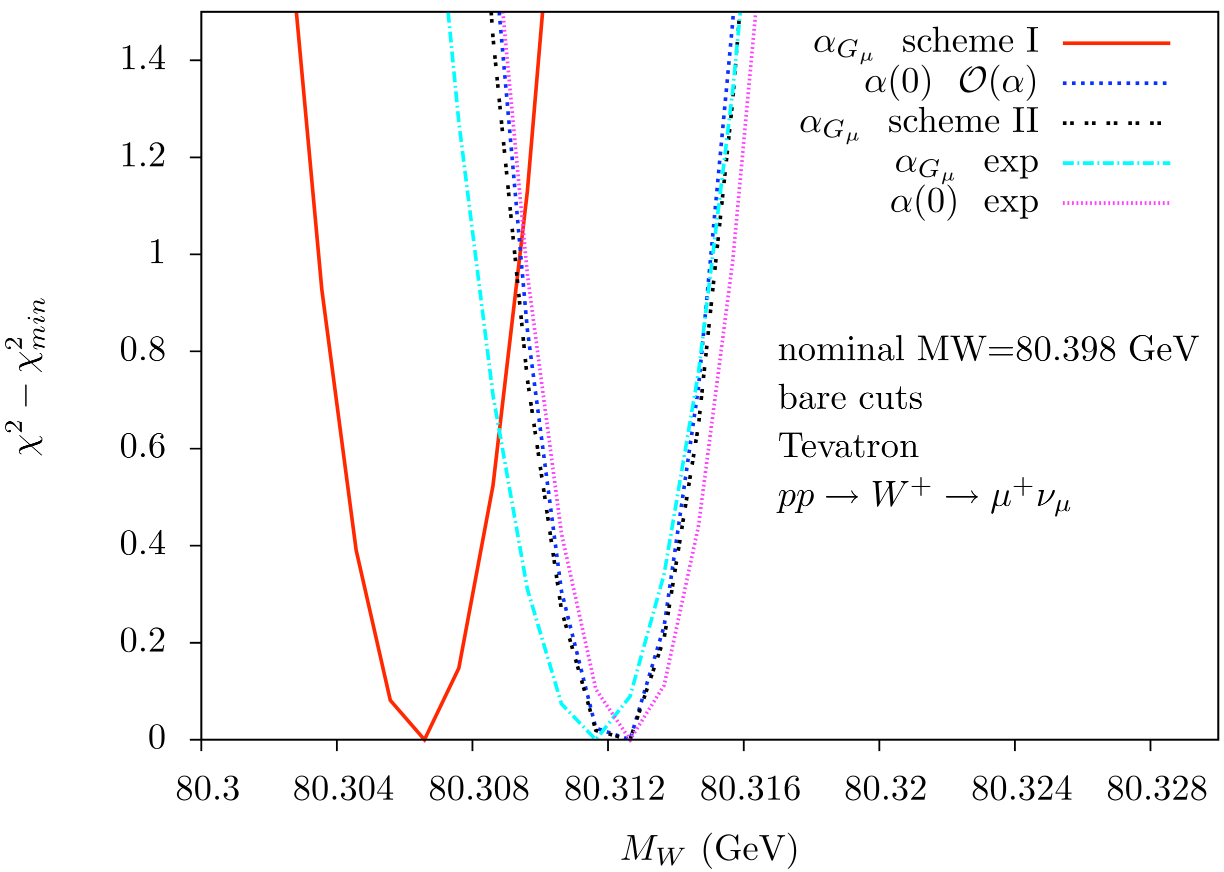
At O(α)
using α_0 or Gmu-II scheme
(same 0- and 1-photon sharing as α_0)
there is no extra shift in MW

In the Gmu-I scheme
O(α) and best approximation
differ by 5 MeV

EW input schemes

Born templates with 10 billions of events: maximal accuracy 2 MeV



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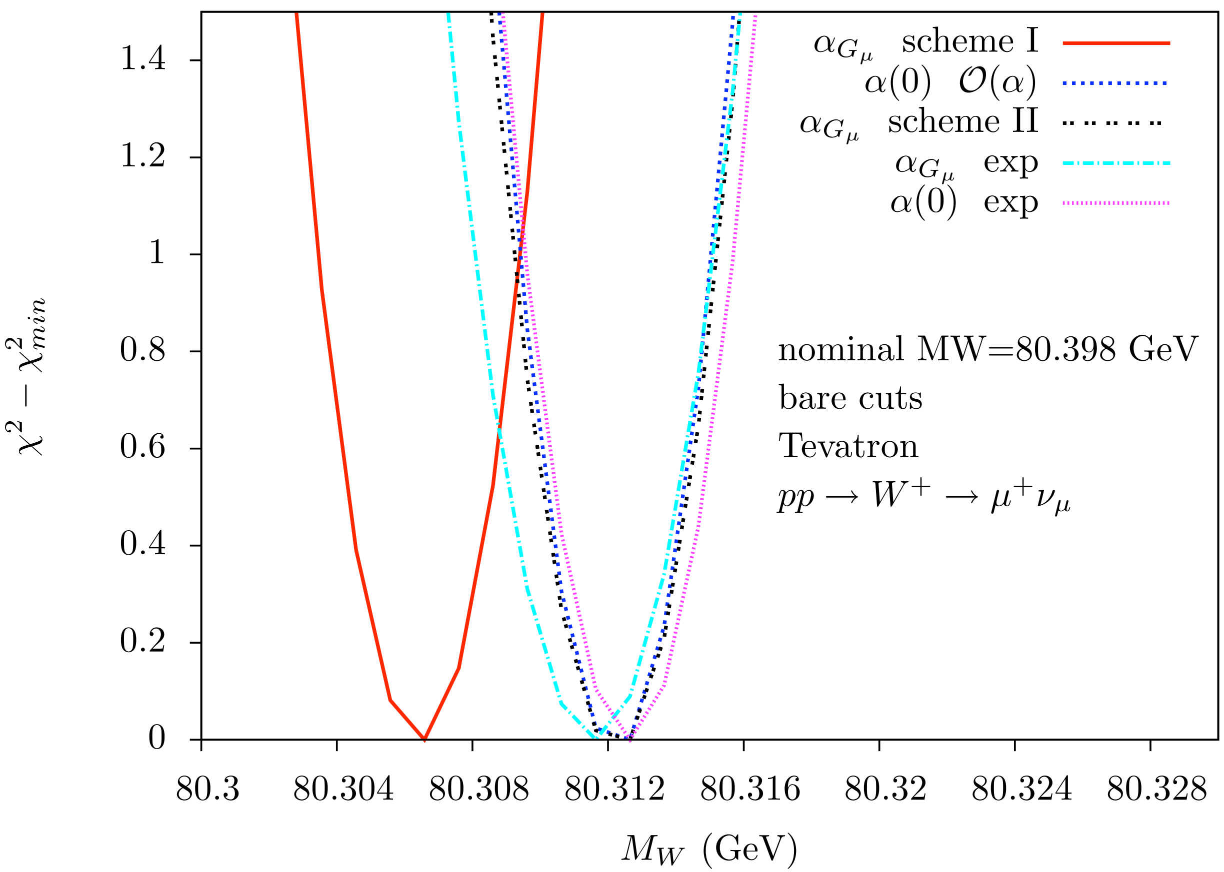
At O(α)
using α_0 or Gmu-II scheme
(same 0- and 1-photon sharing as α_0)
there is no extra shift in MW

