Test Stand Status

Sebastian Vazquez-Torres
Ron Belmont
Jamie Nagle

University of Colorado, Boulder

October 20th, 2015

Cosmics

Some data about polystyrene (scintillator base material)

Z/A	0.53768 mol g^{-1}
Density ρ	1.060 g cm^{-3}
Nuclear interaction length λ_I	77.1 cm
Radiation length X_0	41.31 cm
Mean excitation energy I	68.7 eV
Minimum ionization energy $dE/dx\|_{min}$	2.025 MeV/cm

Cosmics

What about the Bethe formula?

$$-\left\langle \frac{dE}{dx} \right\rangle = \rho K \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln \frac{2 m_e c^2 \beta^2 \gamma^2 T_{max}}{I^2} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right]$$

- $K = 4\pi N_A r_e^2 m_e c^2 = 0.307075$ MeV mol^{-1} cm^2
- $T_{max} = 2 m_e c^2 \beta^2 \gamma^2 / [1 + 2\gamma m_e / M + (m_e/M)^2]$ is the highest kinetic energy that can be imparted to a free electron in a single collision by a particle with mass M
- The $\delta(\beta\gamma)$ can be calculated based on Sternheimer et al, Phys. Rev. B 26, 6067 (1982)—note that in their convention the correction doesn't have the factor 1/2
  $X = \log_{10} \beta\gamma$
  $X < X_0 \rightarrow \delta(X) = 0$
  $X_0 < X < X_1 \rightarrow \delta(X) = 4.6052X + a(X_1 - X)^m + C$
  $X_1 < X \rightarrow \delta(X) = 4.6052X + C$
  where X_0, X_1, a, m, and C are material-specific constants
- Minimum ionizing energy for muon is 318 MeV, using this we obtain $\langle dE/dx \rangle =$ 2.036 MeV/cm, which is quite close to the 2.025 MeV/cm from the data table

Cosmics

Generally we consider the distribution of energies to be a Landau
The Landau distribution is defined by

$$f(\lambda) = \frac{1}{2\pi i} \int_{c+i\infty}^{c+i\infty} e^{s \ln s + \lambda s} ds$$

due to the long tail, the moments are undefined.

However, as derived in J. E. Moyal, Phil. Mag. 46 (1955) 263, the Landau distribution can be well approximated by

$$f(\lambda) = \frac{1}{\sqrt{2\pi}} e^{-\lambda + e^{-\lambda}}$$

which later became known as the Gumbel distribution.
The moments of the Gumbel distribution are defined: for $\lambda = (x - \mu)/\sigma$, the mode (MPV) is μ and the mean is $\mu + \gamma_E \sigma$ (where $\gamma_E \approx 0.577216$ is the Euler-Mascheroni constant)