In the Gmu-I scheme
O(α) and best approximation
differ by 5 MeV

In the best approximation
α_0 or Gmu-I schemes
differ by 2 MeV
(different normalization)

EW input schemes

Born templates with 10 billions of events: maximal accuracy 2 MeV



Good stability of the matched formula against scheme changes

Different schemes may yield at most a change of the χ^2 of the fit

At O(α)
using α_0 or Gmu-I schemes
(different 0- and 1-photon sharing)
yields a change of MW of 6 MeV

At O(α)
using α_0 or Gmu-II scheme
(same 0- and 1-photon sharing as α_0)
there is no extra shift in MW

In the Gmu-I scheme
O(α) and best approximation
differ by 5 MeV

In the best approximation
α_0 or Gmu-I schemes
differ by 2 MeV
(different normalization)

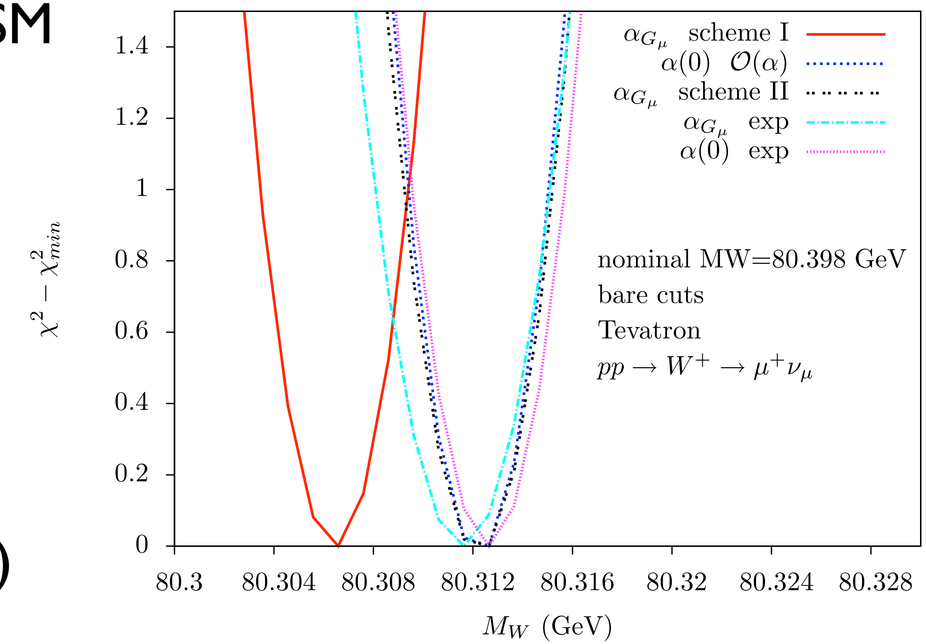
EW input schemes and MW beyond SM

With the SM templates, MW is measured in the SM

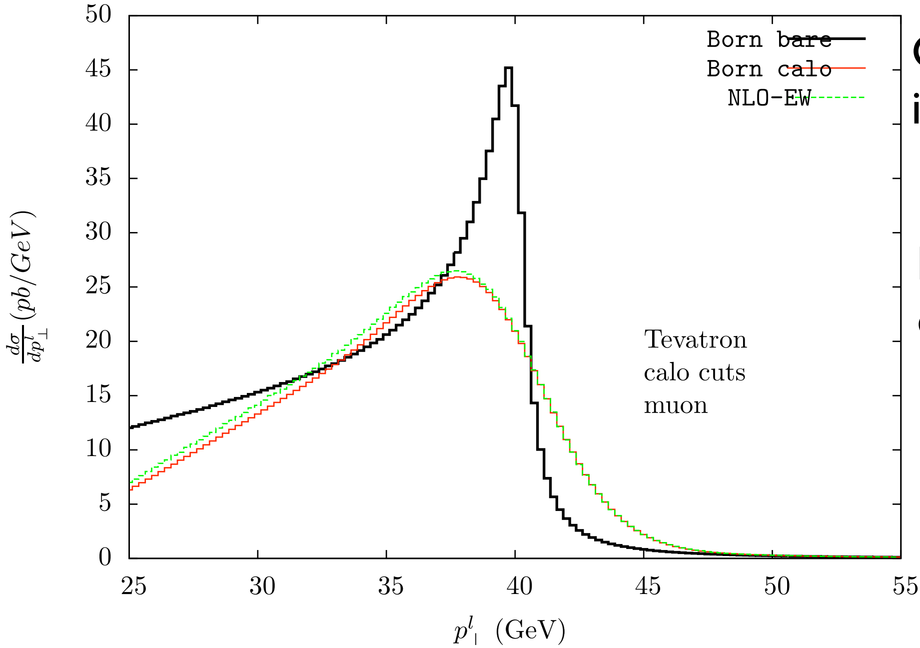
A measurement in the MSSM
could in principle yield different results

The difference between SM and MSSM
enters via Δr

The input scheme prescription (Gmu-I vs Gmu-II)
or the fixed order *vs* matched approximations
may or may not yield a different final result