Cosmics

For energy loss in a material, we can write the energy loss distribution as

$$\Delta E = \frac{1}{\sqrt{2\pi}} e^{-\lambda + e^{-\lambda}}$$

where the independent variable λ is

$$\lambda = \frac{\Delta E - [\Delta E]_{MPV}}{\xi}$$

the width parameter ξ is

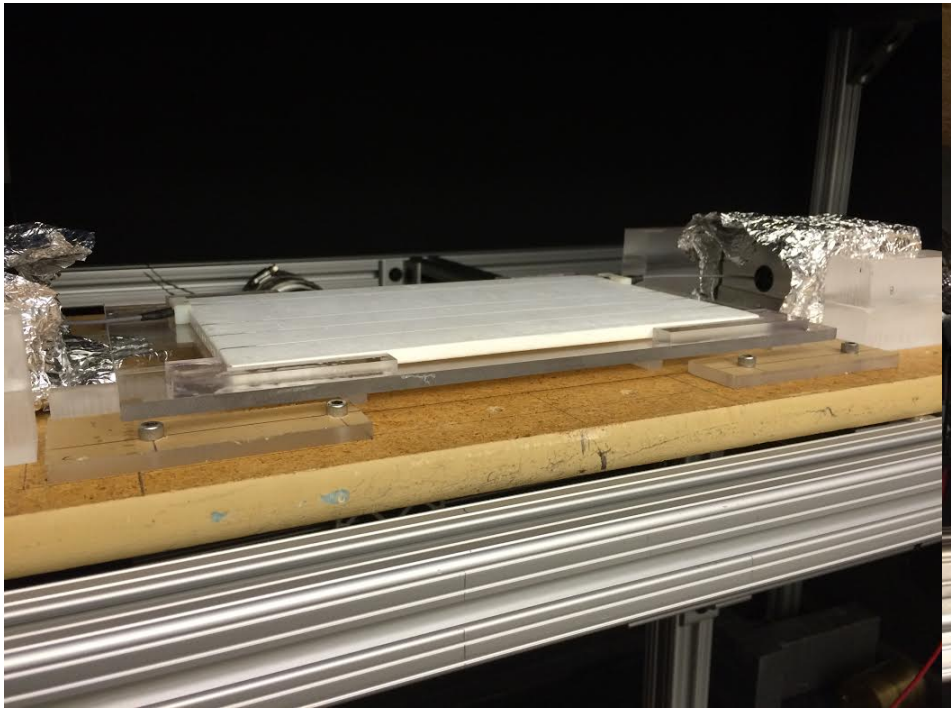
$$\xi = \frac{K}{2} \frac{Z}{A} \frac{1}{\beta^2} \rho \Delta x$$

and the most probable value of the energy loss can be determined by a modified Bethe formula

$$[\Delta E]_{MPV} = \xi \left[\ln \frac{2 m_e c^2 \beta^2 \gamma^2 \xi}{I^2} - \beta^2 + 1 - \gamma_E \right]$$

Cosmics

Some photographs of the cosmics set up



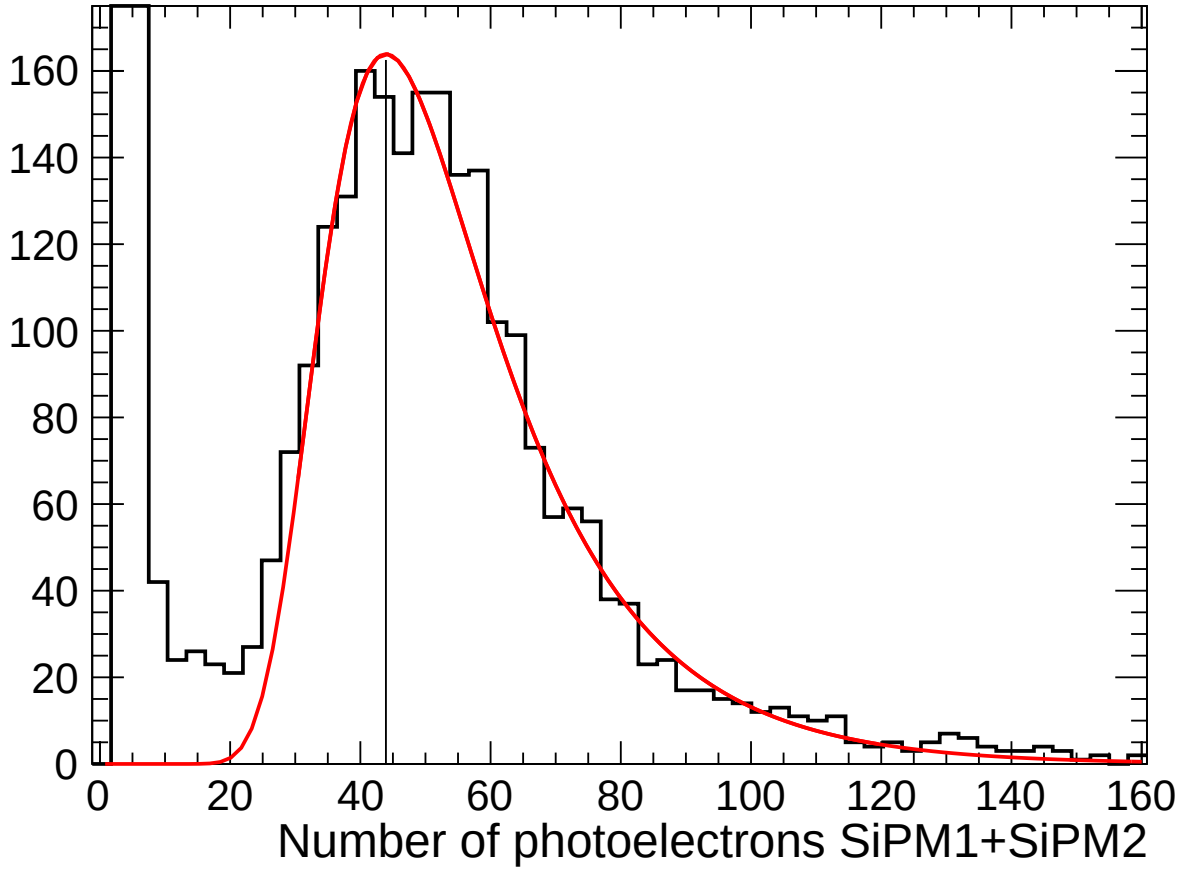
We have both phototubes under the table so that source/LED scans can be run without total deconstruction
We have the upper tube as close to the panel as possible to minimize the fraction of particles that trigger both tubes but miss the panel