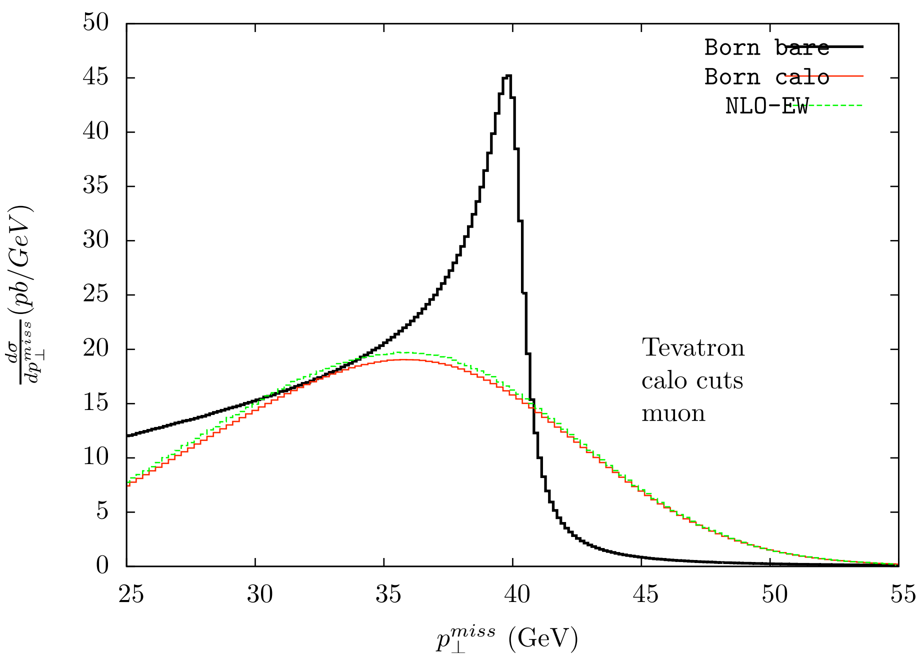
The effect of smearing the momenta and of photon recombination

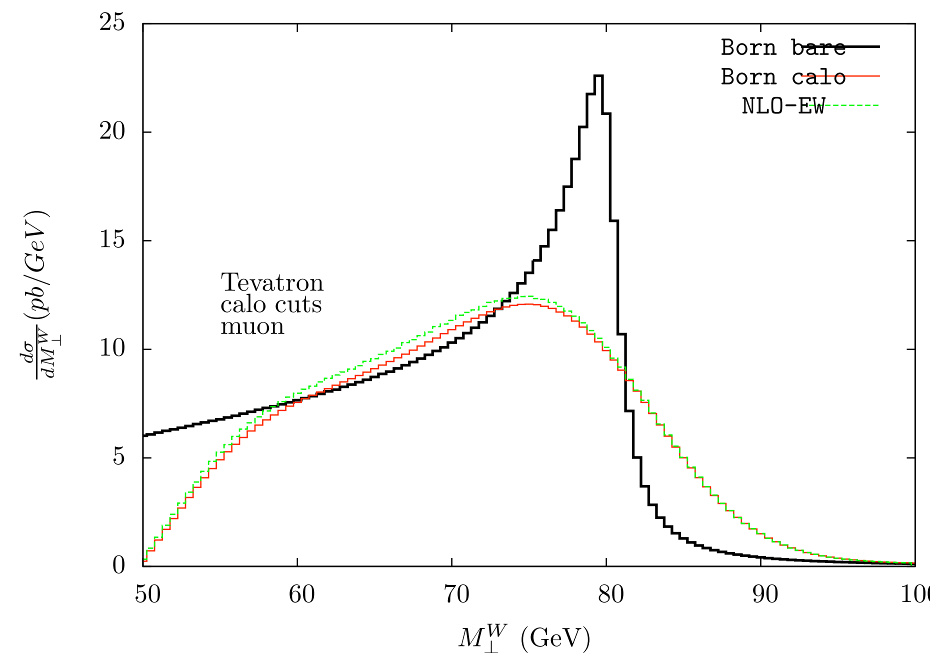


Calorimetric energy deposit
is not pointlike but approximated. by gaussian distribution
→ smearing of the lepton momenta

Photons "close" to the emitting lepton are hardly
disentangled: they are rather merged with the lepton
need to simulate these events by adding photon and
lepton momenta to yield an effective lepton
Effective partial KLN cancellation of FSR collinear logs

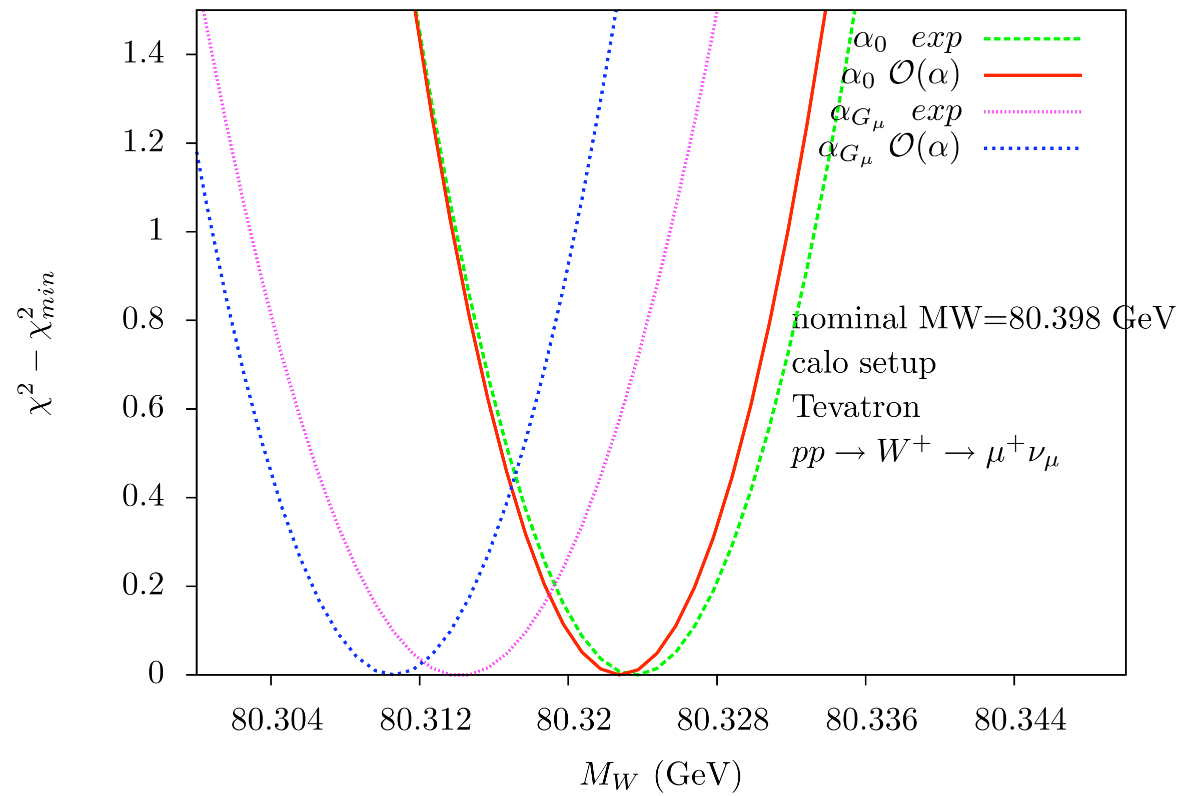
How do the effects of higher order corrections survive
after smearing + recombination?
Effects measured with smeared Born templates





EW corrections impact after smearing and recombination

calo Born templates with 1 billions of events: maximal accuracy 4 MeV
calo setup: smeared lepton momenta (at tree level no recombination)