Cosmics

A little about the geometry...

- The two phototubes are separated by about 3.25", each having 0.25" thickness, and each has a 1" $\times$ 1" scintillator
- The maximum angle off-normal is $\theta_{max} = \tan^{-1}(3.75/\sqrt{2}) \approx 0.361 \approx 20.7^\circ$
- The pathlength L is related to the thickness Δx by $L = \Delta x \sec\theta$, meaning $L_{max} = \Delta x \sec\theta_{max} \approx 1.07\Delta x$
- Panel thickness 0.300" $= 0.762$ cm
- If we ignore the 7% possible deviation in pathlength, for MIP we get $[\Delta E]_{MPV} =$ 1.37 MeV and $\xi = 0.0750$ MeV
- However, since we know the angular distribution of cosmics is $\propto \cos^2\theta$, we can compute a weighted average for the angle, $\theta_{ave} = 0.173$, yielding average pathlength $L_{ave} = 1.02\Delta x = 0.777$ cm
- Using that, we get $[\Delta E]_{MPV} = 1.39$ MeV and $\xi = 0.0765$ MeV

Cosmics

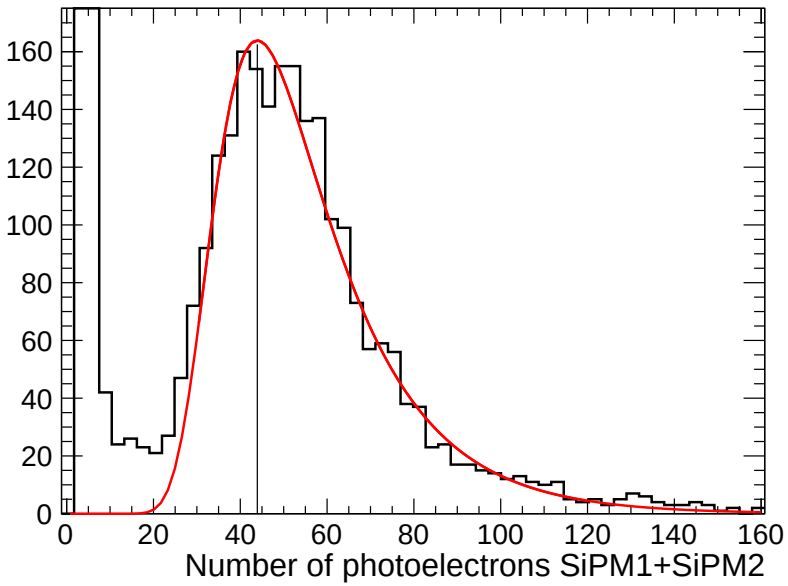


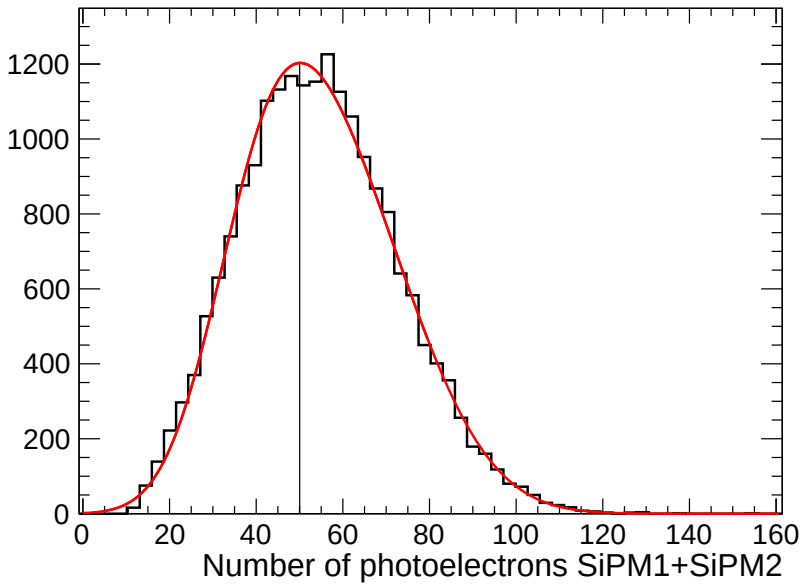
$[\Delta E]_{MPV} = 43.9 \pm 0.5$ photoelectrons and $\xi = 9.3 \pm 0.2$ photoelectrons
$[\Delta E]_{MPV} = 1.39$ MeV (from the previous slide) implies a conversion of 31.6 pe/MeV

Cosmics and Source

What can we learn by comparing the distribution from the Strontium-90 source to the cosmics?

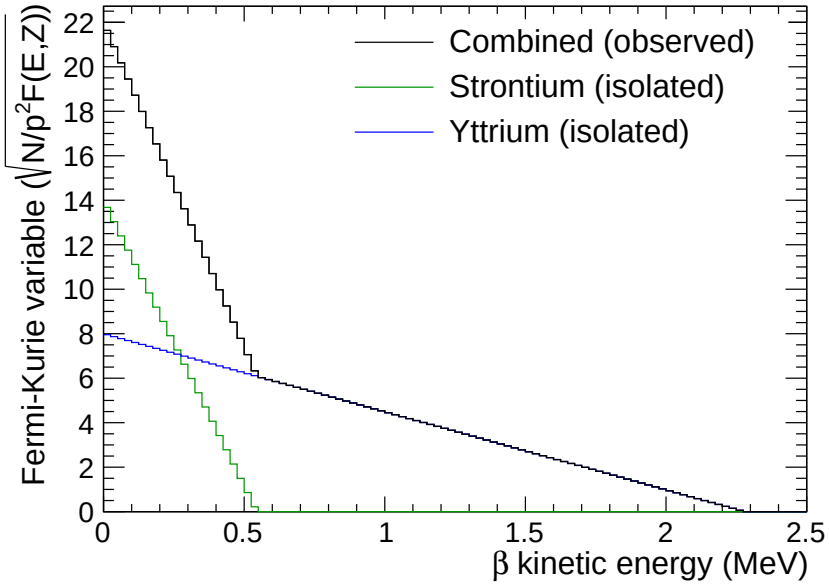
Cosmics and Source

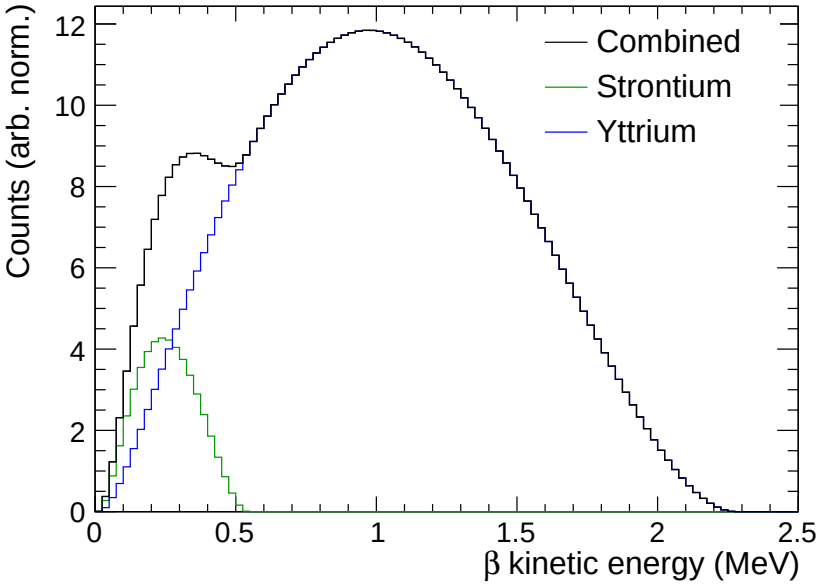




Source

What does the Strontium source spectrum look like?

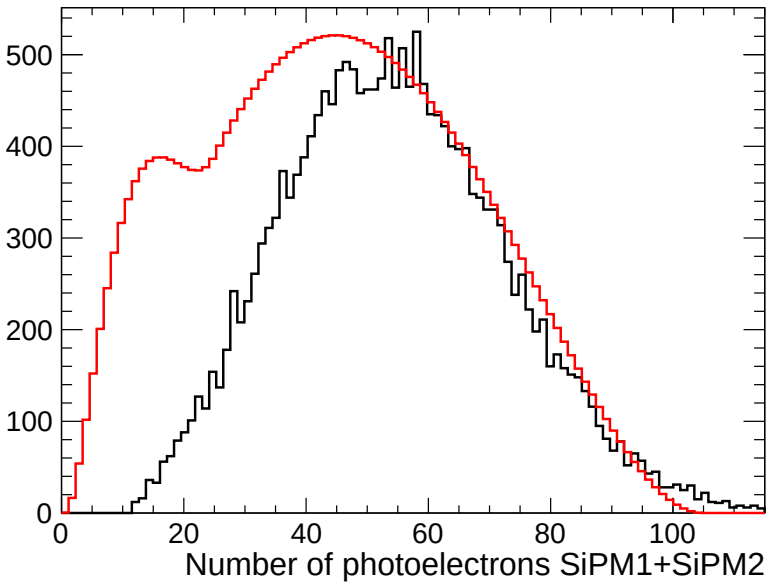


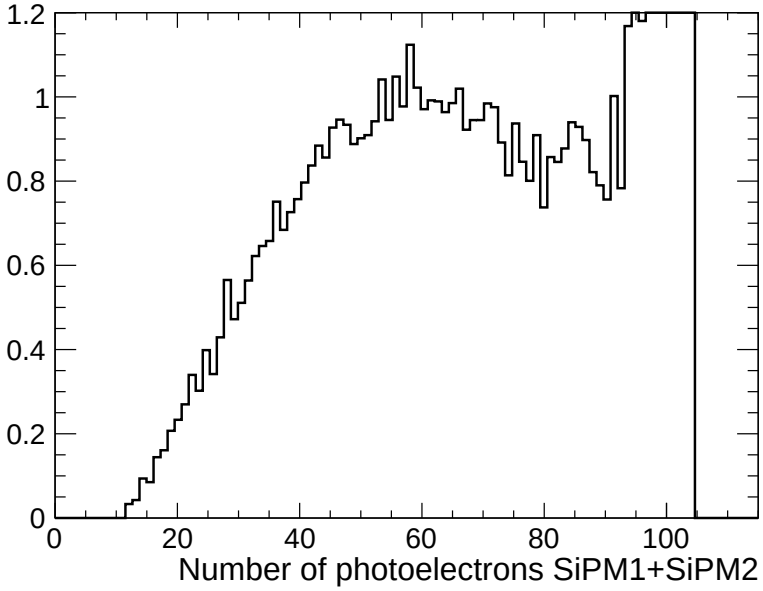


Data from W. E. Meyerhof, Phys. Rev. 74 (1948) 263

Source

Overlay of the source spectrum with measured distribution





There seems to be some inefficiency at low energies, and the ratio resembles a turn-on curve—further investigation is needed

Reminder: we use the SiPMs to self-trigger on the source, so there's an inherent low energy cut-off