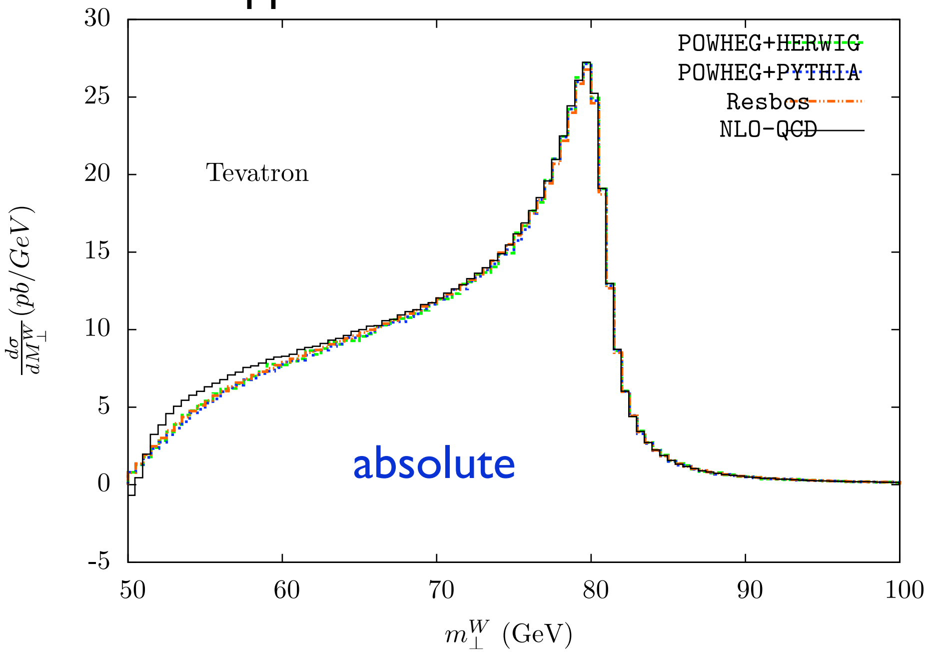
In the α_0, best w.r.t. fixed $O(\alpha)$ results differ by 1 MeV
In the Gmu-I scheme best w.r.t. fixed $O(\alpha)$ results differ by 4 MeV

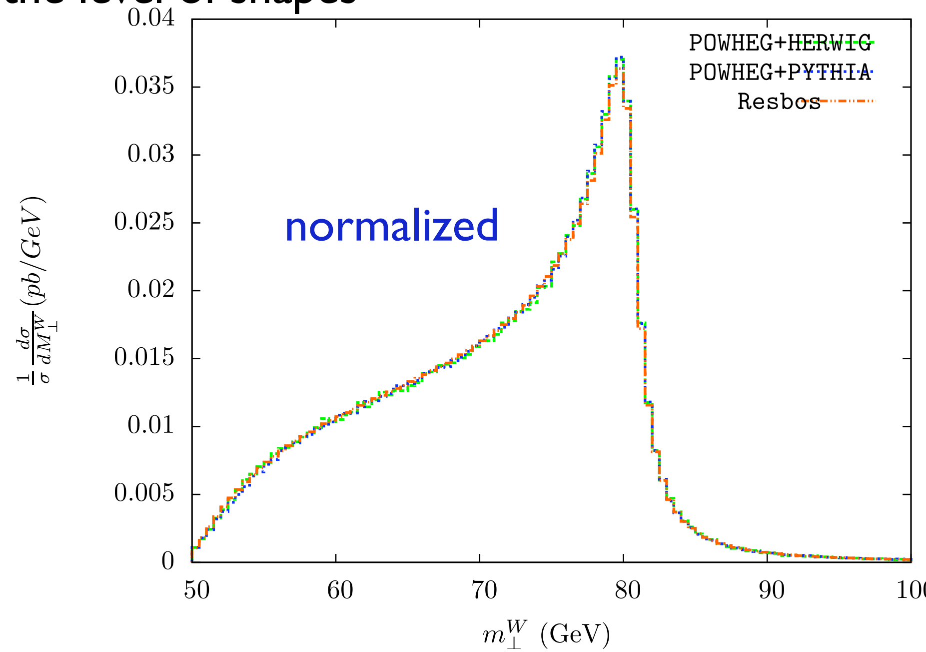
MW and QCD corrections: transverse mass

The perturbative and the non-perturbative content
of POWHEG+HERWIG and POWHEG+PYTHIA are different w.r.t. each other and w.r.t. to Resbos

They share NLO-QCD but differ in the inclusion of subleading higher-orders and in the matching of fixed order with resummed results

Differences appear at the level of normalization and at the level of shapes





Resbos templates: MW=80.398 GeV, 1 billions of calls: maximal accuracy 4 MeV

Fit with "absolute" templates (different normalizations w.r.t. pseudo-data)

POWHEG+HERWIG ΔMW = +18 MeV POWHEG+PYTHIA ΔMW = +18 MeV

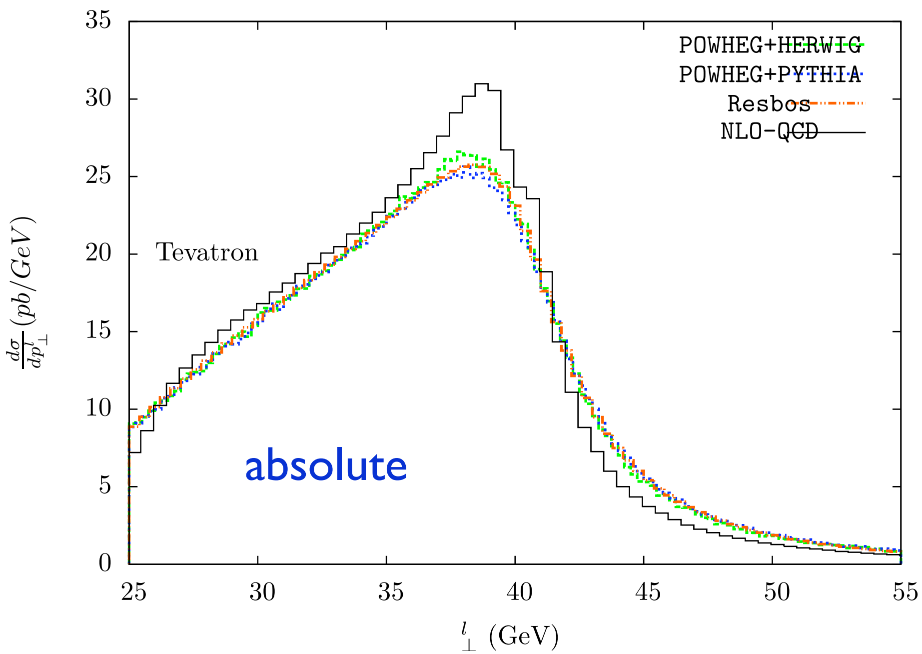
Fit with normalized distributions (templates and pseudo-data each normalized to its cross-section)