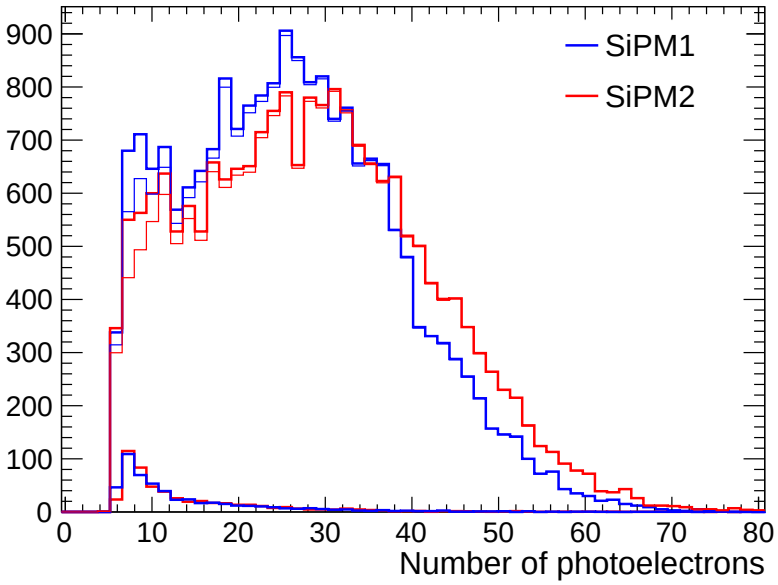
Brief summary

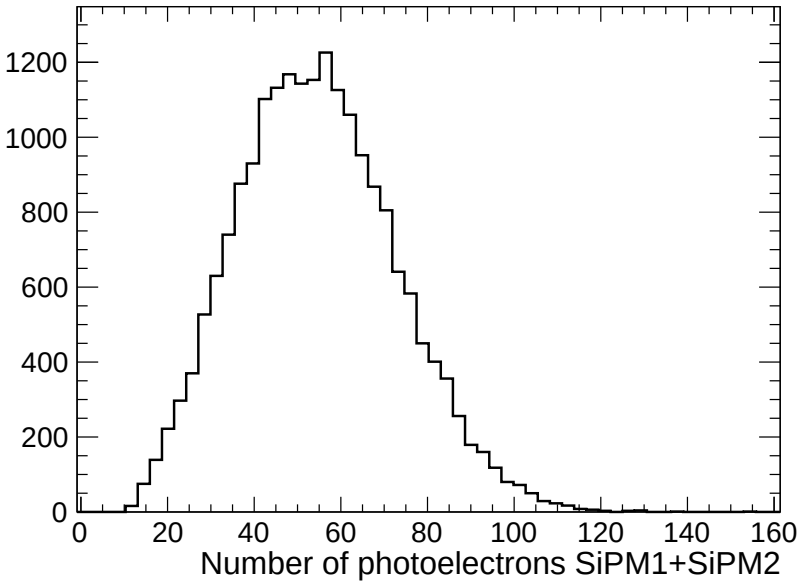
- **Cosmics have been measured with a mean of 43.9 pe and a with of 9.3 pe, with an implied conversion of 31.6 pe/MeV**
- **We are prepared and able to cosmics measurements as soon as we get the full size tiles from BNL**
- **We are seeking input to going further using cosmics to characterize the energy deposited in the tile**
- We can also do an LED scan as soon as we receive them—we plan to do LED scans with the tile inverted, i.e. facing away from the LED so that light going directly into the fiber isn't an issue
- It may also be possible to use the Strontium-90 source to calibrate the energy, though further investigation is needed
- The sampling of the light in the fiber relative to the total light produced may be an important additional consideration