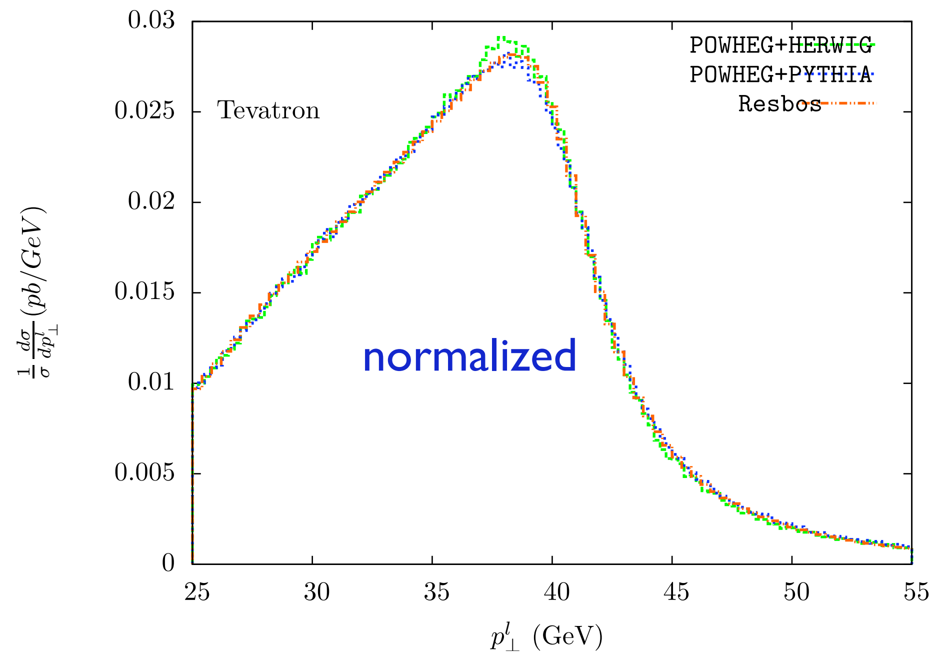
POWHEG+HERWIG ΔMW = + 18 MeV POWHEG+PYTHIA ΔMW = + 18 MeV

Weak sensitivity to the details of multiple gluon radiation

MW and QCD corrections: lepton transverse momentum

The lepton transverse momentum distribution is sensitive to the details of multiple gluon emission (i.e. to the gauge boson transverse momentum)





Resbos templates: MW=80.398 GeV, 1 billions of calls: maximal accuracy 4 MeV

Fit with "absolute" templates (different normalizations w.r.t. pseudo-data)

POWHEG+HERWIG ΔMW = - 48 MeV POWHEG+PYTHIA ΔMW = - 6 MeV

Strong sensitivity to the precise normalization (role of PDFs and choice of non-pert. params)

Fit with normalized distributions (templates and pseudo-data each normalized to its cross-section)

POWHEG+HERWIG ΔMW ~ - 50 MeV POWHEG+PYTHIA ΔMW ~ +46 MeV

PDF uncertainty: Hessian vs Montecarlo approaches

Hessian (CTEQ, MSTW)

For each of the 5 values compute the *pdf* spread (not necessarily symmetric)

$$(\Delta F^{\alpha_S}_{\rm PDF})_+ = \sqrt{\sum_{k=1}^{n} \{\max\left[\, F^{\alpha_S}(S_k^+) - F^{\alpha_S}(S_0),\ F^{\alpha_S}(S_k^-) - F^{\alpha_S}(S_0),\ 0\right]\}^2},$$

$$(\Delta F^{\alpha_S}_{\rm PDF})_- = \sqrt{\sum_{k=1}^{n} \{\max\left[\, F^{\alpha_S}(S_0) - F^{\alpha_S}(S_k^+),\ F^{\alpha_S}(S_0) - F^{\alpha_S}(S_k^-),\ 0\right]\}^2},$$

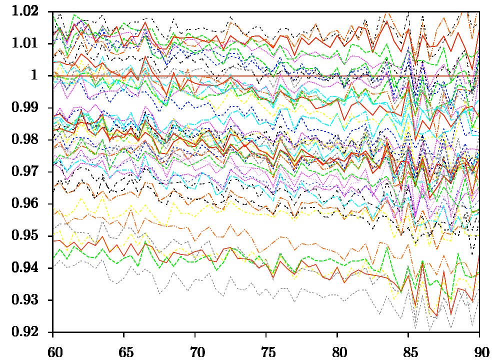
With these Δs one builds a band for the (e.g. transv. mass) distribution
but it is difficult to derive an interval of allowed values for MW

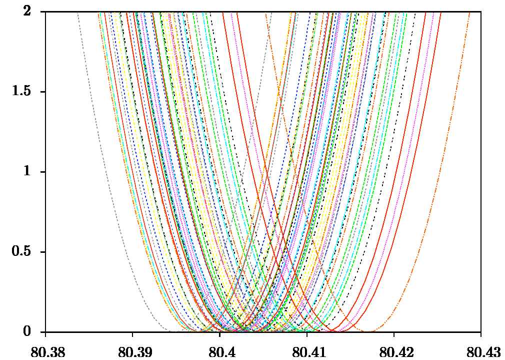
Montecarlo (NNPDF)

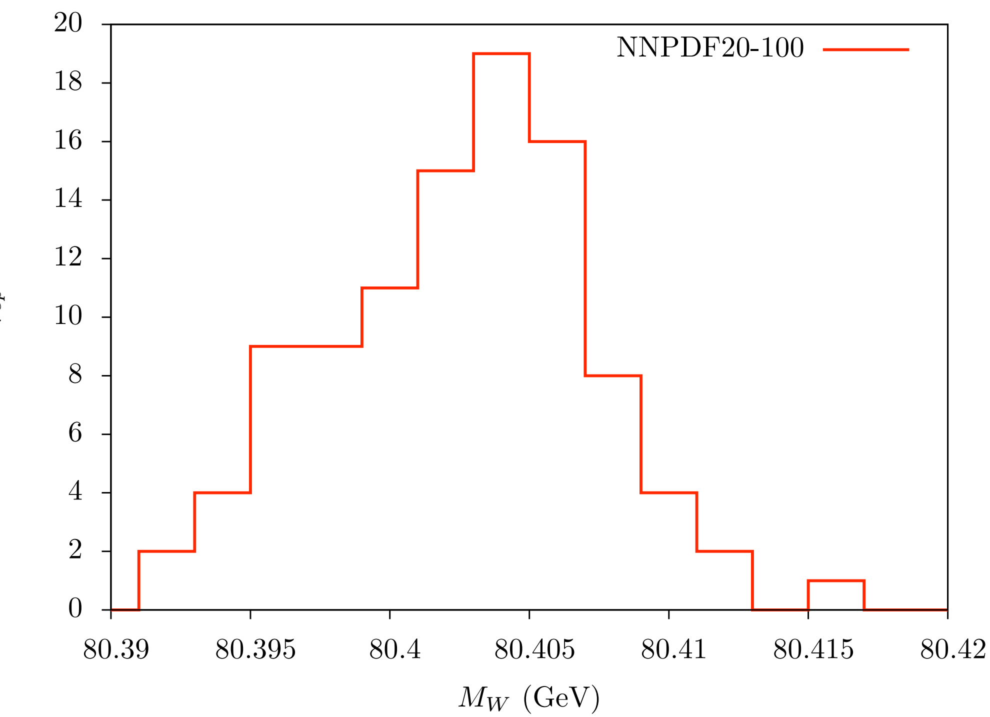
$$\sigma_{\mathcal{F}} = \left(\frac{1}{N_{\rm set}-1} \sum_{k=1}^{N_{\rm set}} \left(\mathcal{F}[\{q^{(k)}\}] - \langle \mathcal{F}[\{q\}] \rangle \right)^2 \right)^{1/2}$$

Average and standard deviation of any observable are derived by computing N times its distributions, each time with a different replica.
Since each replica is a representative of the ensemble of allowed (from the data) proton parametrizations we can fit the transverse mass distribution and obtain the corresponding preferred MW

PDF uncertainty: HORACE Born with NNPDF20_100







The transverse mass distribution computed with different replicas have differents shapes and normalizations

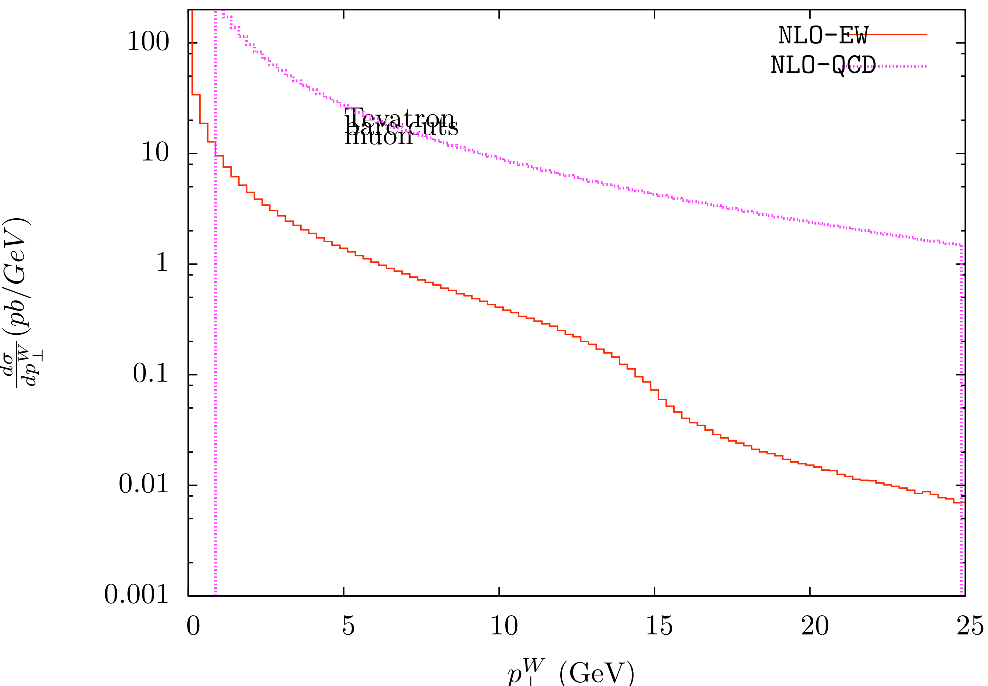
They have been fitted with (HORACE with CTEQ66) templates

The corresponding preferred MW are different

The distribution of the 100 MW values yields
MW = 80.402 +- 0.005 GeV

The choice of the PDF set and of the non pert. parameters to describe soft gluon radiation are correlated

QED induced W(Z) transverse momentum

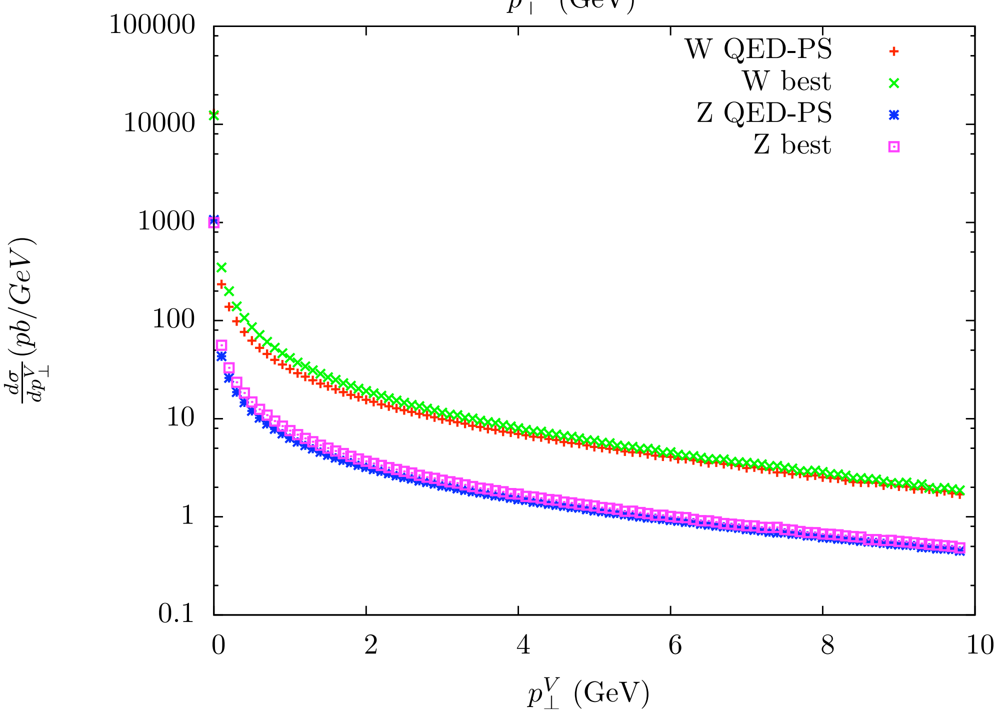


The uncertainty on ptW directly translates into an uncertainty on the final MW value.