Extra material

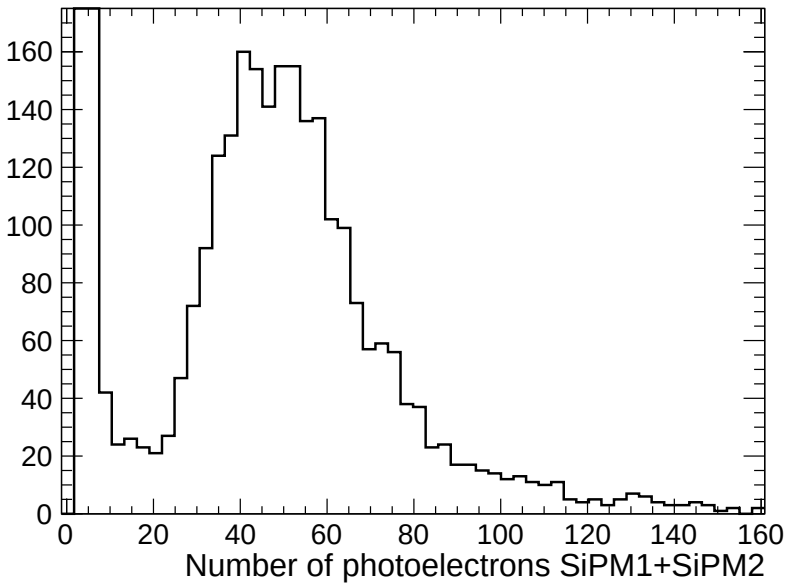
Source

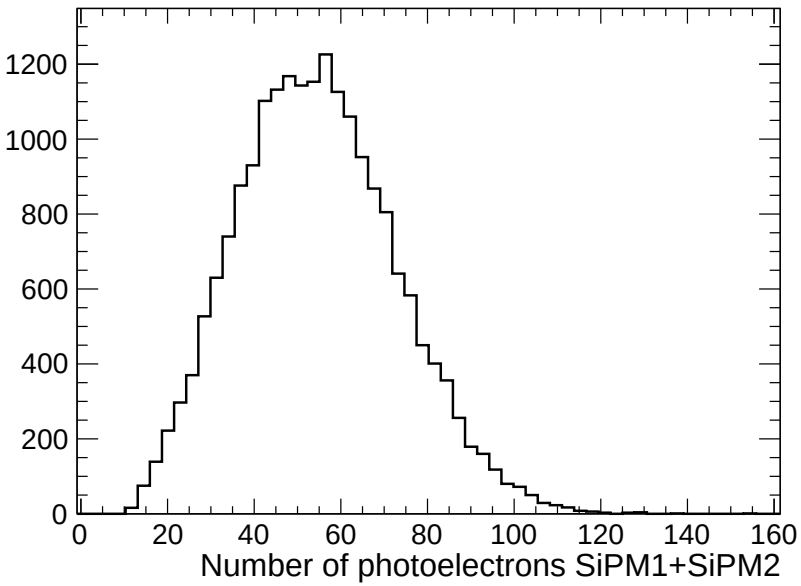
Source distribution, comparison between each SiPM and the sum