Photon radiation yields a tiny gauge boson transverse momentum.

This momentum is different in the CC and NC channels because of the different flavor structure.

The "non-final state" component differs in the 2 cases by 54 (Z) - 33 (W) = 21 MeV



$$\langle p_\perp^V \rangle = $$

Z	FSR-PS	0.409	GeV
Z	best	0.463	GeV
W	FSR-PS	0.174	GeV
W	best	0.207	GeV

The fit of the non perturbative QCD parameters is done on the Z transverse momentum and it is necessary to properly remove the EW corrections to the NC channel

In the simulation of the CC channel the relevant EW corrections are then applied

Combining QCD + EW corrections

G. Balossini, C.M.Carloni Calame, G.Montagna, M.Moretti, O.Nicrosini, F.Piccinini, M.Treccani, A.Vicini, JHEP 1001:013, 2010

factorized prescription

$$\left[\frac{d\sigma}{d\mathcal{O}}\right]_{QCD\otimes EW} = \left(1+\frac{\left[\frac{d\sigma}{d\mathcal{O}}\right]_{MC@NLO}-\left[\frac{d\sigma}{d\mathcal{O}}\right]_{HERWIG\ PS}}{\left[\frac{d\sigma}{d\mathcal{O}}\right]_{LO/NLO}}\right)\times\left\{\left[\frac{d\sigma}{d\mathcal{O}}\right]_{EW}\right\}_{HERWIG\ PS}$$

additive prescription

$$\left[\frac{d\sigma}{d\mathcal{O}}\right]_{QCD\oplus EW} = \left\{\frac{d\sigma}{d\mathcal{O}}\right\}_{QCD} + \left\{\left[\frac{d\sigma}{d\mathcal{O}}\right]_{EW} - \left[\frac{d\sigma}{d\mathcal{O}}\right]_{Born}\right\}_{HERWIG\ PS}$$

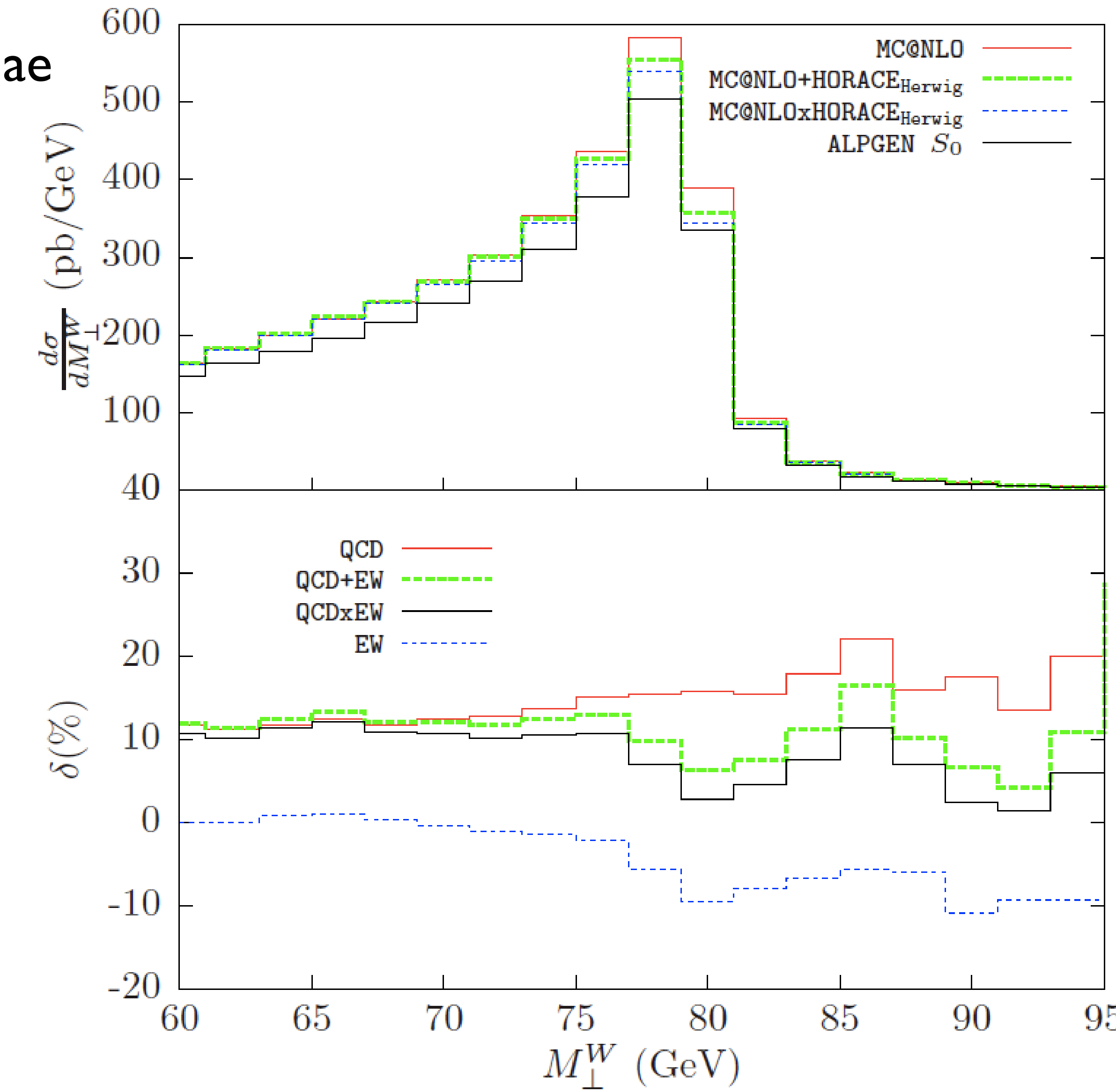
- different inclusion of higher orders $\mathcal{O}(\alpha_s^2)$ and $\mathcal{O}(\alpha\alpha_s)$

the factorized prescription includes the bulk of the reducible $\mathcal{O}(\alpha_s^2)$ terms

Combining QCD + EW corrections

- the factorized and the additive formulae differ by few per cent

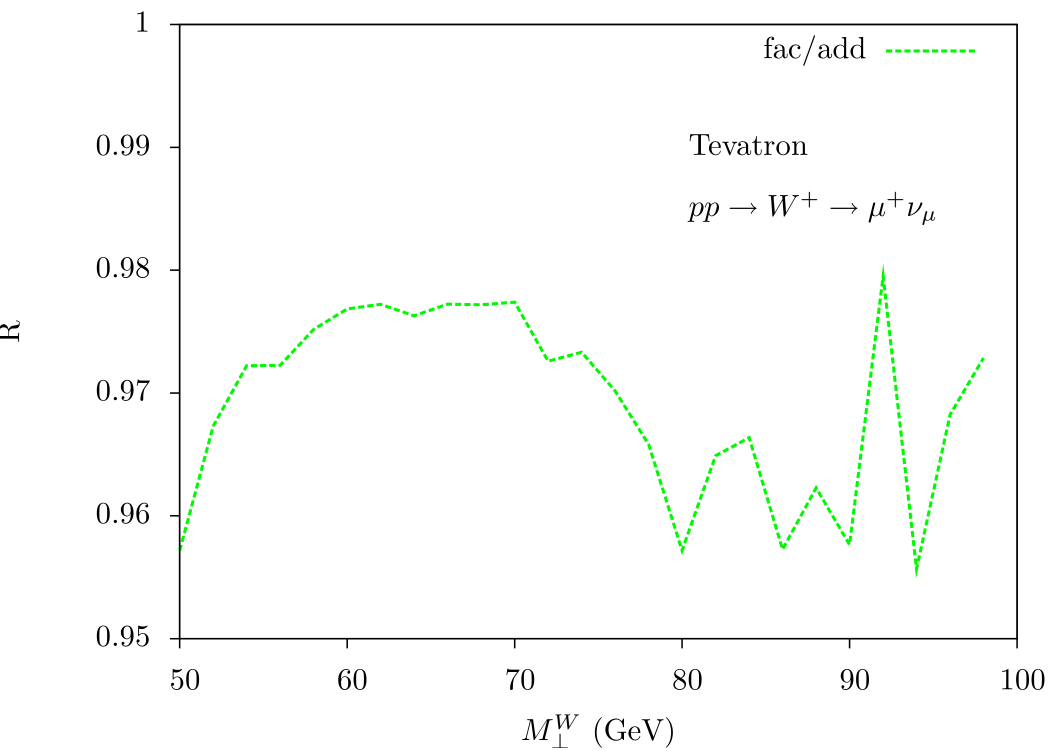
- different inclusion of higher orders
  $\mathcal{O}(\alpha_s^2)$ and $\mathcal{O}(\alpha\alpha_s)$

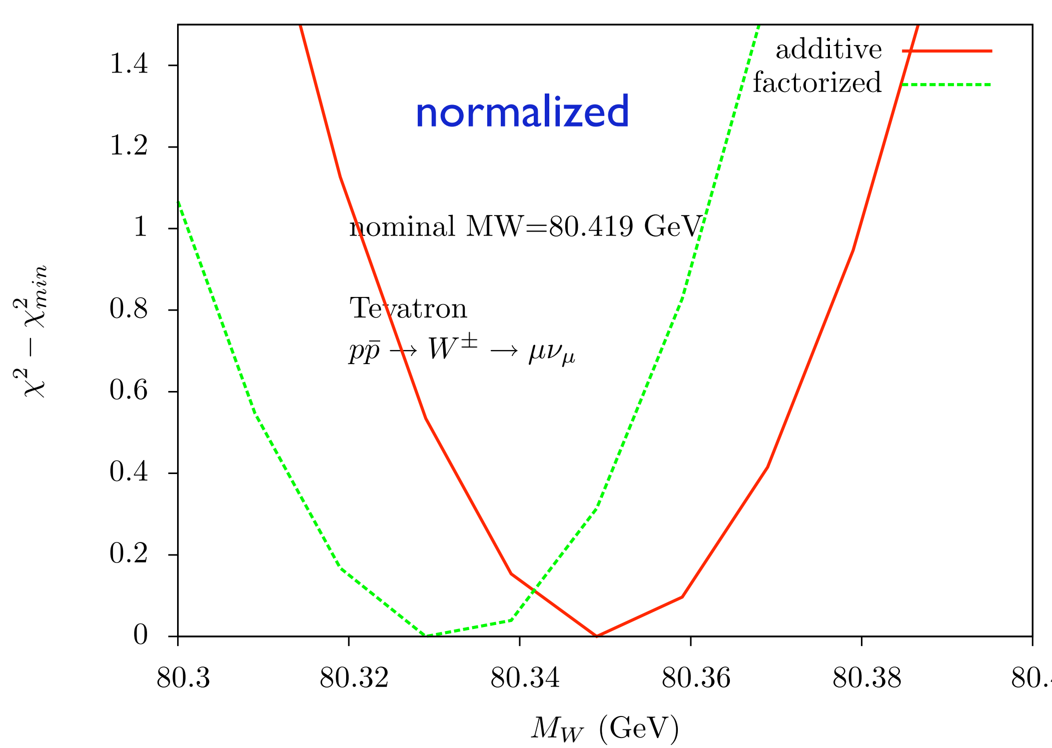


- additive prescription: NLO-EW convoluted with HERWIG QCD-PS
- factorized prescription: NLO-EW convoluted with HERWIG QCD-PS + + NLO-EW times (non-log NLO-QCD)

Combining QCD + EW corrections

templates: Resbos, same inputs of the pseudo-data: MW=80.419 GeV,   GammaW=2.048 GeV





- in the ratio we observe an offset, mostly due to higher order QCD corrections, and a different shape
- the bulk of the shift is due to EW corrections
- the different recipes can be translated into a relative MW shift of ~20 MeV ? (low statistics)

Summary

Many calculations and many codes available: crucial is the tuning phase

the template fit procedure has been implemented to study
EW corrections (bare and calo Born templates)
QCD and QCD+EW corrections (Resbos templates)

in the EW sector we can classify, in terms of MW shifts
the impact of different perturbative approximations and of theoretical ambiguities:
missing higher orders or different scheme choices induce tiny changes of MW
the factorized HORACE formula exhibits a good stability
exact O(α) matched with multiple photon is needed e.g. to precisely determine pt_W

in the QCD sector we can, in principle, compare how different "best predictions"
(perturbative approximations + matching procedures + (soft+non-pert. models))
differ in terms of MW
In practice, a dedicated work of tuning of soft+non.pert. models is required
before one can attempt to make an estimate of the QCD theoretical uncertainty

two recipes to combine QCD+EW corrections induce differences in MW of O(20 MeV)
(although mostly factorized recipes are presently used)

the PDF uncertainty "alone" induces an uncertainty of +- 5 MeV (68% C.L.)
but there is an interplay with the non-pert. parameters

Work in progress in the framework of the W mass workshop

The Z transverse momentum distribution and the W observables

- modeling of soft gluon and non-perturbative effects
  in the Z production case

- extrapolation of this model to the W kinematical region:
  the W transverse momentum distribution is the
  theoretical observable for comparisons

- use of a Montecarlo simulation
  based on the two above ingredients
  to predict in the W case: lepton transverse momentum
  transverse missing momentum
  transverse mass

- a definite improvement has to be obtained in step 1
  (fit of Z observables)
  before any sensible comparison is carried on