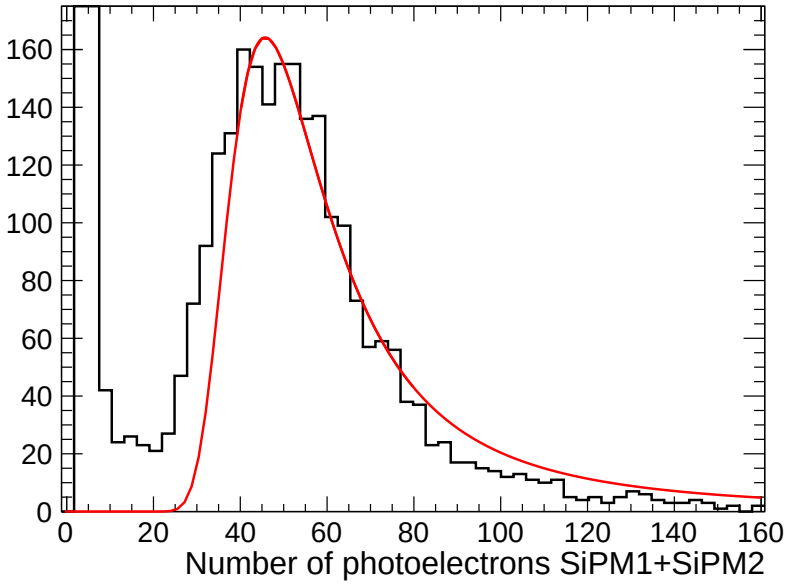
Cosmics and Source

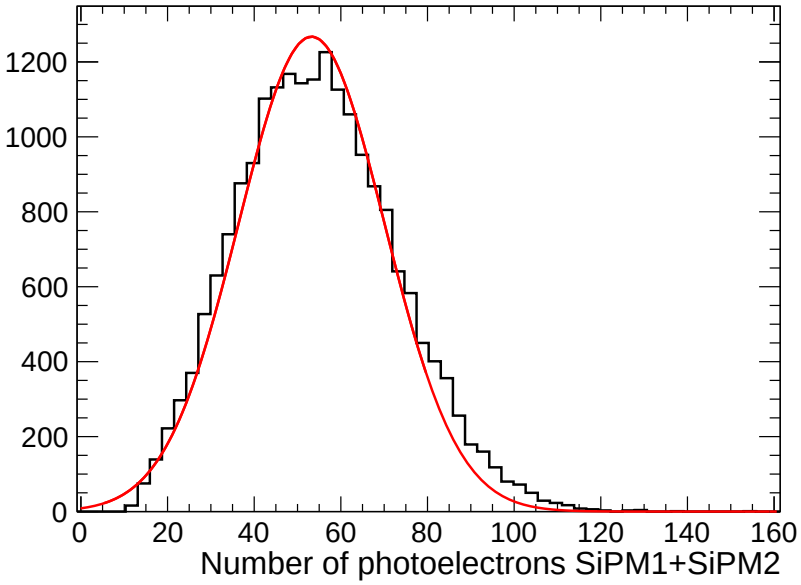




Raw distributions

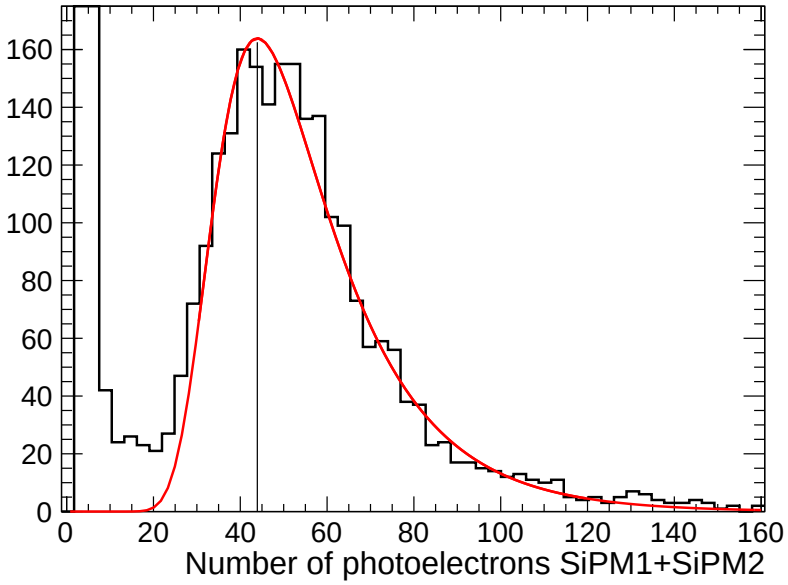
Cosmics and Source

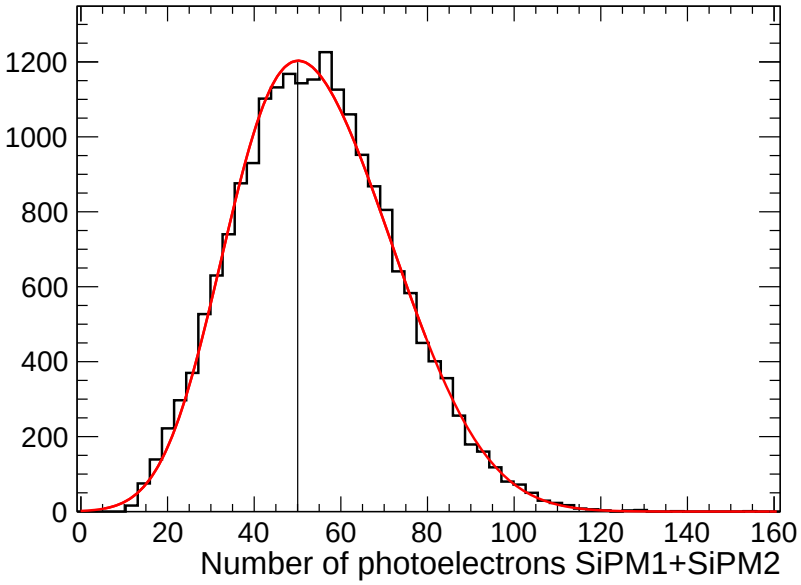




Built-in Landau for cosmics, Built-in Gaussian for source

Cosmics and Source





Gumbel for cosmics, modified Gaussian for source